

Mathematica 11.3 Integration Test Results

Test results for the 306 problems in "4.5.1.3 (d sin)^n (a+b sec)^m.m"

Problem 6: Result more than twice size of optimal antiderivative.

$$\int \text{Csc}[c + d x] (a + a \text{Sec}[c + d x]) dx$$

Optimal (type 3, 30 leaves, 6 steps):

$$\frac{a \text{Log}[1 - \text{Cos}[c + d x]]}{d} - \frac{a \text{Log}[\text{Cos}[c + d x]]}{d}$$

Result (type 3, 65 leaves):

$$-\frac{a \text{Log}[\text{Cos}[\frac{c}{2} + \frac{dx}{2}]]}{d} - \frac{a \text{Log}[\text{Cos}[c + d x]]}{d} + \frac{a \text{Log}[\text{Sin}[\frac{c}{2} + \frac{dx}{2}]]}{d} + \frac{a \text{Log}[\text{Sin}[c + d x]]}{d}$$

Problem 14: Result more than twice size of optimal antiderivative.

$$\int \text{Csc}[c + d x]^2 (a + a \text{Sec}[c + d x]) dx$$

Optimal (type 3, 37 leaves, 7 steps):

$$\frac{a \text{ArcTanh}[\text{Sin}[c + d x]]}{d} - \frac{a \text{Cot}[c + d x]}{d} - \frac{a \text{Csc}[c + d x]}{d}$$

Result (type 3, 106 leaves):

$$-\frac{a \text{Cot}[\frac{1}{2}(c + d x)]}{2d} - \frac{a \text{Cot}[c + d x]}{d} - \frac{a \text{Log}[\text{Cos}[\frac{1}{2}(c + d x)] - \text{Sin}[\frac{1}{2}(c + d x)]]}{d} + \frac{a \text{Log}[\text{Cos}[\frac{1}{2}(c + d x)] + \text{Sin}[\frac{1}{2}(c + d x)]]}{d} - \frac{a \text{Tan}[\frac{1}{2}(c + d x)]}{2d}$$

Problem 15: Result more than twice size of optimal antiderivative.

$$\int \text{Csc}[c + d x]^4 (a + a \text{Sec}[c + d x]) dx$$

Optimal (type 3, 69 leaves, 8 steps):

$$\frac{a \text{ArcTanh}[\text{Sin}[c + d x]]}{d} - \frac{a \text{Cot}[c + d x]}{d} - \frac{a \text{Cot}[c + d x]^3}{3d} - \frac{a \text{Csc}[c + d x]}{d} - \frac{a \text{Csc}[c + d x]^3}{3d}$$

Result (type 3, 190 leaves):

$$\begin{aligned} & - \frac{7 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{12 d} - \frac{2 a \operatorname{Cot}[c+d x]}{3 d} - \\ & \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{24 d} - \frac{a \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]^2}{3 d} - \\ & \frac{a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{d} + \frac{a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{d} - \\ & \frac{7 a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{12 d} - \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{24 d} \end{aligned}$$

Problem 16: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+d x]^6 (a+a \operatorname{Sec}[c+d x]) dx$$

Optimal (type 3, 101 leaves, 8 steps):

$$\begin{aligned} & \frac{a \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{d} - \frac{a \operatorname{Cot}[c+d x]}{d} - \frac{2 a \operatorname{Cot}[c+d x]^3}{3 d} - \\ & \frac{a \operatorname{Cot}[c+d x]^5}{5 d} - \frac{a \operatorname{Csc}[c+d x]}{d} - \frac{a \operatorname{Csc}[c+d x]^3}{3 d} - \frac{a \operatorname{Csc}[c+d x]^5}{5 d} \end{aligned}$$

Result (type 3, 272 leaves):

$$\begin{aligned} & - \frac{149 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{240 d} - \frac{8 a \operatorname{Cot}[c+d x]}{15 d} - \frac{29 a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2}{480 d} - \\ & \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^4}{160 d} - \frac{4 a \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]^2}{15 d} - \\ & \frac{a \operatorname{Cot}[c+d x] \operatorname{Csc}[c+d x]^4}{5 d} - \frac{a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{d} + \\ & \frac{a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{d} - \frac{149 a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{240 d} - \\ & \frac{29 a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{480 d} - \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{160 d} \end{aligned}$$

Problem 17: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+d x]^8 (a+a \operatorname{Sec}[c+d x]) dx$$

Optimal (type 3, 131 leaves, 8 steps):

$$\begin{aligned} & \frac{a \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{d} - \frac{a \operatorname{Cot}[c+d x]}{d} - \frac{a \operatorname{Cot}[c+d x]^3}{d} - \frac{3 a \operatorname{Cot}[c+d x]^5}{5 d} - \\ & \frac{a \operatorname{Cot}[c+d x]^7}{7 d} - \frac{a \operatorname{Csc}[c+d x]}{d} - \frac{a \operatorname{Csc}[c+d x]^3}{3 d} - \frac{a \operatorname{Csc}[c+d x]^5}{5 d} - \frac{a \operatorname{Csc}[c+d x]^7}{7 d} \end{aligned}$$

Result (type 3, 354 leaves):

$$\begin{aligned}
 & - \frac{2161 a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{3360 d} - \frac{16 a \operatorname{Cot}[c+dx]}{35 d} - \frac{481 a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{6720 d} - \\
 & \frac{3 a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{280 d} - \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^6}{896 d} - \\
 & \frac{8 a \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^2}{35 d} - \frac{6 a \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^4}{35 d} - \frac{a \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^6}{7 d} - \\
 & \frac{a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{d} + \frac{a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{d} - \\
 & \frac{2161 a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{3360 d} - \frac{481 a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{6720 d} - \\
 & \frac{3 a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{280 d} - \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^6 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{896 d}
 \end{aligned}$$

Problem 18: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+dx]^{10} (a + a \operatorname{Sec}[c+dx]) dx$$

Optimal (type 3, 165 leaves, 8 steps):

$$\begin{aligned}
 & \frac{a \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{d} - \frac{a \operatorname{Cot}[c+dx]}{d} - \frac{4 a \operatorname{Cot}[c+dx]^3}{3 d} - \frac{6 a \operatorname{Cot}[c+dx]^5}{5 d} - \frac{4 a \operatorname{Cot}[c+dx]^7}{7 d} - \\
 & \frac{a \operatorname{Cot}[c+dx]^9}{9 d} - \frac{a \operatorname{Csc}[c+dx]}{d} - \frac{a \operatorname{Csc}[c+dx]^3}{3 d} - \frac{a \operatorname{Csc}[c+dx]^5}{5 d} - \frac{a \operatorname{Csc}[c+dx]^7}{7 d} - \frac{a \operatorname{Csc}[c+dx]^9}{9 d}
 \end{aligned}$$

Result (type 3, 436 leaves):

$$\begin{aligned}
 & - \frac{53\,089 a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{80\,640 d} - \frac{128 a \operatorname{Cot}[c+dx]}{315 d} - \frac{12\,769 a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{161\,280 d} \\
 & - \frac{751 a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{53\,760 d} - \frac{71 a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^6}{32\,256 d} \\
 & - \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^8}{4608 d} - \frac{64 a \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^2}{315 d} \\
 & - \frac{16 a \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^4}{105 d} - \frac{8 a \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^6}{63 d} \\
 & - \frac{a \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^8}{9 d} - \frac{a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{d} + \\
 & - \frac{a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{d} - \frac{53\,089 a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{80\,640 d} \\
 & - \frac{12\,769 a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{161\,280 d} - \frac{751 a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{53\,760 d} \\
 & - \frac{71 a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^6 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{32\,256 d} - \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^8 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{4608 d}
 \end{aligned}$$

Problem 26: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+dx]^5 (a + a \operatorname{Sec}[c+dx])^2 dx$$

Optimal (type 3, 115 leaves, 5 steps):

$$\begin{aligned}
 & - \frac{a^4}{4 d (a - a \operatorname{Cos}[c+dx])^2} - \frac{5 a^3}{4 d (a - a \operatorname{Cos}[c+dx])} + \frac{17 a^2 \operatorname{Log}[1 - \operatorname{Cos}[c+dx]]}{8 d} \\
 & - \frac{2 a^2 \operatorname{Log}[\operatorname{Cos}[c+dx]]}{d} - \frac{a^2 \operatorname{Log}[1 + \operatorname{Cos}[c+dx]]}{8 d} + \frac{a^2 \operatorname{Sec}[c+dx]}{d}
 \end{aligned}$$

Result (type 3, 598 leaves):

$$\begin{aligned}
 & - \frac{5 \cos [c+d x]^2 \operatorname{Csc}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2}{32 d} - \\
 & \frac{\cos [c+d x]^2 \operatorname{Csc}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2}{64 d} - \\
 & \frac{\cos [c+d x]^2 \operatorname{Log}\left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]\right] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2}{16 d} - \\
 & \frac{\cos [c+d x]^2 \operatorname{Log}[\cos [c+d x]] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2}{2 d} + \\
 & \frac{17 \cos [c+d x]^2 \operatorname{Log}\left[\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2}{16 d} + \\
 & \frac{\cos [c+d x]^2 \operatorname{Sec}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2}{4 d} + \\
 & \frac{\cos [c+d x]^2 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 \sin \left[\frac{d x}{2}\right]}{4 d\left(\cos \left[\frac{c}{2}\right]-\sin \left[\frac{c}{2}\right]\right)\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)} - \\
 & \frac{\cos [c+d x]^2 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 \sin \left[\frac{d x}{2}\right]}{4 d\left(\cos \left[\frac{c}{2}\right]+\sin \left[\frac{c}{2}\right]\right)\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)} + \\
 & x \cos [c+d x]^2 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 \\
 & \left(-\frac{17}{32} \cot \left[\frac{c}{2}\right]+\frac{1}{32}(8+9 \cos [c]) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c]-\frac{1}{32} \tan \left[\frac{c}{2}\right]-\frac{\tan [c]}{2}\right)
 \end{aligned}$$

Problem 27: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+d x]^7 (a+a \operatorname{Sec}[c+d x])^2 dx$$

Optimal (type 3, 160 leaves, 5 steps):

$$\begin{aligned}
 & - \frac{a^5}{12 d (a-a \cos [c+d x])^3} - \frac{3 a^4}{8 d (a-a \cos [c+d x])^2} - \\
 & \frac{23 a^3}{16 d (a-a \cos [c+d x])} + \frac{a^3}{16 d (a+a \cos [c+d x])} + \frac{9 a^2 \operatorname{Log}[1-\cos [c+d x]]}{4 d} - \\
 & \frac{2 a^2 \operatorname{Log}[\cos [c+d x]]}{d} - \frac{a^2 \operatorname{Log}[1+\cos [c+d x]]}{4 d} + \frac{a^2 \operatorname{Sec}[c+d x]}{d}
 \end{aligned}$$

Result (type 3, 697 leaves):

$$\begin{aligned}
 & - \frac{23 \cos [c+d x]^2 \operatorname{Csc}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2}{128 d} - \\
 & \frac{3 \cos [c+d x]^2 \operatorname{Csc}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2}{128 d} - \\
 & \frac{\cos [c+d x]^2 \operatorname{Csc}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2}{384 d} - \\
 & \frac{\cos [c+d x]^2 \operatorname{Log}\left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]\right] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2}{8 d} - \\
 & \frac{\cos [c+d x]^2 \operatorname{Log}[\cos [c+d x]] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2}{2 d} + \\
 & \frac{9 \cos [c+d x]^2 \operatorname{Log}\left[\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2}{8 d} + \\
 & \frac{\cos [c+d x]^2 \operatorname{Sec}[c] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2}{4 d} + \\
 & \frac{\cos [c+d x]^2 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^2}{128 d} + \\
 & \frac{\cos [c+d x]^2 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 \sin \left[\frac{d x}{2}\right]}{4 d\left(\cos \left[\frac{c}{2}\right]-\sin \left[\frac{c}{2}\right]\right)\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)} - \\
 & \frac{\cos [c+d x]^2 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 \sin \left[\frac{d x}{2}\right]}{4 d\left(\cos \left[\frac{c}{2}\right]+\sin \left[\frac{c}{2}\right]\right)\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)} + \\
 & x \cos [c+d x]^2 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \operatorname{Sec}[c+d x])^2 \\
 & \left(-\frac{9}{16} \operatorname{Cot}\left[\frac{c}{2}\right]+\frac{1}{16}(4+5 \cos [c]) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c]-\frac{1}{16} \operatorname{Tan}\left[\frac{c}{2}\right]-\frac{\operatorname{Tan}[c]}{2}\right)
 \end{aligned}$$

Problem 32: Result more than twice size of optimal antiderivative.

$$\int (a+a \operatorname{Sec}[c+d x])^2 \sin [c+d x]^2 dx$$

Optimal (type 3, 73 leaves, 9 steps):

$$-\frac{a^2 x}{2} + \frac{2 a^2 \operatorname{ArcTanh}[\sin [c+d x]]}{d} - \frac{2 a^2 \sin [c+d x]}{d} - \frac{a^2 \cos [c+d x] \sin [c+d x]}{2 d} + \frac{a^2 \tan [c+d x]}{d}$$

Result (type 3, 243 leaves):

$$\frac{1}{16} a^2 (1 + \cos [c + d x])^2 \sec \left[\frac{1}{2} (c + d x) \right]^4$$

$$\left(-2 x - \frac{8 \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right]}{d} + \frac{8 \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right]}{d} - \frac{8 \cos [d x] \sin [c]}{d} - \frac{\cos [2 d x] \sin [2 c]}{d} - \frac{8 \cos [c] \sin [d x]}{d} - \frac{\cos [2 c] \sin [2 d x]}{d} + \frac{4 \sin \left[\frac{d x}{2} \right]}{d \left(\cos \left[\frac{c}{2} \right] - \sin \left[\frac{c}{2} \right] \right) \left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)} + \frac{4 \sin \left[\frac{d x}{2} \right]}{d \left(\cos \left[\frac{c}{2} \right] + \sin \left[\frac{c}{2} \right] \right) \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)} \right)$$

Problem 33: Result more than twice size of optimal antiderivative.

$$\int \csc [c + d x]^2 (a + a \sec [c + d x])^2 dx$$

Optimal (type 3, 57 leaves, 11 steps):

$$\frac{2 a^2 \operatorname{ArcTanh} [\sin [c + d x]]}{d} - \frac{2 a^2 \operatorname{Cot} [c + d x]}{d} - \frac{2 a^2 \csc [c + d x]}{d} + \frac{a^2 \tan [c + d x]}{d}$$

Result (type 3, 401 leaves):

$$-\frac{1}{2 d} \cos [c + d x]^2 \operatorname{Log} \left[\cos \left[\frac{c}{2} + \frac{d x}{2} \right] - \sin \left[\frac{c}{2} + \frac{d x}{2} \right] \right] \sec \left[\frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 +$$

$$\frac{1}{2 d} \cos [c + d x]^2 \operatorname{Log} \left[\cos \left[\frac{c}{2} + \frac{d x}{2} \right] + \sin \left[\frac{c}{2} + \frac{d x}{2} \right] \right] \sec \left[\frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 +$$

$$\frac{1}{2 d} \cos [c + d x]^2 \csc \left[\frac{c}{2} \right] \csc \left[\frac{c}{2} + \frac{d x}{2} \right] \sec \left[\frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 \sin \left[\frac{d x}{2} \right] +$$

$$\frac{\cos [c + d x]^2 \sec \left[\frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 \sin \left[\frac{d x}{2} \right]}{4 d \left(\cos \left[\frac{c}{2} \right] - \sin \left[\frac{c}{2} \right] \right) \left(\cos \left[\frac{c}{2} + \frac{d x}{2} \right] - \sin \left[\frac{c}{2} + \frac{d x}{2} \right] \right)} +$$

$$\frac{\cos [c + d x]^2 \sec \left[\frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 \sin \left[\frac{d x}{2} \right]}{4 d \left(\cos \left[\frac{c}{2} \right] + \sin \left[\frac{c}{2} \right] \right) \left(\cos \left[\frac{c}{2} + \frac{d x}{2} \right] + \sin \left[\frac{c}{2} + \frac{d x}{2} \right] \right)}$$

Problem 34: Result more than twice size of optimal antiderivative.

$$\int \csc [c + d x]^4 (a + a \sec [c + d x])^2 dx$$

Optimal (type 3, 87 leaves, 8 steps):

$$\frac{2 a^2 \operatorname{ArcTanh} [\sin [c + d x]]}{d} + \frac{10 a^2 \tan [c + d x]}{3 d} - \frac{2 a^2 \tan [c + d x]}{d (1 - \cos [c + d x])} - \frac{a^4 \tan [c + d x]}{3 d (a - a \cos [c + d x])^2}$$

Result (type 3, 228 leaves):

$$\frac{1}{24 d} a^2 (1 + \cos [c + d x])^2 \sec \left[\frac{1}{2} (c + d x) \right]^4$$

$$\left(-\cot \left[\frac{c}{2} \right] \csc \left[\frac{1}{2} (c + d x) \right]^2 - (-8 + 7 \cos [c + d x]) \csc \left[\frac{c}{2} \right] \csc \left[\frac{1}{2} (c + d x) \right]^3 \sin \left[\frac{d x}{2} \right] + \right.$$

$$6 \left(-2 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] + 2 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \right) +$$

$$\sin [d x] / \left(\left(\cos \left[\frac{c}{2} \right] - \sin \left[\frac{c}{2} \right] \right) \left(\cos \left[\frac{c}{2} \right] + \sin \left[\frac{c}{2} \right] \right) \right.$$

$$\left. \left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right) \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right) \right)$$

Problem 35: Result more than twice size of optimal antiderivative.

$$\int \csc [c + d x]^6 (a + a \sec [c + d x])^2 dx$$

Optimal (type 3, 129 leaves, 12 steps):

$$\frac{2 a^2 \operatorname{ArcTanh} \left[\sin [c + d x] \right]}{d} - \frac{4 a^2 \cot [c + d x]}{d} - \frac{5 a^2 \cot [c + d x]^3}{3 d} - \frac{2 a^2 \cot [c + d x]^5}{5 d} -$$

$$\frac{2 a^2 \csc [c + d x]}{d} - \frac{2 a^2 \csc [c + d x]^3}{3 d} - \frac{2 a^2 \csc [c + d x]^5}{5 d} + \frac{a^2 \tan [c + d x]}{d}$$

Result (type 3, 317 leaves):

$$\frac{1}{7680 d} a^2 \cos [c + d x] \sec \left[\frac{1}{2} (c + d x) \right]^4 (1 + \sec [c + d x])^2$$

$$\left(-3840 \cos [c + d x] \log \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] + \right.$$

$$3840 \cos [c + d x] \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] + \csc [2 c] \csc \left[\frac{1}{2} (c + d x) \right]^4$$

$$\csc [c + d x] \left(320 \sin [2 c] - 596 \sin [d x] + 864 \sin [2 d x] + 216 \sin [c - d x] - \right.$$

$$416 \sin [c + d x] + 624 \sin [2 (c + d x)] - 416 \sin [3 (c + d x)] + 104 \sin [4 (c + d x)] -$$

$$596 \sin [2 c + d x] - 680 \sin [3 c + d x] + 894 \sin [c + 2 d x] + 224 \sin [2 (c + 2 d x)] +$$

$$894 \sin [3 c + 2 d x] + 480 \sin [4 c + 2 d x] - 776 \sin [c + 3 d x] - 596 \sin [2 c + 3 d x] -$$

$$\left. \left. 596 \sin [4 c + 3 d x] - 120 \sin [5 c + 3 d x] + 149 \sin [3 c + 4 d x] + 149 \sin [5 c + 4 d x] \right) \right)$$

Problem 36: Result more than twice size of optimal antiderivative.

$$\int \csc [c + d x]^8 (a + a \sec [c + d x])^2 dx$$

Optimal (type 3, 163 leaves, 12 steps):

$$\frac{2 a^2 \operatorname{ArcTanh}[\sin [c+d x]]}{d} - \frac{5 a^2 \operatorname{Cot}[c+d x]}{d} - \frac{3 a^2 \operatorname{Cot}[c+d x]^3}{d} - \frac{7 a^2 \operatorname{Cot}[c+d x]^5}{d} - \frac{2 a^2 \operatorname{Cot}[c+d x]^7}{d} - \frac{2 a^2 \operatorname{Csc}[c+d x]}{d} - \frac{2 a^2 \operatorname{Csc}[c+d x]^3}{3 d} - \frac{2 a^2 \operatorname{Csc}[c+d x]^5}{5 d} - \frac{2 a^2 \operatorname{Csc}[c+d x]^7}{7 d} + \frac{a^2 \operatorname{Tan}[c+d x]}{d}$$

Result (type 3, 428 leaves):

$$\frac{1}{13762560 d} a^2 \cos [c+d x] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^4 (1+\operatorname{Sec}[c+d x])^2 \left(-6881280 \cos [c+d x] \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right]+6881280 \cos [c+d x] \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right]-32 \operatorname{Csc}[2 c] \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^4 \operatorname{Csc}[c+d x]^3 (-9856 \sin [2 c]+17288 \sin [d x]-29056 \sin [2 d x]-7264 \sin [c-d x]+14208 \sin [c+d x]-19536 \sin [2(c+d x)]+7104 \sin [3(c+d x)]+7104 \sin [4(c+d x)]-7104 \sin [5(c+d x)]+1776 \sin [6(c+d x)]+17288 \sin [2 c+d x]+20384 \sin [3 c+d x]-23771 \sin [c+2 d x]+7104 \sin [2(c+2 d x)]-23771 \sin [3 c+2 d x]-8960 \sin [4 c+2 d x]+19984 \sin [c+3 d x]+8644 \sin [2 c+3 d x]+8644 \sin [4 c+3 d x]-6160 \sin [5 c+3 d x]+8644 \sin [3 c+4 d x]+8644 \sin [5 c+4 d x]+6720 \sin [6 c+4 d x]-12144 \sin [3 c+5 d x]-8644 \sin [4 c+5 d x]-8644 \sin [6 c+5 d x]-1680 \sin [7 c+5 d x]+3456 \sin [4 c+6 d x]+2161 \sin [5 c+6 d x]+2161 \sin [7 c+6 d x])\right)$$

Problem 37: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+d x]^{10} (a+a \operatorname{Sec}[c+d x])^2 dx$$

Optimal (type 3, 201 leaves, 12 steps):

$$\frac{2 a^2 \operatorname{ArcTanh}[\sin [c+d x]]}{d} - \frac{6 a^2 \operatorname{Cot}[c+d x]}{d} - \frac{14 a^2 \operatorname{Cot}[c+d x]^3}{3 d} - \frac{16 a^2 \operatorname{Cot}[c+d x]^5}{5 d} - \frac{9 a^2 \operatorname{Cot}[c+d x]^7}{7 d} - \frac{2 a^2 \operatorname{Cot}[c+d x]^9}{9 d} - \frac{2 a^2 \operatorname{Csc}[c+d x]}{d} - \frac{2 a^2 \operatorname{Csc}[c+d x]^3}{3 d} - \frac{2 a^2 \operatorname{Csc}[c+d x]^5}{5 d} - \frac{2 a^2 \operatorname{Csc}[c+d x]^7}{7 d} - \frac{2 a^2 \operatorname{Csc}[c+d x]^9}{9 d} + \frac{a^2 \operatorname{Tan}[c+d x]}{d}$$

Result (type 3, 1050 leaves):

$$\begin{aligned}
& - \frac{1}{80640 d} 6899 \cos [c+d x]^2 \cot \left[\frac{c}{2}\right] \csc \left[\frac{c}{2}+\frac{d x}{2}\right]^2 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 - \\
& \frac{1}{13440 d} 193 \cos [c+d x]^2 \cot \left[\frac{c}{2}\right] \csc \left[\frac{c}{2}+\frac{d x}{2}\right]^4 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 - \\
& \frac{1}{32256 d} 71 \cos [c+d x]^2 \cot \left[\frac{c}{2}\right] \csc \left[\frac{c}{2}+\frac{d x}{2}\right]^6 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 - \\
& \frac{\cos [c+d x]^2 \cot \left[\frac{c}{2}\right] \csc \left[\frac{c}{2}+\frac{d x}{2}\right]^8 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2}{4608 d} - \frac{1}{2 d} \\
& \cos [c+d x]^2 \log \left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 + \frac{1}{2 d} \\
& \cos [c+d x]^2 \log \left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 + \frac{1}{161280 d} \\
& 123041 \cos [c+d x]^2 \csc \left[\frac{c}{2}\right] \csc \left[\frac{c}{2}+\frac{d x}{2}\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 \sin \left[\frac{d x}{2}\right] + \\
& \frac{1}{80640 d} 6899 \cos [c+d x]^2 \csc \left[\frac{c}{2}\right] \csc \left[\frac{c}{2}+\frac{d x}{2}\right]^3 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 \sin \left[\frac{d x}{2}\right] + \\
& \frac{1}{13440 d} 193 \cos [c+d x]^2 \csc \left[\frac{c}{2}\right] \csc \left[\frac{c}{2}+\frac{d x}{2}\right]^5 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 \sin \left[\frac{d x}{2}\right] + \\
& \frac{1}{32256 d} 71 \cos [c+d x]^2 \csc \left[\frac{c}{2}\right] \csc \left[\frac{c}{2}+\frac{d x}{2}\right]^7 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 \sin \left[\frac{d x}{2}\right] + \\
& \frac{1}{4608 d} \cos [c+d x]^2 \csc \left[\frac{c}{2}\right] \csc \left[\frac{c}{2}+\frac{d x}{2}\right]^9 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 \sin \left[\frac{d x}{2}\right] + \\
& \frac{803 \cos [c+d x]^2 \sec \left[\frac{c}{2}\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^5 (a+a \sec [c+d x])^2 \sin \left[\frac{d x}{2}\right]}{7680 d} + \\
& \frac{49 \cos [c+d x]^2 \sec \left[\frac{c}{2}\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^7 (a+a \sec [c+d x])^2 \sin \left[\frac{d x}{2}\right]}{7680 d} + \\
& \frac{\cos [c+d x]^2 \sec \left[\frac{c}{2}\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^9 (a+a \sec [c+d x])^2 \sin \left[\frac{d x}{2}\right]}{2560 d} + \\
& \frac{\cos [c+d x] \sec [c] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 \sin [d x]}{4 d} + \\
& \frac{49 \cos [c+d x]^2 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^2 \tan \left[\frac{c}{2}\right]}{7680 d} + \\
& \frac{\cos [c+d x]^2 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^2 \tan \left[\frac{c}{2}\right]}{2560 d}
\end{aligned}$$

Problem 46: Result more than twice size of optimal antiderivative.

$$\int \csc [c+d x]^7 (a+a \sec [c+d x])^3 dx$$

Optimal (type 3, 157 leaves, 5 steps):

$$\begin{aligned}
 & - \frac{a^6}{6d(a - a \cos[c + dx])^3} - \frac{7a^5}{8d(a - a \cos[c + dx])^2} - \\
 & \frac{31a^4}{8d(a - a \cos[c + dx])} + \frac{111a^3 \log[1 - \cos[c + dx]]}{16d} - \frac{7a^3 \log[\cos[c + dx]]}{d} + \\
 & \frac{a^3 \log[1 + \cos[c + dx]]}{16d} + \frac{3a^3 \sec[c + dx]}{d} + \frac{a^3 \sec[c + dx]^2}{2d}
 \end{aligned}$$

Result (type 3, 799 leaves):

$$\begin{aligned}
 & - \frac{31 \cos[c + dx]^3 \operatorname{Csc}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3}{128d} - \\
 & \frac{7 \cos[c + dx]^3 \operatorname{Csc}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3}{256d} - \\
 & \frac{\cos[c + dx]^3 \operatorname{Csc}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3}{384d} + \\
 & \frac{\cos[c + dx]^3 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3}{64d} - \\
 & \frac{7 \cos[c + dx]^3 \log[\cos[c + dx]] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3}{8d} + \frac{1}{64d} \\
 & \frac{111 \cos[c + dx]^3 \log\left[\sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3}{8d} + \\
 & \frac{3 \cos[c + dx]^3 \sec[c] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3}{8d} + \\
 & \frac{\cos[c + dx]^3 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3}{32d \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right)^2} + \\
 & \frac{3 \cos[c + dx]^3 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 \sin\left[\frac{dx}{2}\right]}{8d \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} + \\
 & \frac{\cos[c + dx]^3 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3}{32d \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right)^2} - \\
 & \frac{3 \cos[c + dx]^3 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 \sin\left[\frac{dx}{2}\right]}{8d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} + \\
 & x \cos[c + dx]^3 \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a + a \sec[c + dx])^3 \\
 & \left(-\frac{111}{128} \cot\left[\frac{c}{2}\right] + \frac{1}{128} (56 + 55 \cos[c]) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \sec[c] + \frac{1}{128} \tan\left[\frac{c}{2}\right] - \frac{7 \tan[c]}{8}\right)
 \end{aligned}$$

Problem 51: Result more than twice size of optimal antiderivative.

$$\int (a + a \operatorname{Sec}[c + d x])^3 \operatorname{Sin}[c + d x]^2 dx$$

Optimal (type 3, 98 leaves, 11 steps):

$$-\frac{5 a^3 x}{2} + \frac{5 a^3 \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{2 d} - \frac{3 a^3 \operatorname{Sin}[c + d x]}{d} - \frac{a^3 \operatorname{Cos}[c + d x] \operatorname{Sin}[c + d x]}{2 d} + \frac{3 a^3 \operatorname{Tan}[c + d x]}{d} + \frac{a^3 \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{2 d}$$

Result (type 3, 300 leaves):

$$\frac{1}{32} a^3 (1 + \operatorname{Cos}[c + d x])^3 \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^6 \left(-10 x - \frac{10 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]}{d} + \frac{10 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right]}{d} - \frac{12 \operatorname{Cos}[d x] \operatorname{Sin}[c]}{d} - \frac{\operatorname{Cos}[2 d x] \operatorname{Sin}[2 c]}{d} - \frac{12 \operatorname{Cos}[c] \operatorname{Sin}[d x]}{d} - \frac{\operatorname{Cos}[2 c] \operatorname{Sin}[2 d x]}{d} + \frac{1}{d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} + \frac{12 \operatorname{Sin}\left[\frac{d x}{2}\right]}{d \left(\operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right]\right) \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)} - \frac{1}{d \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} + \frac{12 \operatorname{Sin}\left[\frac{d x}{2}\right]}{d \left(\operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right]\right) \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)} \right)$$

Problem 52: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c + d x]^2 (a + a \operatorname{Sec}[c + d x])^3 dx$$

Optimal (type 3, 80 leaves, 9 steps):

$$\frac{9 a^3 \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{2 d} - \frac{4 a^3 \operatorname{Sin}[c + d x]}{d (1 - \operatorname{Cos}[c + d x])} + \frac{3 a^3 \operatorname{Tan}[c + d x]}{d} + \frac{a^3 \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{2 d}$$

Result (type 3, 244 leaves):

$$\frac{1}{32 d} a^3 (1 + \cos [c + d x])^3 \sec \left[\frac{1}{2} (c + d x) \right]^6$$

$$\left(-18 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] + 18 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \right) +$$

$$16 \operatorname{Csc} \left[\frac{c}{2} \right] \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right] \sin \left[\frac{d x}{2} \right] + \frac{1}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} -$$

$$\frac{1}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} +$$

$$(12 \sin [d x]) / \left(\left(\cos \left[\frac{c}{2} \right] - \sin \left[\frac{c}{2} \right] \right) \left(\cos \left[\frac{c}{2} \right] + \sin \left[\frac{c}{2} \right] \right) \right.$$

$$\left. \left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right) \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right) \right)$$

Problem 53: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c + d x]^4 (a + a \operatorname{Sec}[c + d x])^3 dx$$

Optimal (type 3, 110 leaves, 11 steps):

$$\frac{11 a^3 \operatorname{ArcTanh}[\sin [c + d x]]}{2 d} - \frac{2 a^3 \sin [c + d x]}{3 d (1 - \cos [c + d x])^2} -$$

$$\frac{17 a^3 \sin [c + d x]}{3 d (1 - \cos [c + d x])} + \frac{3 a^3 \tan [c + d x]}{d} + \frac{a^3 \operatorname{Sec}[c + d x] \tan [c + d x]}{2 d}$$

Result (type 3, 678 leaves):

$$\begin{aligned}
 & -\frac{1}{24 d} \cos [c+d x]^3 \cot \left[\frac{c}{2}\right] \operatorname{Csc}\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 -\frac{1}{16 d} \\
 & 11 \cos [c+d x]^3 \operatorname{Log}\left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 + \\
 & \frac{1}{16 d} 11 \cos [c+d x]^3 \operatorname{Log}\left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 + \\
 & \frac{1}{24 d} 17 \cos [c+d x]^3 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Csc}\left[\frac{c}{2}+\frac{d x}{2}\right] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 \sin \left[\frac{d x}{2}\right] + \\
 & \frac{1}{24 d} \cos [c+d x]^3 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Csc}\left[\frac{c}{2}+\frac{d x}{2}\right]^3 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 \sin \left[\frac{d x}{2}\right] + \\
 & \frac{\cos [c+d x]^3 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3}{32 d\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)^2} + \\
 & \frac{3 \cos [c+d x]^3 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 \sin \left[\frac{d x}{2}\right]}{8 d\left(\cos \left[\frac{c}{2}\right]-\sin \left[\frac{c}{2}\right]\right)\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)} - \\
 & \frac{\cos [c+d x]^3 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3}{32 d\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)^2} + \\
 & \frac{3 \cos [c+d x]^3 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \operatorname{Sec}[c+d x])^3 \sin \left[\frac{d x}{2}\right]}{8 d\left(\cos \left[\frac{c}{2}\right]+\sin \left[\frac{c}{2}\right]\right)\left(\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right)}
 \end{aligned}$$

Problem 54: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+d x]^6 (a+a \operatorname{Sec}[c+d x])^3 dx$$

Optimal (type 3, 165 leaves, 10 steps):

$$\begin{aligned}
 & \frac{13 a^3 \operatorname{ArcTanh}[\sin [c+d x]]}{2 d} + \frac{152 a^3 \tan [c+d x]}{15 d} + \frac{13 a^3 \operatorname{Sec}[c+d x] \tan [c+d x]}{2 d} - \\
 & \frac{a^6 \operatorname{Sec}[c+d x] \tan [c+d x]}{5 d(a-a \cos [c+d x])^3} - \frac{11 a^5 \operatorname{Sec}[c+d x] \tan [c+d x]}{15 d(a-a \cos [c+d x])^2} - \frac{76 a^6 \operatorname{Sec}[c+d x] \tan [c+d x]}{15 d\left(a^3-a^3 \cos [c+d x]\right)}
 \end{aligned}$$

Result (type 3, 353 leaves):

$$\begin{aligned}
 & -\frac{1}{30720d} a^3 (1 + \cos [c + dx])^3 \sec \left[\frac{1}{2} (c + dx) \right]^6 \\
 & \sec [c + dx]^2 \left(24960 \cos [c + dx]^2 \left(\log \left[\cos \left[\frac{1}{2} (c + dx) \right] - \sin \left[\frac{1}{2} (c + dx) \right] \right] \right) - \right. \\
 & \quad \left. \log \left[\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right] \right) + \csc \left[\frac{c}{2} \right] \csc \left[\frac{1}{2} (c + dx) \right]^5 \sec [c] \\
 & \left(-1235 \sin \left[\frac{dx}{2} \right] + 3805 \sin \left[\frac{3dx}{2} \right] + 4329 \sin \left[c - \frac{dx}{2} \right] - 1989 \sin \left[c + \frac{dx}{2} \right] - \right. \\
 & \quad 3575 \sin \left[2c + \frac{dx}{2} \right] + 475 \sin \left[c + \frac{3dx}{2} \right] + 2005 \sin \left[2c + \frac{3dx}{2} \right] + 2275 \sin \left[3c + \frac{3dx}{2} \right] - \\
 & \quad 2673 \sin \left[c + \frac{5dx}{2} \right] + 105 \sin \left[2c + \frac{5dx}{2} \right] - 1593 \sin \left[3c + \frac{5dx}{2} \right] - 975 \sin \left[4c + \frac{5dx}{2} \right] + \\
 & \quad 1325 \sin \left[2c + \frac{7dx}{2} \right] - 255 \sin \left[3c + \frac{7dx}{2} \right] + 875 \sin \left[4c + \frac{7dx}{2} \right] + 195 \sin \left[5c + \frac{7dx}{2} \right] - \\
 & \quad \left. \left. 304 \sin \left[3c + \frac{9dx}{2} \right] + 90 \sin \left[4c + \frac{9dx}{2} \right] - 214 \sin \left[5c + \frac{9dx}{2} \right] \right) \right)
 \end{aligned}$$

Problem 55: Result more than twice size of optimal antiderivative.

$$\int \csc [c + dx]^8 (a + a \sec [c + dx])^3 dx$$

Optimal (type 3, 192 leaves, 17 steps):

$$\begin{aligned}
 & \frac{15 a^3 \operatorname{ArcTanh}[\sin [c + dx]]}{2 d} - \frac{13 a^3 \cot [c + dx]}{d} - \frac{7 a^3 \cot [c + dx]^3}{d} - \\
 & \frac{3 a^3 \cot [c + dx]^5}{d} - \frac{4 a^3 \cot [c + dx]^7}{7 d} - \frac{15 a^3 \csc [c + dx]}{2 d} - \frac{5 a^3 \csc [c + dx]^3}{2 d} - \\
 & \frac{3 a^3 \csc [c + dx]^5}{2 d} - \frac{15 a^3 \csc [c + dx]^7}{14 d} + \frac{a^3 \csc [c + dx]^7 \sec [c + dx]^2}{2 d} + \frac{3 a^3 \tan [c + dx]}{d}
 \end{aligned}$$

Result (type 3, 430 leaves):

$$\begin{aligned}
 & \frac{1}{917504d} a^3 \cos [c + dx] \sec \left[\frac{1}{2} (c + dx) \right]^6 (1 + \sec [c + dx])^3 \\
 & \left(-860160 \cos [c + dx]^2 \log \left[\cos \left[\frac{1}{2} (c + dx) \right] - \sin \left[\frac{1}{2} (c + dx) \right] \right] + \right. \\
 & \quad 860160 \cos [c + dx]^2 \log \left[\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right] - \\
 & \quad 8 \csc [2c] \csc \left[\frac{1}{2} (c + dx) \right]^6 \csc [c + dx] (5264 \sin [2c] - 9580 \sin [dx] + 8480 \sin [2dx] + \\
 & \quad 2776 \sin [c - dx] - 6080 \sin [c + dx] + 8816 \sin [2(c + dx)] - 7904 \sin [3(c + dx)] + \\
 & \quad 4864 \sin [4(c + dx)] - 1824 \sin [5(c + dx)] + 304 \sin [6(c + dx)] - 9580 \sin [2c + dx] - \\
 & \quad 10024 \sin [3c + dx] + 13891 \sin [c + 2dx] + 7720 \sin [2(c + 2dx)] + 13891 \sin [3c + 2dx] + \\
 & \quad 10080 \sin [4c + 2dx] - 10060 \sin [c + 3dx] - 12454 \sin [2c + 3dx] - \\
 & \quad 12454 \sin [4c + 3dx] - 6580 \sin [5c + 3dx] + 7664 \sin [3c + 4dx] + 7664 \sin [5c + 4dx] + \\
 & \quad 2520 \sin [6c + 4dx] - 3420 \sin [3c + 5dx] - 2874 \sin [4c + 5dx] - 2874 \sin [6c + 5dx] - \\
 & \quad \left. \left. 420 \sin [7c + 5dx] + 640 \sin [4c + 6dx] + 479 \sin [5c + 6dx] + 479 \sin [7c + 6dx] \right) \right)
 \end{aligned}$$

Problem 56: Result more than twice size of optimal antiderivative.

$$\int \text{Csc}[c + dx]^{10} (a + a \text{Sec}[c + dx])^3 dx$$

Optimal (type 3, 232 leaves, 17 steps):

$$\frac{17 a^3 \text{ArcTanh}[\text{Sin}[c + dx]]}{2 d} - \frac{16 a^3 \text{Cot}[c + dx]}{d} - \frac{34 a^3 \text{Cot}[c + dx]^3}{3 d} - \frac{36 a^3 \text{Cot}[c + dx]^5}{5 d} - \frac{19 a^3 \text{Cot}[c + dx]^7}{7 d} - \frac{4 a^3 \text{Cot}[c + dx]^9}{9 d} - \frac{17 a^3 \text{Csc}[c + dx]}{2 d} - \frac{17 a^3 \text{Csc}[c + dx]^3}{6 d} - \frac{17 a^3 \text{Csc}[c + dx]^5}{10 d} - \frac{17 a^3 \text{Csc}[c + dx]^7}{14 d} - \frac{17 a^3 \text{Csc}[c + dx]^9}{18 d} + \frac{a^3 \text{Csc}[c + dx]^9 \text{Sec}[c + dx]^2}{2 d} + \frac{3 a^3 \text{Tan}[c + dx]}{d}$$

Result (type 3, 1000 leaves):

$$\begin{aligned}
 & - \frac{1}{80640 d} 9833 \cos [c+d x]^3 \cot \left[\frac{c}{2}\right] \csc \left[\frac{c}{2}+\frac{d x}{2}\right]^2 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 - \\
 & \frac{1}{53760 d} 979 \cos [c+d x]^3 \cot \left[\frac{c}{2}\right] \csc \left[\frac{c}{2}+\frac{d x}{2}\right]^4 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 - \\
 & \frac{1}{2016 d} 5 \cos [c+d x]^3 \cot \left[\frac{c}{2}\right] \csc \left[\frac{c}{2}+\frac{d x}{2}\right]^6 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 - \\
 & \frac{\cos [c+d x]^3 \cot \left[\frac{c}{2}\right] \csc \left[\frac{c}{2}+\frac{d x}{2}\right]^8 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3}{4608 d} - \frac{1}{16 d} \\
 & 17 \cos [c+d x]^3 \log \left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 + \frac{1}{16 d} \\
 & 17 \cos [c+d x]^3 \log \left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 + \frac{1}{161280 d} \\
 & 197147 \cos [c+d x]^3 \csc \left[\frac{c}{2}\right] \csc \left[\frac{c}{2}+\frac{d x}{2}\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 \sin \left[\frac{d x}{2}\right] + \\
 & \frac{1}{80640 d} 9833 \cos [c+d x]^3 \csc \left[\frac{c}{2}\right] \csc \left[\frac{c}{2}+\frac{d x}{2}\right]^3 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 \sin \left[\frac{d x}{2}\right] + \\
 & \frac{1}{53760 d} 979 \cos [c+d x]^3 \csc \left[\frac{c}{2}\right] \csc \left[\frac{c}{2}+\frac{d x}{2}\right]^5 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 \sin \left[\frac{d x}{2}\right] + \\
 & \frac{1}{2016 d} 5 \cos [c+d x]^3 \csc \left[\frac{c}{2}\right] \csc \left[\frac{c}{2}+\frac{d x}{2}\right]^7 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 \sin \left[\frac{d x}{2}\right] + \\
 & \frac{1}{4608 d} \cos [c+d x]^3 \csc \left[\frac{c}{2}\right] \csc \left[\frac{c}{2}+\frac{d x}{2}\right]^9 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 \sin \left[\frac{d x}{2}\right] - \\
 & \frac{35 \cos [c+d x]^3 \sec \left[\frac{c}{2}\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^7 (a+a \sec [c+d x])^3 \sin \left[\frac{d x}{2}\right]}{1536 d} - \\
 & \frac{\cos [c+d x]^3 \sec \left[\frac{c}{2}\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^9 (a+a \sec [c+d x])^3 \sin \left[\frac{d x}{2}\right]}{1536 d} + \\
 & \frac{\cos [c+d x] \sec [c] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 \sin [d x]}{16 d} + \frac{1}{16 d} \\
 & \cos [c+d x]^2 \sec [c] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 (\sin [c]+6 \sin [d x]) - \\
 & \frac{\cos [c+d x]^3 \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^8 (a+a \sec [c+d x])^3 \tan \left[\frac{c}{2}\right]}{1536 d}
 \end{aligned}$$

Problem 70: Result more than twice size of optimal antiderivative.

$$\int \frac{\csc [c+d x]^4}{a+a \sec [c+d x]} dx$$

Optimal (type 3, 55 leaves, 7 steps):

$$\frac{\cot [c+d x]^3}{3 a d} + \frac{\cot [c+d x]^5}{5 a d} - \frac{\csc [c+d x]^5}{5 a d}$$

Result (type 3, 116 leaves):

$$- \left(\left(\text{Csc}[c] \text{Csc}[c+dx]^3 \text{Sec}[c+dx] \left(240 \text{Sin}[c] - 96 \text{Sin}[dx] - 54 \text{Sin}[c+dx] - 18 \text{Sin}[2(c+dx)] + 18 \text{Sin}[3(c+dx)] + 9 \text{Sin}[4(c+dx)] - 32 \text{Sin}[c+2dx] + 32 \text{Sin}[2c+3dx] + 16 \text{Sin}[3c+4dx] \right) \right) / \left(960 a d (1 + \text{Sec}[c+dx]) \right) \right)$$

Problem 71: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Csc}[c+dx]^6}{a+a \text{Sec}[c+dx]} dx$$

Optimal (type 3, 73 leaves, 7 steps):

$$\frac{\text{Cot}[c+dx]^3}{3ad} + \frac{2 \text{Cot}[c+dx]^5}{5ad} + \frac{\text{Cot}[c+dx]^7}{7ad} - \frac{\text{Csc}[c+dx]^7}{7ad}$$

Result (type 3, 158 leaves):

$$\frac{1}{53760 a d (1 + \text{Sec}[c+dx])} \text{Csc}[c] \text{Csc}[c+dx]^5 \text{Sec}[c+dx] \left(-8960 \text{Sin}[c] + 2560 \text{Sin}[dx] + 1500 \text{Sin}[c+dx] + 375 \text{Sin}[2(c+dx)] - 750 \text{Sin}[3(c+dx)] - 300 \text{Sin}[4(c+dx)] + 150 \text{Sin}[5(c+dx)] + 75 \text{Sin}[6(c+dx)] + 640 \text{Sin}[c+2dx] - 1280 \text{Sin}[2c+3dx] - 512 \text{Sin}[3c+4dx] + 256 \text{Sin}[4c+5dx] + 128 \text{Sin}[5c+6dx] \right)$$

Problem 72: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Csc}[c+dx]^8}{a+a \text{Sec}[c+dx]} dx$$

Optimal (type 3, 91 leaves, 7 steps):

$$\frac{\text{Cot}[c+dx]^3}{3ad} + \frac{3 \text{Cot}[c+dx]^5}{5ad} + \frac{3 \text{Cot}[c+dx]^7}{7ad} + \frac{\text{Cot}[c+dx]^9}{9ad} - \frac{\text{Csc}[c+dx]^9}{9ad}$$

Result (type 3, 200 leaves):

$$\frac{1}{5160960 a d (1 + \text{Sec}[c+dx])} \text{Csc}[c] \text{Csc}[c+dx]^7 \text{Sec}[c+dx] \left(645120 \text{Sin}[c] - 143360 \text{Sin}[dx] - 85750 \text{Sin}[c+dx] - 17150 \text{Sin}[2(c+dx)] + 51450 \text{Sin}[3(c+dx)] + 17150 \text{Sin}[4(c+dx)] - 17150 \text{Sin}[5(c+dx)] - 7350 \text{Sin}[6(c+dx)] + 2450 \text{Sin}[7(c+dx)] + 1225 \text{Sin}[8(c+dx)] - 28672 \text{Sin}[c+2dx] + 86016 \text{Sin}[2c+3dx] + 28672 \text{Sin}[3c+4dx] - 28672 \text{Sin}[4c+5dx] - 12288 \text{Sin}[5c+6dx] + 4096 \text{Sin}[6c+7dx] + 2048 \text{Sin}[7c+8dx] \right)$$

Problem 73: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Csc}[c+dx]^{10}}{a+a \text{Sec}[c+dx]} dx$$

Optimal (type 3, 109 leaves, 7 steps):

$$\frac{\text{Cot}[c+dx]^3}{3ad} + \frac{4 \text{Cot}[c+dx]^5}{5ad} + \frac{6 \text{Cot}[c+dx]^7}{7ad} + \frac{4 \text{Cot}[c+dx]^9}{9ad} + \frac{\text{Cot}[c+dx]^{11}}{11ad} - \frac{\text{Csc}[c+dx]^{11}}{11ad}$$

Result (type 3, 242 leaves):

$$\frac{1}{454164480 a d (1 + \operatorname{Sec}[c + d x])}$$

$$\operatorname{Csc}[c] \operatorname{Csc}[c + d x]^9 \operatorname{Sec}[c + d x] \left(-45416448 \operatorname{Sin}[c] + 8257536 \operatorname{Sin}[d x] + 5000940 \operatorname{Sin}[c + d x] + 833490 \operatorname{Sin}[2(c + d x)] - 3333960 \operatorname{Sin}[3(c + d x)] - 952560 \operatorname{Sin}[4(c + d x)] + 1428840 \operatorname{Sin}[5(c + d x)] + 535815 \operatorname{Sin}[6(c + d x)] - 357210 \operatorname{Sin}[7(c + d x)] - 158760 \operatorname{Sin}[8(c + d x)] + 39690 \operatorname{Sin}[9(c + d x)] + 19845 \operatorname{Sin}[10(c + d x)] + 1376256 \operatorname{Sin}[c + 2 d x] - 5505024 \operatorname{Sin}[2c + 3 d x] - 1572864 \operatorname{Sin}[3c + 4 d x] + 2359296 \operatorname{Sin}[4c + 5 d x] + 884736 \operatorname{Sin}[5c + 6 d x] - 589824 \operatorname{Sin}[6c + 7 d x] - 262144 \operatorname{Sin}[7c + 8 d x] + 65536 \operatorname{Sin}[8c + 9 d x] + 32768 \operatorname{Sin}[9c + 10 d x] \right)$$

Problem 99: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Csc}[c + d x]^5}{(a + a \operatorname{Sec}[c + d x])^3} dx$$

Optimal (type 3, 128 leaves, 6 steps):

$$\frac{3 \operatorname{ArcTanh}[\operatorname{Cos}[c + d x]]}{128 a^3 d} - \frac{1}{128 a d (a - a \operatorname{Cos}[c + d x])^2} - \frac{a^2}{40 d (a + a \operatorname{Cos}[c + d x])^5} + \frac{3 a}{64 d (a + a \operatorname{Cos}[c + d x])^4} - \frac{1}{64 a d (a + a \operatorname{Cos}[c + d x])^2} - \frac{3}{128 d (a^3 + a^3 \operatorname{Cos}[c + d x])}$$

Result (type 3, 412 leaves):

$$\frac{\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Sec}[c + d x]^3}{32 d (a + a \operatorname{Sec}[c + d x])^3} - \frac{3 \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \operatorname{Sec}[c + d x]^3}{32 d (a + a \operatorname{Sec}[c + d x])^3} - \frac{\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Cot}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \operatorname{Sec}[c + d x]^3}{64 d (a + a \operatorname{Sec}[c + d x])^3} + \frac{3 \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]\right] \operatorname{Sec}[c + d x]^3}{16 d (a + a \operatorname{Sec}[c + d x])^3} - \frac{3 \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \operatorname{Log}\left[\operatorname{Sin}\left[\frac{c}{2} + \frac{d x}{2}\right]\right] \operatorname{Sec}[c + d x]^3}{16 d (a + a \operatorname{Sec}[c + d x])^3} + \frac{3 \operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Sec}[c + d x]^3}{128 d (a + a \operatorname{Sec}[c + d x])^3} - \frac{\operatorname{Sec}\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \operatorname{Sec}[c + d x]^3}{160 d (a + a \operatorname{Sec}[c + d x])^3} + \frac{\left(x \operatorname{Cos}\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \operatorname{Sec}[c + d x]^3 \left(\frac{3}{32} \operatorname{Cot}\left[\frac{c}{2}\right] - \frac{3}{32} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] + \frac{3}{32} \operatorname{Tan}\left[\frac{c}{2}\right]\right)\right)}{(a + a \operatorname{Sec}[c + d x])^3}$$

Problem 121: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \operatorname{Sin}[c + d x])^{5/2}}{a + a \operatorname{Sec}[c + d x]} dx$$

Optimal (type 4, 104 leaves, 7 steps):

$$-\frac{4 e^2 \text{EllipticE}\left[\frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{e \operatorname{Sin}[c+d x]}}{5 a d \sqrt{\operatorname{Sin}[c+d x]}} + \frac{2 e\left(e \operatorname{Sin}[c+d x]\right)^{3 / 2}}{3 a d} - \frac{2 e \operatorname{Cos}[c+d x]\left(e \operatorname{Sin}[c+d x]\right)^{3 / 2}}{5 a d}$$

Result (type 5, 232 leaves):

$$\left(2 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Sec}[c+d x]\left(e \operatorname{Sin}[c+d x]\right)^{5 / 2}\right. \\ \left.\left(\left(2 e^{-i d x} \sqrt{2-2 e^{2 i(c+d x)}}\left(3 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, e^{2 i(c+d x)}\right]+e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, e^{2 i(c+d x)}\right]\right) \operatorname{Sec}[c]\right) / \right. \\ \left.\left(\sqrt{-i e^{-i(c+d x)}(-1+e^{2 i(c+d x)})}+\sqrt{\operatorname{Sin}[c+d x]}\left(10 \operatorname{Cos}[d x] \operatorname{Sin}[c]-3 \operatorname{Cos}[2 d x] \operatorname{Sin}[2 c]+10 \operatorname{Cos}[c] \operatorname{Sin}[d x]-3 \operatorname{Cos}[2 c] \operatorname{Sin}[2 d x]-12 \operatorname{Tan}[c]\right)\right)\right) / \\ \left.(15 a d\left(1+\operatorname{Sec}[c+d x]\right) \operatorname{Sin}[c+d x]^{5 / 2}\right)$$

Problem 123: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{e \operatorname{Sin}[c+d x]}}{a+a \operatorname{Sec}[c+d x]} d x$$

Optimal (type 4, 95 leaves, 7 steps):

$$-\frac{2 e}{a d \sqrt{e \operatorname{Sin}[c+d x]}} + \frac{2 e \operatorname{Cos}[c+d x]}{a d \sqrt{e \operatorname{Sin}[c+d x]}} + \frac{4 \text{EllipticE}\left[\frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{e \operatorname{Sin}[c+d x]}}{a d \sqrt{\operatorname{Sin}[c+d x]}}$$

Result (type 5, 249 leaves):

$$\left(2\left(3-9 e^{2 i c}+6 e^{i(c+d x)}-9 e^{2 i(c+d x)}+3 e^{2 i(2 c+d x)}+6 e^{i(3 c+d x)}+12 e^{2 i c} \sqrt{1-e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, e^{2 i(c+d x)}\right]+4 e^{2 i(c+d x)} \sqrt{1-e^{2 i(c+d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, e^{2 i(c+d x)}\right]\right) \sqrt{e \operatorname{Sin}[c+d x]}\right) / \\ \left(3 a d\left(1+i e^{i c}\right)\left(i+e^{i c}\right)\left(-1+e^{i(c+d x)}\right)\left(1+e^{i(c+d x)}\right)\right)$$

Problem 125: Result unnecessarily involves higher level functions.

$$\int \frac{1}{\left(a+a \operatorname{Sec}[c+d x]\right)\left(e \operatorname{Sin}[c+d x]\right)^{3 / 2}} d x$$

Optimal (type 4, 135 leaves, 8 steps):

$$\begin{aligned}
 & -\frac{2e}{5ad(e\sin[c+dx])^{5/2}} + \frac{2e\cos[c+dx]}{5ad(e\sin[c+dx])^{5/2}} - \\
 & \frac{4\cos[c+dx]}{5ade\sqrt{e\sin[c+dx]}} - \frac{4\text{EllipticE}\left[\frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), 2\right]\sqrt{e\sin[c+dx]}}{5ade^2\sqrt{\sin[c+dx]}}
 \end{aligned}$$

Result (type 5, 175 leaves):

$$\begin{aligned}
 & -\left(\left(e^{-i(3c+2dx)}(1+e^{2ic})\left(\sqrt{1-e^{2i(c+dx)}}(1+2e^{i(c+dx)}+2e^{2i(c+dx)})\right)+\right.\right. \\
 & \quad \left.\left.(-1+e^{i(c+dx)})(1+e^{i(c+dx)})^3\text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, e^{2i(c+dx)}\right]\right)\right) \\
 & \quad \text{Sec}[c]\text{Tan}\left[\frac{1}{2}(c+dx)\right]\left/\left(5ad\sqrt{1-e^{2i(c+dx)}}(e\sin[c+dx])^{3/2}\right)\right)
 \end{aligned}$$

Problem 128: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e\sin[c+dx])^{5/2}}{(a+a\sec[c+dx])^2} dx$$

Optimal (type 4, 187 leaves, 14 steps):

$$\begin{aligned}
 & \frac{4e^3}{a^2d\sqrt{e\sin[c+dx]}} - \frac{2e^3\cos[c+dx]}{a^2d\sqrt{e\sin[c+dx]}} - \\
 & \frac{2e^3\cos[c+dx]^3}{a^2d\sqrt{e\sin[c+dx]}} - \frac{44e^2\text{EllipticE}\left[\frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), 2\right]\sqrt{e\sin[c+dx]}}{5a^2d\sqrt{\sin[c+dx]}} + \\
 & \frac{4e(e\sin[c+dx])^{3/2}}{3a^2d} - \frac{12e\cos[c+dx](e\sin[c+dx])^{3/2}}{5a^2d}
 \end{aligned}$$

Result (type 5, 451 leaves):

$$\left(\cos \left[\frac{c}{2} + \frac{dx}{2} \right]^4 \operatorname{Csc}[c+dx]^2 \operatorname{Sec}[c+dx]^2 \right. \\ \left. \left(\frac{16 \cos[dx] \sin[c]}{3d} - \frac{16 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c] \left(8 \sin\left[\frac{c}{2}\right] + 3 \sin\left[\frac{3c}{2}\right]\right)}{5d} - \frac{4 \cos[2dx] \sin[2c]}{5d} + \right. \right. \\ \left. \left. \frac{16 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \sin\left[\frac{dx}{2}\right]}{d} + \frac{16 \cos[c] \sin[dx]}{3d} - \frac{4 \cos[2c] \sin[2dx]}{5d} \right) \right. \\ \left. (e \sin[c+dx])^{5/2} \right) / (a + a \operatorname{Sec}[c+dx])^2 + \\ \left(44 i \cos \left[\frac{c}{2} + \frac{dx}{2} \right]^4 \left(- \left(\left(2 i e^{-i dx} \sqrt{2 - 2 e^{2i(c+dx)}} \operatorname{Hypergeometric2F1} \left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, e^{2i(c+dx)} \right] \right) \right) / \right. \right. \\ \left. \left(d \sqrt{-i e^{-i(c+dx)} (-1 + e^{2i(c+dx)})} \right) \right) - \\ \left(2 i e^{i dx} \sqrt{2 - 2 e^{2i(c+dx)}} \operatorname{Hypergeometric2F1} \left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, e^{2i(c+dx)} \right] \right) / \\ \left(3 d \sqrt{-i e^{-i(c+dx)} (-1 + e^{2i(c+dx)})} \right) \operatorname{Sec}[c+dx]^2 (e \sin[c+dx])^{5/2} \right) / \\ \left(5 (a + a \operatorname{Sec}[c+dx])^2 \left(\cos \left[\frac{c}{2} \right] - \sin \left[\frac{c}{2} \right] \right) \left(\cos \left[\frac{c}{2} \right] + \sin \left[\frac{c}{2} \right] \right) \sin[c+dx]^{5/2} \right)$$

Problem 130: Result unnecessarily involves higher level functions.

$$\int \frac{\sqrt{e \sin[c+dx]}}{(a + a \operatorname{Sec}[c+dx])^2} dx$$

Optimal (type 4, 188 leaves, 15 steps):

$$\frac{4 e^3}{5 a^2 d (e \sin[c+dx])^{5/2}} - \frac{2 e^3 \cos[c+dx]}{5 a^2 d (e \sin[c+dx])^{5/2}} - \frac{2 e^3 \cos[c+dx]^3}{5 a^2 d (e \sin[c+dx])^{5/2}} - \\ \frac{4 e}{a^2 d \sqrt{e \sin[c+dx]}} + \frac{16 e \cos[c+dx]}{5 a^2 d \sqrt{e \sin[c+dx]}} + \frac{28 \operatorname{EllipticE} \left[\frac{1}{2} \left(c - \frac{\pi}{2} + dx \right), 2 \right] \sqrt{e \sin[c+dx]}}{5 a^2 d \sqrt{\sin[c+dx]}}$$

Result (type 5, 222 leaves):

$$\left(4 \cos \left[\frac{1}{2} (c+dx) \right]^4 \operatorname{Sec}[c+dx]^2 \sqrt{e \sin[c+dx]} \right. \\ \left(\left(56 i e^{2i c} \left(3 \operatorname{Hypergeometric2F1} \left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, e^{2i(c+dx)} \right] + \right. \right. \right. \\ \left. \left. \left. e^{2i dx} \operatorname{Hypergeometric2F1} \left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, e^{2i(c+dx)} \right] \right) \right) / \left((1 + e^{2i c}) \sqrt{1 - e^{2i(c+dx)}} \right) + \right. \\ \left. \frac{3}{4} \operatorname{Sec}[c] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^3 \left(49 \sin \left[\frac{1}{2} (c-dx) \right] + 35 \sin \left[\frac{1}{2} (3c+dx) \right] - \right. \right. \\ \left. \left. 23 \sin \left[\frac{1}{2} (c+3dx) \right] + 5 \sin \left[\frac{1}{2} (5c+3dx) \right] \right) \right) \right) / (15 a^2 d (1 + \operatorname{Sec}[c+dx])^2)$$

Problem 132: Result unnecessarily involves higher level functions.

$$\int \frac{1}{(a + a \operatorname{Sec}[c + d x])^2 (e \operatorname{Sin}[c + d x])^{3/2}} dx$$

Optimal (type 4, 224 leaves, 17 steps):

$$\begin{aligned} & \frac{4 e^3}{9 a^2 d (e \operatorname{Sin}[c + d x])^{9/2}} - \frac{2 e^3 \operatorname{Cos}[c + d x]}{9 a^2 d (e \operatorname{Sin}[c + d x])^{9/2}} - \\ & \frac{2 e^3 \operatorname{Cos}[c + d x]^3}{9 a^2 d (e \operatorname{Sin}[c + d x])^{9/2}} - \frac{4 e}{5 a^2 d (e \operatorname{Sin}[c + d x])^{5/2}} + \frac{16 e \operatorname{Cos}[c + d x]}{45 a^2 d (e \operatorname{Sin}[c + d x])^{5/2}} - \\ & \frac{4 \operatorname{Cos}[c + d x]}{15 a^2 d e \sqrt{e \operatorname{Sin}[c + d x]}} - \frac{4 \operatorname{EllipticE}\left[\frac{1}{2}(c - \frac{\pi}{2} + d x), 2\right] \sqrt{e \operatorname{Sin}[c + d x]}}{15 a^2 d e^2 \sqrt{\operatorname{Sin}[c + d x]}} \end{aligned}$$

Result (type 5, 222 leaves):

$$\begin{aligned} & \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^4 \right. \\ & \left. \left(\left(96 i (1 - e^{2 i (c+d x)})^{3/2} \left(-\sqrt{1 - e^{2 i (c+d x)}} + (1 + e^{2 i c}) \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, e^{2 i (c+d x)}\right] \right) \right) \right) / \left((1 + e^{2 i c}) (1 + e^{2 i (c+d x)})^2 \right) - \right. \\ & \left. 2 (28 \operatorname{Cos}[c] + 31 \operatorname{Cos}[d x] + 16 \operatorname{Cos}[2 c + d x] + 12 \operatorname{Cos}[c + 2 d x] + 3 \operatorname{Cos}[2 c + 3 d x]) \right. \\ & \left. \operatorname{Sec}[c] \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \operatorname{Sec}[c + d x]^2 \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] \right) / \\ & (45 a^2 d (1 + \operatorname{Sec}[c + d x])^2 (e \operatorname{Sin}[c + d x])^{3/2}) \end{aligned}$$

Problem 134: Unable to integrate problem.

$$\int (a + a \operatorname{Sec}[c + d x])^3 (e \operatorname{Sin}[c + d x])^m dx$$

Optimal (type 5, 247 leaves, 9 steps):

$$\begin{aligned} & \left(a^3 \operatorname{Cos}[c + d x] \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, \operatorname{Sin}[c + d x]^2\right] (e \operatorname{Sin}[c + d x])^{1+m} \right) / \\ & \left(d e (1+m) \sqrt{\operatorname{Cos}[c + d x]^2} \right) + \frac{1}{d e (1+m)} \\ & 3 a^3 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{2}, \frac{3+m}{2}, \operatorname{Sin}[c + d x]^2\right] (e \operatorname{Sin}[c + d x])^{1+m} + \\ & \frac{a^3 \operatorname{Hypergeometric2F1}\left[2, \frac{1+m}{2}, \frac{3+m}{2}, \operatorname{Sin}[c + d x]^2\right] (e \operatorname{Sin}[c + d x])^{1+m}}{d e (1+m)} + \\ & \frac{1}{d e (1+m)} 3 a^3 \sqrt{\operatorname{Cos}[c + d x]^2} \\ & \operatorname{Hypergeometric2F1}\left[\frac{3}{2}, \frac{1+m}{2}, \frac{3+m}{2}, \operatorname{Sin}[c + d x]^2\right] \operatorname{Sec}[c + d x] (e \operatorname{Sin}[c + d x])^{1+m} \end{aligned}$$

Result (type 8, 25 leaves):

$$\int (a + a \operatorname{Sec}[c + d x])^3 (e \operatorname{Sin}[c + d x])^m dx$$

Problem 135: Unable to integrate problem.

$$\int (a + a \operatorname{Sec}[c + d x])^2 (e \operatorname{Sin}[c + d x])^m dx$$

Optimal (type 5, 195 leaves, 7 steps):

$$\begin{aligned} & \left(a^2 \operatorname{Cos}[c + d x] \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, \operatorname{Sin}[c + d x]^2\right] (e \operatorname{Sin}[c + d x])^{1+m} \right) / \\ & \left(d e (1+m) \sqrt{\operatorname{Cos}[c + d x]^2} \right) + \frac{1}{d e (1+m)} \\ & 2 a^2 \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{2}, \frac{3+m}{2}, \operatorname{Sin}[c + d x]^2\right] (e \operatorname{Sin}[c + d x])^{1+m} + \\ & \frac{1}{d e (1+m)} a^2 \sqrt{\operatorname{Cos}[c + d x]^2} \\ & \operatorname{Hypergeometric2F1}\left[\frac{3}{2}, \frac{1+m}{2}, \frac{3+m}{2}, \operatorname{Sin}[c + d x]^2\right] \operatorname{Sec}[c + d x] (e \operatorname{Sin}[c + d x])^{1+m} \end{aligned}$$

Result (type 8, 25 leaves):

$$\int (a + a \operatorname{Sec}[c + d x])^2 (e \operatorname{Sin}[c + d x])^m dx$$

Problem 136: Unable to integrate problem.

$$\int (a + a \operatorname{Sec}[c + d x]) (e \operatorname{Sin}[c + d x])^m dx$$

Optimal (type 5, 119 leaves, 5 steps):

$$\begin{aligned} & \left(a \operatorname{Cos}[c + d x] \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, \operatorname{Sin}[c + d x]^2\right] (e \operatorname{Sin}[c + d x])^{1+m} \right) / \\ & \left(d e (1+m) \sqrt{\operatorname{Cos}[c + d x]^2} \right) + \\ & \frac{a \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{2}, \frac{3+m}{2}, \operatorname{Sin}[c + d x]^2\right] (e \operatorname{Sin}[c + d x])^{1+m}}{d e (1+m)} \end{aligned}$$

Result (type 8, 23 leaves):

$$\int (a + a \operatorname{Sec}[c + d x]) (e \operatorname{Sin}[c + d x])^m dx$$

Problem 137: Unable to integrate problem.

$$\int \frac{(e \operatorname{Sin}[c + d x])^m}{a + a \operatorname{Sec}[c + d x]} dx$$

Optimal (type 5, 100 leaves, 5 steps):

$$-\frac{e (e \sin [c+d x])^{-1+m}}{a d (1-m)} + \left(e \cos [c+d x] \operatorname{Hypergeometric2F1}\left[-\frac{1}{2}, \frac{1}{2}(-1+m), \frac{1+m}{2}, \sin [c+d x]^2\right] (e \sin [c+d x])^{-1+m} \right) / \left(a d (1-m) \sqrt{\cos [c+d x]^2} \right)$$

Result (type 8, 25 leaves):

$$\int \frac{(e \sin [c+d x])^m}{a+a \sec [c+d x]} dx$$

Problem 138: Unable to integrate problem.

$$\int \frac{(e \sin [c+d x])^m}{(a+a \sec [c+d x])^2} dx$$

Optimal (type 5, 207 leaves, 9 steps):

$$\frac{2 e^3 (e \sin [c+d x])^{-3+m}}{a^2 d (3-m)} - \left(e^3 \cos [c+d x] \operatorname{Hypergeometric2F1}\left[-\frac{3}{2}, \frac{1}{2}(-3+m), \frac{1}{2}(-1+m), \sin [c+d x]^2\right] (e \sin [c+d x])^{-3+m} \right) / \left(a^2 d (3-m) \sqrt{\cos [c+d x]^2} \right) - \left(e^3 \cos [c+d x] \operatorname{Hypergeometric2F1}\left[-\frac{1}{2}, \frac{1}{2}(-3+m), \frac{1}{2}(-1+m), \sin [c+d x]^2\right] (e \sin [c+d x])^{-3+m} \right) / \left(a^2 d (3-m) \sqrt{\cos [c+d x]^2} \right) - \frac{2 e (e \sin [c+d x])^{-1+m}}{a^2 d (1-m)}$$

Result (type 8, 25 leaves):

$$\int \frac{(e \sin [c+d x])^m}{(a+a \sec [c+d x])^2} dx$$

Problem 139: Unable to integrate problem.

$$\int \frac{(e \sin [c+d x])^m}{(a+a \sec [c+d x])^3} dx$$

Optimal (type 5, 236 leaves, 12 steps):

$$\begin{aligned}
 & - \frac{4 e^5 (e \operatorname{Sin}[c+d x])^{-5+m}}{a^3 d (5-m)} + \\
 & \left(e^5 \operatorname{Cos}[c+d x] \operatorname{Hypergeometric2F1}\left[-\frac{5}{2}, \frac{1}{2}(-5+m), \frac{1}{2}(-3+m), \operatorname{Sin}[c+d x]^2\right] \right. \\
 & \quad \left. (e \operatorname{Sin}[c+d x])^{-5+m} \right) / \left(a^3 d (5-m) \sqrt{\operatorname{Cos}[c+d x]^2} \right) + \\
 & \left(3 e^5 \operatorname{Cos}[c+d x] \operatorname{Hypergeometric2F1}\left[-\frac{3}{2}, \frac{1}{2}(-5+m), \frac{1}{2}(-3+m), \operatorname{Sin}[c+d x]^2\right] \right. \\
 & \quad \left. (e \operatorname{Sin}[c+d x])^{-5+m} \right) / \left(a^3 d (5-m) \sqrt{\operatorname{Cos}[c+d x]^2} \right) + \\
 & \frac{7 e^3 (e \operatorname{Sin}[c+d x])^{-3+m}}{a^3 d (3-m)} - \frac{3 e (e \operatorname{Sin}[c+d x])^{-1+m}}{a^3 d (1-m)}
 \end{aligned}$$

Result (type 8, 25 leaves):

$$\int \frac{(e \operatorname{Sin}[c+d x])^m}{(a+a \operatorname{Sec}[c+d x])^3} dx$$

Problem 140: Result more than twice size of optimal antiderivative.

$$\int (a+a \operatorname{Sec}[c+d x])^{3/2} (e \operatorname{Sin}[c+d x])^m dx$$

Optimal (type 6, 106 leaves, 5 steps):

$$\begin{aligned}
 & \frac{1}{d} 2 a e \operatorname{AppellF1}\left[-\frac{1}{2}, \frac{1-m}{2}, \frac{1}{2}(-2-m), \frac{1}{2}, \operatorname{Cos}[c+d x], -\operatorname{Cos}[c+d x]\right] \\
 & (1-\operatorname{Cos}[c+d x])^{\frac{1-m}{2}} (1+\operatorname{Cos}[c+d x])^{-m/2} \sqrt{a+a \operatorname{Sec}[c+d x]} (e \operatorname{Sin}[c+d x])^{-1+m}
 \end{aligned}$$

Result (type 6, 7867 leaves):

$$\begin{aligned}
 & - \left(2^{-1+m} (3+m) (a (1+\operatorname{Sec}[c+d x]))^{3/2} (e \operatorname{Sin}[c+d x])^m \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] \left(\frac{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \right)^m \left(\operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \right. \right. \right. \\
 & \quad \left. \left. \frac{3+m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right] / \left(\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \right) \right. \right. \\
 & \quad \left. \left. \left(-(3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right] + \right. \right. \right. \\
 & \quad \left. \left. \left(2(1+m) \operatorname{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right] + \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right] \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{2}(c+dx)\right]^2 \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \Big/ \\
 & \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, \frac{1}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. \left(-2m \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{3}{2}, m, \frac{5+m}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 - \right. \\
 & \left. \left(2 \operatorname{AppellF1}\left[\frac{1+m}{2}, \frac{3}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \Big/ \right. \\
 & \left. \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, \frac{3}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \left. \left. \left(-2m \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{3}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 3 \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{5}{2}, m, \frac{5+m}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) \Big) + \\
 & \frac{1}{1+m} 2^{-2+m} (3+m) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \left(\frac{\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^m \\
 & \left(\operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \Big/ \right. \\
 & \left. \left(\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \left(- (3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \right. \right. \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \left(2(1+m) \operatorname{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, \right. \right. \right. \right. \\
 & \left. \left. 2+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, \right. \right. \right. \\
 & \left. \left. 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) \Big) + \\
 & \frac{1}{\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2} \left(\left(\operatorname{AppellF1}\left[\frac{1+m}{2}, \frac{1}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \Big/ \left(\left(3+m\right) \operatorname{AppellF1}\left[\frac{1+m}{2}, \frac{1}{2}, \right. \right. \right. \\
 & \left. \left. m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \left(-2m \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \text{AppellF1}\left[\frac{3+m}{2}, \right. \\
 & \left. \frac{3}{2}, m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & \left(2 \text{AppellF1}\left[\frac{1+m}{2}, \frac{3}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) / \\
 & \left((3+m) \text{AppellF1}\left[\frac{1+m}{2}, \frac{3}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. \left(-2m \text{AppellF1}\left[\frac{3+m}{2}, \frac{3}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 3 \text{AppellF1}\left[\frac{3+m}{2}, \frac{5}{2}, m, \frac{5+m}{2}, \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) - \\
 & \frac{1}{(1+m) \sqrt{\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}}} 2^{-1+m} m (3+m) \tan\left[\frac{1}{2}(c+dx)\right] \left(\frac{\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{-1+m} \\
 & \left(-\frac{\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2}{\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2} + \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2}{2\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right) \\
 & \left(\text{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] / \right. \\
 & \left. \left(\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \left(-(3+m) \text{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \left(2(1+m) \text{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. 2+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \text{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) + \\
 & \frac{1}{\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2} \left(\left(\text{AppellF1}\left[\frac{1+m}{2}, \frac{1}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right) / \left((3+m) \text{AppellF1}\left[\frac{1+m}{2}, \frac{1}{2}, \right. \right. \right. \\
 & \left. \left. \left. m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \left(-2m \text{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \text{AppellF1}\left[\frac{3+m}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{3}{2}, m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left(2 \operatorname{AppellF1} \left[\frac{1+m}{2}, \frac{3}{2}, m, \frac{3+m}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) / \\
 & \left((3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, \frac{3}{2}, m, \frac{3+m}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \left(-2m \operatorname{AppellF1} \left[\frac{3+m}{2}, \frac{3}{2}, 1+m, \frac{5+m}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + 3 \operatorname{AppellF1} \left[\frac{3+m}{2}, \frac{5}{2}, m, \frac{5+m}{2}, \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 \left. \right) \right) - \\
 & \frac{1}{(1+m) \sqrt{1 - \tan \left[\frac{1}{2} (c+dx) \right]^2}} 2^{-1+m} (3+m) \tan \left[\frac{1}{2} (c+dx) \right] \left(\frac{\tan \left[\frac{1}{2} (c+dx) \right]}{1 + \tan \left[\frac{1}{2} (c+dx) \right]^2} \right)^m \\
 & \left(- \left(\left(\operatorname{AppellF1} \left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \right. \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] \right) / \left(\left(1 + \tan \left[\frac{1}{2} (c+dx) \right]^2 \right)^2 \right) \right. \\
 & \quad \left(- (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \left(2 (1+m) \operatorname{AppellF1} \left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \operatorname{AppellF1} \left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \right. \right. \\
 & \quad \left. \left. \frac{5+m}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 \left. \right) \right) + \\
 & \left(-\frac{1}{3+m} (1+m)^2 \operatorname{AppellF1} \left[1 + \frac{1+m}{2}, -\frac{1}{2}, 2+m, 1 + \frac{3+m}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] - \frac{1}{2(3+m)} \right. \\
 & \quad \left. (1+m) \operatorname{AppellF1} \left[1 + \frac{1+m}{2}, \frac{1}{2}, 1+m, 1 + \frac{3+m}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] \right) / \\
 & \left(\left(1 + \tan \left[\frac{1}{2} (c+dx) \right]^2 \right) \left(- (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \left(2 (1+m) \operatorname{AppellF1} \left[\frac{3+m}{2}, -\frac{1}{2}, \right. \right. \right. \\
 & \quad \left. \left. 2+m, \frac{5+m}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \operatorname{AppellF1} \left[\frac{3+m}{2}, \frac{1}{2}, \right. \right. \\
 & \quad \left. \left. 1+m, \frac{5+m}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 \left. \right) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{(-1 + \tan[\frac{1}{2}(c+dx)]^2)^3} 2 \operatorname{Sec}[\frac{1}{2}(c+dx)]^2 \tan[\frac{1}{2}(c+dx)] \\
 & \left(\left(\operatorname{AppellF1}\left[\frac{1+m}{2}, \frac{1}{2}, m, \frac{3+m}{2}, \tan[\frac{1}{2}(c+dx)]^2, -\tan[\frac{1}{2}(c+dx)]^2\right] \right. \right. \\
 & \quad \left. \left. (-1 + \tan[\frac{1}{2}(c+dx)]^2) \right) \right) / \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, \frac{1}{2}, m, \frac{3+m}{2}, \right. \right. \\
 & \quad \tan[\frac{1}{2}(c+dx)]^2, -\tan[\frac{1}{2}(c+dx)]^2] + \left(-2m \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \right. \right. \\
 & \quad \left. \left. \frac{5+m}{2}, \tan[\frac{1}{2}(c+dx)]^2, -\tan[\frac{1}{2}(c+dx)]^2\right] + \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{3}{2}, m, \right. \right. \\
 & \quad \left. \left. \frac{5+m}{2}, \tan[\frac{1}{2}(c+dx)]^2, -\tan[\frac{1}{2}(c+dx)]^2\right] \right) \tan[\frac{1}{2}(c+dx)]^2 - \\
 & \quad \left. \left(2 \operatorname{AppellF1}\left[\frac{1+m}{2}, \frac{3}{2}, m, \frac{3+m}{2}, \tan[\frac{1}{2}(c+dx)]^2, -\tan[\frac{1}{2}(c+dx)]^2\right] \right) \right) / \\
 & \quad \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, \frac{3}{2}, m, \frac{3+m}{2}, \tan[\frac{1}{2}(c+dx)]^2, -\tan[\frac{1}{2}(c+dx)]^2\right] + \right. \\
 & \quad \left. \left(-2m \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{3}{2}, 1+m, \frac{5+m}{2}, \tan[\frac{1}{2}(c+dx)]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan[\frac{1}{2}(c+dx)]^2\right] + 3 \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{5}{2}, m, \frac{5+m}{2}, \right. \right. \\
 & \quad \left. \left. \tan[\frac{1}{2}(c+dx)]^2, -\tan[\frac{1}{2}(c+dx)]^2\right] \right) \tan[\frac{1}{2}(c+dx)]^2 \right) - \\
 & \quad \left(\operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan[\frac{1}{2}(c+dx)]^2, -\tan[\frac{1}{2}(c+dx)]^2\right] \right. \\
 & \quad \left. \left(\left(2(1+m) \operatorname{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \tan[\frac{1}{2}(c+dx)]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\tan[\frac{1}{2}(c+dx)]^2\right] + \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \tan[\frac{1}{2}(c+dx)]^2, \right. \right. \\
 & \quad \left. \left. -\tan[\frac{1}{2}(c+dx)]^2\right] \right) \operatorname{Sec}[\frac{1}{2}(c+dx)]^2 \tan[\frac{1}{2}(c+dx)] - (3+m) \right. \\
 & \quad \left. \left(-\frac{1}{3+m} (1+m)^2 \operatorname{AppellF1}\left[1 + \frac{1+m}{2}, -\frac{1}{2}, 2+m, 1 + \frac{3+m}{2}, \tan[\frac{1}{2}(c+dx)]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan[\frac{1}{2}(c+dx)]^2\right] \operatorname{Sec}[\frac{1}{2}(c+dx)]^2 \tan[\frac{1}{2}(c+dx)] - \frac{1}{2(3+m)} \right. \\
 & \quad \left. (1+m) \operatorname{AppellF1}\left[1 + \frac{1+m}{2}, \frac{1}{2}, 1+m, 1 + \frac{3+m}{2}, \tan[\frac{1}{2}(c+dx)]^2, \right. \right. \\
 & \quad \left. \left. -\tan[\frac{1}{2}(c+dx)]^2\right] \operatorname{Sec}[\frac{1}{2}(c+dx)]^2 \tan[\frac{1}{2}(c+dx)] \right) \right) + \\
 & \quad \tan[\frac{1}{2}(c+dx)]^2 \left(-\frac{1}{5+m} (1+m) (3+m) \operatorname{AppellF1}\left[1 + \frac{3+m}{2}, \frac{1}{2}, \right. \right. \\
 & \quad \left. \left. 2+m, 1 + \frac{5+m}{2}, \tan[\frac{1}{2}(c+dx)]^2, -\tan[\frac{1}{2}(c+dx)]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}[\frac{1}{2}(c+dx)]^2 \tan[\frac{1}{2}(c+dx)] + \frac{1}{2(5+m)} (3+m) \operatorname{AppellF1}\left[\right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(1 + \frac{3+m}{2}, \frac{3}{2}, 1+m, 1 + \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 2(1+m) \left(-\frac{1}{5+m}(2+m)(3+m) \right. \\
 & \quad \text{AppellF1}\left[1 + \frac{3+m}{2}, -\frac{1}{2}, 3+m, 1 + \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \frac{1}{2(5+m)} \right. \\
 & \quad \left. (3+m) \text{AppellF1}\left[1 + \frac{3+m}{2}, \frac{1}{2}, 2+m, 1 + \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Bigg) \Bigg) / \\
 & \left(\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left(-(3+m) \text{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left(2(1+m) \text{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \text{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg) + \\
 & \frac{1}{\left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2} \left(\left(\text{AppellF1}\left[\frac{1+m}{2}, \frac{1}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \Bigg) / \\
 & \left((3+m) \text{AppellF1}\left[\frac{1+m}{2}, \frac{1}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left(-2m \text{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \text{AppellF1}\left[\frac{3+m}{2}, \frac{3}{2}, m, \frac{5+m}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
 & \left(\left(-\frac{1}{3+m} m(1+m) \text{AppellF1}\left[1 + \frac{1+m}{2}, \frac{1}{2}, 1+m, 1 + \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{2(3+m)} \right. \right. \\
 & \quad \left. \left. (1+m) \text{AppellF1}\left[1 + \frac{1+m}{2}, \frac{3}{2}, m, 1 + \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Bigg) \\
 & \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg) / \left((3+m) \text{AppellF1}\left[\frac{1+m}{2}, \frac{1}{2}, m, \frac{3+m}{2}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2) + \left(-2m \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{3}{2}, m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 - \\
 & \left(2\left(-\frac{1}{3+m}m(1+m) \operatorname{AppellF1}\left[1+\frac{1+m}{2}, \frac{3}{2}, 1+m, 1+\frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{2(3+m)}\right.\right. \\
 & \left.3(1+m) \operatorname{AppellF1}\left[1+\frac{1+m}{2}, \frac{5}{2}, m, 1+\frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\right) / \\
 & \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, \frac{3}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left(-2m \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{3}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 3 \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{5}{2}, m, \frac{5+m}{2}, \right.\right. \\
 & \left.\left.\tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 - \right. \\
 & \left.\left[\operatorname{AppellF1}\left[\frac{1+m}{2}, \frac{1}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right.\right. \\
 & \left.\left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \left(\left(-2m \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \right.\right.\right. \\
 & \left.\left.\tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{3}{2}, m, \frac{5+m}{2}, \right.\right. \\
 & \left.\left.\tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \tan\left[\frac{1}{2}(c+dx)\right] + (3+m) \left(-\frac{1}{3+m}m(1+m) \operatorname{AppellF1}\left[1+\frac{1+m}{2}, \frac{1}{2}, 1+m, \right.\right. \\
 & \left.1+\frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{2(3+m)}(1+m) \operatorname{AppellF1}\left[1+\frac{1+m}{2}, \frac{3}{2}, m, \right. \\
 & \left.1+\frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \tan\left[\frac{1}{2}(c+dx)\right]\right) + \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(-\frac{1}{5+m}m(3+m) \operatorname{AppellF1}\left[\right.\right. \\
 & \left.1+\frac{3+m}{2}, \frac{3}{2}, 1+m, 1+\frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \left.\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{2(5+m)}3(3+m) \operatorname{AppellF1}\left[\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & 1 + \frac{3+m}{2}, \frac{5}{2}, m, 1 + \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - 2m \left(-\frac{1}{5+m}(1+m)(3+m)\right. \\
 & \quad \text{AppellF1}\left[1 + \frac{3+m}{2}, \frac{1}{2}, 2+m, 1 + \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{2(5+m)}\right. \\
 & \quad \left. (3+m) \text{AppellF1}\left[1 + \frac{3+m}{2}, \frac{3}{2}, 1+m, 1 + \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\right) \Bigg) \Bigg) / \\
 & \left((3+m) \text{AppellF1}\left[\frac{1+m}{2}, \frac{1}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. \left(-2m \text{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \text{AppellF1}\left[\frac{3+m}{2}, \frac{3}{2}, m, \frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 + \\
 & \left(2 \text{AppellF1}\left[\frac{1+m}{2}, \frac{3}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \left(\left(-2m \text{AppellF1}\left[\frac{3+m}{2}, \frac{3}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\
 & \quad \left. \left. (c+dx)\right]^2\right] + 3 \text{AppellF1}\left[\frac{3+m}{2}, \frac{5}{2}, m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + (3+m) \right. \\
 & \quad \left. \left(-\frac{1}{3+m}m(1+m) \text{AppellF1}\left[1 + \frac{1+m}{2}, \frac{3}{2}, 1+m, 1 + \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{2(3+m)}\right. \right. \\
 & \quad \left. \left. 3(1+m) \text{AppellF1}\left[1 + \frac{1+m}{2}, \frac{5}{2}, m, 1 + \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) \right) + \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(-2m \left(-\frac{1}{5+m}(1+m)(3+m) \text{AppellF1}\left[1 + \frac{3+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, 2+m, 1 + \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{2(5+m)}3(3+m) \right. \right. \\
 & \quad \left. \left. \text{AppellF1}\left[1 + \frac{3+m}{2}, \frac{5}{2}, 1+m, 1 + \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 3\left(-\frac{1}{5+m}\right. \\
 & m(3+m) \operatorname{AppellF1}\left[1+\frac{3+m}{2}, \frac{5}{2}, 1+m, 1+\frac{5+m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \\
 & \left.-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{2(5+m)}\right. \\
 & 5(3+m) \operatorname{AppellF1}\left[1+\frac{3+m}{2}, \frac{7}{2}, m, 1+\frac{5+m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\right) \Bigg) \Bigg) / \\
 & \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, \frac{3}{2}, m, \frac{3+m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) + \right. \\
 & \left(-2m \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{3}{2}, 1+m, \frac{5+m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \right. \\
 & \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) + 3 \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{5}{2}, m, \frac{5+m}{2}, \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \Bigg) \Bigg) \Bigg)
 \end{aligned}$$

Problem 141: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \sqrt{a + a \operatorname{Sec}[c + dx]} (e \operatorname{Sin}[c + dx])^m dx$$

Optimal (type 6, 107 leaves, 5 steps):

$$\begin{aligned}
 & -\frac{1}{d} e \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1-m}{2}, -\frac{m}{2}, \frac{3}{2}, \operatorname{Cos}[c+dx], -\operatorname{Cos}[c+dx]\right] (1 - \operatorname{Cos}[c+dx])^{\frac{1-m}{2}} \\
 & \operatorname{Cos}[c+dx] (1 + \operatorname{Cos}[c+dx])^{-m/2} \sqrt{a + a \operatorname{Sec}[c+dx]} (e \operatorname{Sin}[c+dx])^{-1+m}
 \end{aligned}$$

Result (type 6, 5279 leaves):

$$\begin{aligned}
 & \left((3+m) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1 + \operatorname{Sec}[c+dx])} \right. \\
 & (e \operatorname{Sin}[c+dx])^m \left(-\frac{i \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \operatorname{Sin}[c+dx]^m}{2 \sqrt{\operatorname{Sec}[c+dx]}} + \right. \\
 & \left. \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \left(-\frac{1}{2} i \operatorname{Sin}[c+dx]^m + \frac{1}{2} \operatorname{Sin}[c+dx]^{1+m} \right) + \right. \\
 & \left. \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \left(\frac{\operatorname{Sin}[c+dx]^m}{2 \sqrt{\operatorname{Sec}[c+dx]}} + \sqrt{\operatorname{Sec}[c+dx]} \left(\frac{1}{2} \operatorname{Sin}[c+dx]^m + \frac{1}{2} i \operatorname{Sin}[c+dx]^{1+m} \right) \right) \right) \Bigg) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left(\left(\operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{2}(c+dx)\right]^2 \cos\left[\frac{1}{2}(c+dx)\right]^2 \Big/ \\
 & \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & \left(2(1+m) \operatorname{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - \operatorname{AppellF1}\left[\frac{1+m}{2}, \frac{1}{2}, m, \frac{3+m}{2}, \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \Big/ \left(\left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, \frac{1}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. \left(-2m \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{3}{2}, m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Big/ \\
 & \left(d(1+m) \sqrt{\sec[c+dx]} \sqrt{\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]} \right. \\
 & \left. \frac{1}{2(1+m) \sqrt{\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]}} \right) \\
 & (3+m) \sec\left[\frac{1}{2}(c+dx)\right]^2 \sin[c+dx]^m \left(\left(\operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \right. \right. \right. \\
 & \left. \left. \left. \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \cos\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big/ \right. \\
 & \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & \left(2(1+m) \operatorname{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \operatorname{AppellF1}\left[\frac{1+m}{2}, \frac{1}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \Big/ \left(\left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, \frac{1}{2}, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 + \left(-2m \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, \right. \right. \\
 & \quad \left. \left. 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{3}{2}, m, \right. \right. \\
 & \quad \left. \left. \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) + \\
 & \frac{1}{(1+m) \sqrt{\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]}} m(3+m) \cos[c+dx] \sin[c+dx]^{-1+m} \\
 & \tan\left[\frac{1}{2}(c+dx)\right] \\
 & \left(\left(\operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \cos\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \left(2(1+m) \operatorname{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \right. \right. \\
 & \quad \left. \left. \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 - \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{1+m}{2}, \frac{1}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] / \right. \\
 & \quad \left(\left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, \frac{1}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \left(-2m \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{3}{2}, m, \frac{5+m}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big) + \\
 & \frac{1}{(1+m) \sqrt{\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]}} (3+m) \sin[c+dx]^m \tan\left[\frac{1}{2}(c+dx)\right] \\
 & \left(- \left(\left(\operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\
 & \quad \left. \left. \cos\left[\frac{1}{2}(c+dx)\right] \sin\left[\frac{1}{2}(c+dx)\right] \right) / \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \left(2(1+m) \operatorname{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \right. \right. \right. \\
 & \quad \left. \left. \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \right. \right. \\
 & \quad \left. \left. \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left(\cos \left[\frac{1}{2} (c + d x) \right] \right)^2 \left(-\frac{1}{3+m} (1+m)^2 \operatorname{AppellF1} \left[1 + \frac{1+m}{2}, -\frac{1}{2}, 2+m, 1 + \frac{3+m}{2}, \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] \sec \left[\frac{1}{2} (c + d x) \right]^2 \tan \left[\frac{1}{2} (c + d x) \right] - \right. \\
 & \quad \left. \frac{1}{2(3+m)} (1+m) \operatorname{AppellF1} \left[1 + \frac{1+m}{2}, \frac{1}{2}, 1+m, 1 + \frac{3+m}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] \sec \left[\frac{1}{2} (c + d x) \right]^2 \tan \left[\frac{1}{2} (c + d x) \right] \right) / \\
 & \left((3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] - \right. \\
 & \left(2(1+m) \operatorname{AppellF1} \left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] \right) \\
 & \tan \left[\frac{1}{2} (c + d x) \right]^2 \right) + \left(\operatorname{AppellF1} \left[\frac{1+m}{2}, \frac{1}{2}, m, \frac{3+m}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] \sec \left[\frac{1}{2} (c + d x) \right]^2 \tan \left[\frac{1}{2} (c + d x) \right] \right) / \\
 & \left(\left(-1 + \tan \left[\frac{1}{2} (c + d x) \right]^2 \right)^2 \left((3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, \frac{1}{2}, m, \frac{3+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] + \left(-2m \operatorname{AppellF1} \left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \right. \right. \right. \\
 & \quad \left. \left. \frac{5+m}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] + \operatorname{AppellF1} \left[\frac{3+m}{2}, \frac{3}{2}, m, \right. \right. \\
 & \quad \left. \left. \frac{5+m}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c + d x) \right]^2 \right) - \\
 & \left(-\frac{1}{3+m} m (1+m) \operatorname{AppellF1} \left[1 + \frac{1+m}{2}, \frac{1}{2}, 1+m, 1 + \frac{3+m}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] \sec \left[\frac{1}{2} (c + d x) \right]^2 \tan \left[\frac{1}{2} (c + d x) \right] + \right. \\
 & \quad \left. \frac{1}{2(3+m)} (1+m) \operatorname{AppellF1} \left[1 + \frac{1+m}{2}, \frac{3}{2}, m, 1 + \frac{3+m}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] \sec \left[\frac{1}{2} (c + d x) \right]^2 \tan \left[\frac{1}{2} (c + d x) \right] \right) / \\
 & \left(\left(-1 + \tan \left[\frac{1}{2} (c + d x) \right]^2 \right) \left((3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, \frac{1}{2}, m, \frac{3+m}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] + \left(-2m \operatorname{AppellF1} \left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] + \operatorname{AppellF1} \left[\frac{3+m}{2}, \frac{3}{2}, m, \right. \right. \\
 & \quad \left. \left. \frac{5+m}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c + d x) \right]^2 \right) - \\
 & \left(\operatorname{AppellF1} \left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \cos\left[\frac{1}{2}(c+dx)\right]^2 \left(-\left(2(1+m) \operatorname{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) + \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \\
 & \quad (3+m) \left(-\frac{1}{3+m}(1+m)^2 \operatorname{AppellF1}\left[1+\frac{1+m}{2}, -\frac{1}{2}, 2+m, 1+\frac{3+m}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \right. \\
 & \quad \left. \frac{1}{2(3+m)}(1+m) \operatorname{AppellF1}\left[1+\frac{1+m}{2}, \frac{1}{2}, 1+m, 1+\frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) - \\
 & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(-\frac{1}{5+m}(1+m)(3+m) \operatorname{AppellF1}\left[1+\frac{3+m}{2}, \frac{1}{2}, 2+m, 1+\frac{5+m}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{1}{2(5+m)}(3+m) \operatorname{AppellF1}\left[1+\frac{3+m}{2}, \frac{3}{2}, 1+m, 1+\frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 2(1+m) \left(-\frac{1}{5+m} \right. \right. \\
 & \quad \left. \left. (2+m)(3+m) \operatorname{AppellF1}\left[1+\frac{3+m}{2}, -\frac{1}{2}, 3+m, 1+\frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \frac{1}{2(5+m)} \right. \right. \\
 & \quad \left. \left. (3+m) \operatorname{AppellF1}\left[1+\frac{3+m}{2}, \frac{1}{2}, 2+m, 1+\frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Bigg/ \\
 & \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & \quad \left(2(1+m) \operatorname{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) + \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 + \\
 & \quad \left(\operatorname{AppellF1}\left[\frac{1+m}{2}, \frac{1}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left(\left(-2m \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) + \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{3}{2}, m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right.
 \end{aligned}$$

$$\begin{aligned}
 & (c + dx)^2 \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] + (3 + m) \left(-\frac{1}{3 + m} m (1 + m) \operatorname{AppellF1}\left[1 + \frac{1 + m}{2}, \frac{1}{2}, \right. \right. \\
 & \quad \left. \left. 1 + m, 1 + \frac{3 + m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] + \frac{1}{2(3 + m)} (1 + m) \operatorname{AppellF1}\left[1 + \frac{1 + m}{2}, \frac{3}{2}, m, 1 + \frac{3 + m}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] \right) + \\
 & \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 \left(-\frac{1}{5 + m} m (3 + m) \operatorname{AppellF1}\left[1 + \frac{3 + m}{2}, \frac{3}{2}, 1 + m, 1 + \frac{5 + m}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] + \right. \\
 & \quad \left. \frac{1}{2(5 + m)} 3(3 + m) \operatorname{AppellF1}\left[1 + \frac{3 + m}{2}, \frac{5}{2}, m, 1 + \frac{5 + m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] - 2m \left(-\frac{1}{5 + m} \right. \right. \\
 & \quad \left. \left. (1 + m)(3 + m) \operatorname{AppellF1}\left[1 + \frac{3 + m}{2}, \frac{1}{2}, 2 + m, 1 + \frac{5 + m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] + \frac{1}{2(5 + m)} \right. \right. \\
 & \quad \left. \left. (3 + m) \operatorname{AppellF1}\left[1 + \frac{3 + m}{2}, \frac{3}{2}, 1 + m, 1 + \frac{5 + m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] \right) \right) \Big/ \\
 & \left(\left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 \right) \left((3 + m) \operatorname{AppellF1}\left[\frac{1 + m}{2}, \frac{1}{2}, m, \frac{3 + m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] + \left(-2m \operatorname{AppellF1}\left[\frac{3 + m}{2}, \frac{1}{2}, 1 + m, \frac{5 + m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3 + m}{2}, \frac{3}{2}, m, \frac{5 + m}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2 \right) \Big) - \\
 & \frac{1}{2(1 + m) \left(\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]^2 \operatorname{Sec}[c + dx] \right)^{3/2}} (3 + m) \operatorname{Sin}[c + dx]^m \\
 & \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] \\
 & \left(\left(\operatorname{AppellF1}\left[\frac{1 + m}{2}, -\frac{1}{2}, 1 + m, \frac{3 + m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]^2 \right) \Big/ \right. \\
 & \left. \left((3 + m) \operatorname{AppellF1}\left[\frac{1 + m}{2}, -\frac{1}{2}, 1 + m, \frac{3 + m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right] - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(2 (1+m) \operatorname{AppellF1} \left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \operatorname{AppellF1} \left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 - \\
 & \operatorname{AppellF1} \left[\frac{1+m}{2}, \frac{1}{2}, m, \frac{3+m}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] / \\
 & \left(\left(-1 + \tan \left[\frac{1}{2} (c+dx) \right]^2 \right) \left((3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, \frac{1}{2}, m, \frac{3+m}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \left(-2m \operatorname{AppellF1} \left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \operatorname{AppellF1} \left[\frac{3+m}{2}, \frac{3}{2}, m, \right. \right. \\
 & \quad \left. \left. \frac{5+m}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 \right) \\
 & \left(-\cos \left[\frac{1}{2} (c+dx) \right] \sec [c+dx] \sin \left[\frac{1}{2} (c+dx) \right] + \cos \left[\frac{1}{2} (c+dx) \right]^2 \right. \\
 & \quad \left. \left. \sec [c+dx] \tan [c+dx] \right) \right)
 \end{aligned}$$

Problem 142: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \sin [c+dx])^m}{\sqrt{a+a \sec [c+dx]}} dx$$

Optimal (type 6, 115 leaves, 5 steps):

$$\begin{aligned}
 & - \left(\left(2 e \operatorname{AppellF1} \left[\frac{3}{2}, \frac{1-m}{2}, \frac{2-m}{2}, \frac{5}{2}, \cos [c+dx], -\cos [c+dx] \right] (1-\cos [c+dx])^{\frac{1-m}{2}} \right. \right. \\
 & \quad \left. \left. \cos [c+dx] (1+\cos [c+dx])^{1-\frac{m}{2}} (e \sin [c+dx])^{-1+m} \right) / \left(3 d \sqrt{a+a \sec [c+dx]} \right) \right)
 \end{aligned}$$

Result (type 6, 2679 leaves):

$$\begin{aligned}
 & \left(\sqrt{2} (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. \cos [c+dx] \sqrt{1+\sec [c+dx]} \sin [c+dx]^m (e \sin [c+dx])^m \tan \left[\frac{1}{2} (c+dx) \right] \right) / \\
 & \left(d (1+m) \sqrt{a (1+\sec [c+dx])} \right. \\
 & \quad \left((3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] - \right. \\
 & \quad \left. \left(2 (1+m) \operatorname{AppellF1} \left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) + \right.
 \end{aligned}$$

$$\begin{aligned}
& \text{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(\left((3+m) \text{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{1+\sec[c+dx]} \sin[c+dx]^m \right) / \right. \\
& \left(\sqrt{2} (1+m) \left((3+m) \text{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \left(2(1+m) \text{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \right. \right. \right. \right. \\
& \quad \quad \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \text{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \right. \right. \right. \\
& \quad \quad \left. \left. \left. \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
& \left(\sqrt{2} m (3+m) \text{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \cos[c+dx]^2 \sqrt{1+\sec[c+dx]} \sin[c+dx]^{-1+m} \tan\left[\frac{1}{2}(c+dx)\right] \right) / \\
& \left((1+m) \left((3+m) \text{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
& \quad \left(2(1+m) \text{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. \text{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
& \left((3+m) \text{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \sec[c+dx] \sin[c+dx]^{1+m} \tan\left[\frac{1}{2}(c+dx)\right] \right) / \left(\sqrt{2} (1+m) \sqrt{1+\sec[c+dx]} \right) \\
& \left((3+m) \text{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
& \quad \left(2(1+m) \text{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. \text{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
& \left(\sqrt{2} (3+m) \text{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \sqrt{1+\sec[c+dx]} \sin[c+dx]^{1+m} \tan\left[\frac{1}{2}(c+dx)\right] \right) / \\
& \left((1+m) \left((3+m) \text{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
& \quad \left(2(1+m) \text{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.
\end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2\right) + \left(\sqrt{2}(3+m) \cos[c+dx] \sqrt{1+\sec[c+dx]} \sin[c+dx]^m \right. \\
 & \tan\left[\frac{1}{2}(c+dx)\right] \left(-\frac{1}{3+m}(1+m)^2 \text{AppellF1}\left[1+\frac{1+m}{2}, -\frac{1}{2}, 2+m, 1+\frac{3+m}{2}, \right. \right. \\
 & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \\
 & \quad \frac{1}{2(3+m)}(1+m) \text{AppellF1}\left[1+\frac{1+m}{2}, \frac{1}{2}, 1+m, 1+\frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\right) / \\
 & \left((1+m) \left((3+m) \text{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
 & \quad \left(2(1+m) \text{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. \text{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) - \\
 & \left(\sqrt{2}(3+m) \text{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \cos[c+dx] \sqrt{1+\sec[c+dx]} \sin[c+dx]^m \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \quad \left. - \left(2(1+m) \text{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. \text{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + (3+m) \left(-\frac{1}{3+m}(1+m)^2 \text{AppellF1}\left[1+\frac{1+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\frac{1}{2}, 2+m, 1+\frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] - \frac{1}{2(3+m)}(1+m) \text{AppellF1}\left[1+\frac{1+m}{2}, \frac{1}{2}, 1+m, 1+\frac{3+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) - \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(-\frac{1}{5+m}(1+m)(3+m) \text{AppellF1}\left[1+\frac{3+m}{2}, \frac{1}{2}, 2+m, 1+\frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \left. \frac{1}{2(5+m)}(3+m) \text{AppellF1}\left[1+\frac{3+m}{2}, \frac{3}{2}, 1+m, 1+\frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 (1+m) \left(-\frac{1}{5+m} (2+m) (3+m) \operatorname{AppellF1} \left[1 + \frac{3+m}{2}, -\frac{1}{2}, 3+m, 1 + \frac{5+m}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] - \right. \\
 & \quad \left. \frac{1}{2 (5+m)} (3+m) \operatorname{AppellF1} \left[1 + \frac{3+m}{2}, \frac{1}{2}, 2+m, 1 + \frac{5+m}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) \Bigg) \Bigg) / \\
 & \left((1+m) \left((3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] - \right. \right. \\
 & \quad \left. \left(2 (1+m) \operatorname{AppellF1} \left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] + \operatorname{AppellF1} \left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \Bigg) \Bigg)
 \end{aligned}$$

Problem 143: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \operatorname{Sin}[c+dx])^m}{(a+a \operatorname{Sec}[c+dx])^{3/2}} dx$$

Optimal (type 6, 120 leaves, 5 steps):

$$\begin{aligned}
 & - \left(\left(2 e \operatorname{AppellF1} \left[\frac{5}{2}, \frac{1-m}{2}, \frac{4-m}{2}, \frac{7}{2}, \operatorname{Cos}[c+dx], -\operatorname{Cos}[c+dx] \right] (1-\operatorname{Cos}[c+dx])^{\frac{1-m}{2}} \right. \right. \\
 & \quad \left. \left. \operatorname{Cos}[c+dx]^2 (1+\operatorname{Cos}[c+dx])^{1-\frac{m}{2}} (e \operatorname{Sin}[c+dx])^{-1+m} \right) / (5 a d \sqrt{a+a \operatorname{Sec}[c+dx]}) \right)
 \end{aligned}$$

Result (type 6, 5702 leaves):

$$\begin{aligned}
 & \left(2^{1+m} (3+m) \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Sec}[c+dx]^{3/2} \operatorname{Sin} \left[\frac{1}{2} (c+dx) \right] \right. \\
 & \quad \operatorname{Sin}[c+dx]^{-m} (e \operatorname{Sin}[c+dx])^m \left(\frac{1}{2} \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^3 \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]^m + \right. \\
 & \quad \left. \frac{1}{2} \operatorname{Cos} [2 (c+dx)] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^3 \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]^m \right) \\
 & \quad \left(\frac{1}{1-\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2} \right)^{3/2} \left(-1+\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right)^2 \left(\frac{\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]}{1+\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2} \right)^m \\
 & \quad \left(- \left(\operatorname{AppellF1} \left[\frac{1+m}{2}, -\frac{1}{2}, m, \frac{3+m}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) / \right. \right. \\
 & \quad \left. \left((3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, -\frac{1}{2}, m, \frac{3+m}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] - \right. \right. \\
 & \quad \left. \left(2 m \operatorname{AppellF1} \left[\frac{3+m}{2}, -\frac{1}{2}, 1+m, \frac{5+m}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) + \\
 & \left(2 \text{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \Bigg) / \right. \\
 & \left. \left(\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right. \right. \\
 & \quad \left((3+m) \text{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & \quad \left. \left(2(1+m) \text{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. \text{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) / \left(d(1+m) (a(1+\sec[c+dx]))^{3/2} \right. \\
 & \left. \left(\frac{1}{1+m} 2^{2+m} (3+m) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{3/2} \right. \right. \\
 & \quad \left. \left. \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \left(\frac{\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^m \right. \right. \\
 & \quad \left. \left(-\left(\text{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] / \right. \right. \right. \\
 & \quad \left. \left((3+m) \text{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
 & \quad \left. \left(2m \text{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. \text{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) + \\
 & \left(2 \text{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \Bigg) / \right. \\
 & \left(\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \left((3+m) \text{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \left(2(1+m) \text{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \text{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \right. \right. \\
 & \quad \left. \left. \left. \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg) \Bigg) +
 \end{aligned}$$

$$\begin{aligned}
& \frac{1}{1+m} 2^m (3+m) \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \left(\frac{1}{1 - \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2} \right)^{3/2} \left(-1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right)^2 \\
& \left(\frac{\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]}{1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2} \right)^m \\
& \left(- \left(\operatorname{AppellF1} \left[\frac{1+m}{2}, -\frac{1}{2}, m, \frac{3+m}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) / \right. \\
& \quad \left((3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, -\frac{1}{2}, m, \frac{3+m}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] - \right. \\
& \quad \left(2m \operatorname{AppellF1} \left[\frac{3+m}{2}, -\frac{1}{2}, 1+m, \frac{5+m}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \left. \operatorname{AppellF1} \left[\frac{3+m}{2}, \frac{1}{2}, m, \frac{5+m}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \right) + \\
& \left(2 \operatorname{AppellF1} \left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) / \\
& \left(\left(1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \left((3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
& \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] - \left(2(1+m) \operatorname{AppellF1} \left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \right. \right. \right. \\
& \quad \left. \left. \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] + \operatorname{AppellF1} \left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \right. \right. \\
& \quad \left. \left. \frac{5+m}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \right) + \\
& \frac{1}{1+m} 3 \times 2^m (3+m) \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \left(\frac{1}{1 - \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2} \right)^{5/2} \\
& \left(-1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right)^2 \left(\frac{\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]}{1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2} \right)^m \\
& \left(- \left(\operatorname{AppellF1} \left[\frac{1+m}{2}, -\frac{1}{2}, m, \frac{3+m}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) / \right. \\
& \quad \left((3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, -\frac{1}{2}, m, \frac{3+m}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] - \right. \\
& \quad \left(2m \operatorname{AppellF1} \left[\frac{3+m}{2}, -\frac{1}{2}, 1+m, \frac{5+m}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \left. \operatorname{AppellF1} \left[\frac{3+m}{2}, \frac{1}{2}, m, \frac{5+m}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \right) + \\
& \left(2 \operatorname{AppellF1} \left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) / \\
& \left(\left(1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \left((3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{2}(c+dx)\right]^2 - \left(2(1+m) \operatorname{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \right. \right. \\
 & \quad \left. \left. \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) + \\
 & \frac{1}{1+m} 2^{1+m} m(3+m) \tan\left[\frac{1}{2}(c+dx)\right] \left(\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^{3/2} \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \\
 & \left(\frac{\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^{-1+m} \\
 & \left(-\frac{\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2}{\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2} + \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2}{2\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right) \\
 & \left(-\left(\operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] / \right. \right. \\
 & \quad \left. \left. \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \right. \\
 & \quad \left. \left. \left(2m \operatorname{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) + \right. \\
 & \quad \left. \left. \left(2 \operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) / \right. \right. \\
 & \quad \left. \left. \left(\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \left(2(1+m) \operatorname{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \Big) + \\
 & \frac{1}{1+m} 2^{1+m} (3+m) \tan\left[\frac{1}{2}(c+dx)\right] \left(\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^{3/2} \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \\
 & \left(\frac{\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^m \\
 & \left(-\left(\left(-\frac{1}{3+m} m(1+m) \operatorname{AppellF1}\left[1+\frac{1+m}{2}, -\frac{1}{2}, 1+m, 1+\frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{2}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \frac{1}{2(3+m)}(1+m) \\
 & \operatorname{AppellF1}\left[1+\frac{1+m}{2}, \frac{1}{2}, m, 1+\frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \Big/ \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, m, \frac{3+m}{2}, \right. \right. \\
 & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \Big] - \left(2m \operatorname{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 1+m, \right. \right. \\
 & \quad \left. \left. \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, m, \right. \right. \\
 & \quad \left. \left. \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) - \\
 & \left(2 \operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \Big/ \\
 & \left(\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \right. \right. \right. \\
 & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \Big] - \left(2(1+m) \operatorname{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \right. \right. \\
 & \quad \left. \left. \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \right. \right. \\
 & \quad \left. \left. \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big) + \\
 & \left(2 \left(-\frac{1}{3+m}(1+m)^2 \operatorname{AppellF1}\left[1+\frac{1+m}{2}, -\frac{1}{2}, 2+m, 1+\frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \frac{1}{2(3+m)} \right. \right. \\
 & \quad \left. \left. (1+m) \operatorname{AppellF1}\left[1+\frac{1+m}{2}, \frac{1}{2}, 1+m, 1+\frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Big/ \\
 & \left(\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \right. \right. \right. \\
 & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \Big] - \left(2(1+m) \operatorname{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \right. \right. \\
 & \quad \left. \left. \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \right. \right. \\
 & \quad \left. \left. \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big) + \\
 & \left(\operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \\
 & \quad \left. - \left(2m \operatorname{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \\
 & (3+m) \left(-\frac{1}{3+m} m(1+m) \text{AppellF1}\left[1+\frac{1+m}{2}, -\frac{1}{2}, 1+m, 1+\frac{3+m}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \right. \\
 & \quad \left. \frac{1}{2(3+m)} (1+m) \text{AppellF1}\left[1+\frac{1+m}{2}, \frac{1}{2}, m, 1+\frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) - \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(-\frac{1}{5+m} m(3+m) \text{AppellF1}\left[1+\frac{3+m}{2}, \frac{1}{2}, 1+m, 1+\frac{5+m}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{1}{2(5+m)} (3+m) \text{AppellF1}\left[1+\frac{3+m}{2}, \frac{3}{2}, m, 1+\frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 2m \left(-\frac{1}{5+m} \right. \right. \\
 & \quad \left. \left. (1+m)(3+m) \text{AppellF1}\left[1+\frac{3+m}{2}, -\frac{1}{2}, 2+m, 1+\frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \frac{1}{2(5+m)} \right. \right. \\
 & \quad \left. \left. (3+m) \text{AppellF1}\left[1+\frac{3+m}{2}, \frac{1}{2}, 1+m, 1+\frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Big/ \\
 & \left((3+m) \text{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & \quad \left. \left(2m \text{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. \text{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \right. \\
 & \left. \left(2 \text{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. - \left(2(1+m) \text{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \text{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
& (3+m) \left(-\frac{1}{3+m} (1+m)^2 \operatorname{AppellF1}\left[1+\frac{1+m}{2}, -\frac{1}{2}, 2+m, 1+\frac{3+m}{2}, \right. \right. \\
& \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - \right. \\
& \quad \left. \frac{1}{2(3+m)} (1+m) \operatorname{AppellF1}\left[1+\frac{1+m}{2}, \frac{1}{2}, 1+m, 1+\frac{3+m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) - \\
& \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left(-\frac{1}{5+m} (1+m) (3+m) \operatorname{AppellF1}\left[1+\frac{3+m}{2}, \frac{1}{2}, 2+m, 1+\frac{5+m}{2}, \right. \right. \\
& \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
& \quad \left. \frac{1}{2(5+m)} (3+m) \operatorname{AppellF1}\left[1+\frac{3+m}{2}, \frac{3}{2}, 1+m, 1+\frac{5+m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 2(1+m) \left(-\frac{1}{5+m} \right. \right. \\
& \quad \left. \left. (2+m) (3+m) \operatorname{AppellF1}\left[1+\frac{3+m}{2}, -\frac{1}{2}, 3+m, 1+\frac{5+m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - \frac{1}{2(5+m)} \right. \right. \\
& \quad \left. \left. (3+m) \operatorname{AppellF1}\left[1+\frac{3+m}{2}, \frac{1}{2}, 2+m, 1+\frac{5+m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \\
& \left(\left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, -\frac{1}{2}, 1+m, \frac{3+m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] - \left(2(1+m) \operatorname{AppellF1}\left[\frac{3+m}{2}, -\frac{1}{2}, 2+m, \right. \right. \right. \\
& \quad \left. \left. \frac{5+m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3+m}{2}, \frac{1}{2}, 1+m, \right. \right. \\
& \quad \left. \left. \frac{5+m}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right)
\end{aligned}$$

Problem 144: Result more than twice size of optimal antiderivative.

$$\int (a + a \operatorname{Sec}[c + dx])^n (e \operatorname{Sin}[c + dx])^m dx$$

Optimal (type 6, 130 leaves, 5 steps):

$$\frac{1}{d(1-n)} e \operatorname{AppellF1}\left[1-n, \frac{1-m}{2}, \frac{1}{2}(1-m-2n), 2-n, \cos[c+dx], -\cos[c+dx]\right] (1-\cos[c+dx])^{\frac{1-m}{2}} \cos[c+dx] (1+\cos[c+dx])^{\frac{1}{2}(1-m-2n)} (a+a \sec[c+dx])^n (e \sin[c+dx])^{-1+m}$$

Result (type 6, 2135 leaves):

$$\begin{aligned}
 & \left(2^n (3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, n, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]\right)^n (a(1+\sec[c+dx]))^n \sin[c+dx]^{1+m} (e \sin[c+dx])^m\right) / \\
 & \left(d(1+m) \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, n, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
 & \quad \left. \left. 2 \left((1+m) \operatorname{AppellF1}\left[\frac{3+m}{2}, n, 2+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \right. \\
 & \quad \left. \left. \left. n \operatorname{AppellF1}\left[\frac{3+m}{2}, 1+n, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\right) \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \left(\left(2^n (3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, n, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \cos[c+dx] \left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]\right)^n \sin[c+dx]^m\right) / \\
 & \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, n, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
 & \quad \left. 2 \left((1+m) \operatorname{AppellF1}\left[\frac{3+m}{2}, n, 2+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
 & \quad \left. \left. n \operatorname{AppellF1}\left[\frac{3+m}{2}, 1+n, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\right) \\
 & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2 + \left(2^n (3+m) \left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]\right)^n \sin[c+dx]^{1+m} \right. \\
 & \quad \left. \left(-\frac{1}{3+m} (1+m)^2 \operatorname{AppellF1}\left[1+\frac{1+m}{2}, n, 2+m, 1+\frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3+m} \right. \\
 & \quad \left. (1+m) n \operatorname{AppellF1}\left[1+\frac{1+m}{2}, 1+n, 1+m, 1+\frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) / \\
 & \left((1+m) \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, n, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
 & \quad \left. \left. 2 \left((1+m) \operatorname{AppellF1}\left[\frac{3+m}{2}, n, 2+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \right. \\
 & \quad \left. \left. \left. n \operatorname{AppellF1}\left[\frac{3+m}{2}, 1+n, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\right) \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - \left(2^n (3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, n, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right.
 \end{aligned}$$

$$\begin{aligned}
& -\tan\left[\frac{1}{2}(c+dx)\right]^2 \left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]\right)^n \sin[c+dx]^{1+m} \\
& \left(-2 \left((1+m) \operatorname{AppellF1}\left[\frac{3+m}{2}, n, 2+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
& \quad \left. \left. n \operatorname{AppellF1}\left[\frac{3+m}{2}, 1+n, 1+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \right. \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + (3+m) \left(-\frac{1}{3+m} (1+m)^2 \operatorname{AppellF1}\left[1+\frac{1+m}{2}, n, \right. \right. \right. \\
& \quad \left. \left. 2+m, 1+\frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \right. \\
& \quad \left. \left. + \frac{1}{3+m} (1+m) n \operatorname{AppellF1}\left[1+\frac{1+m}{2}, 1+n, 1+m, 1+\frac{3+m}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) \right. \\
& \quad \left. 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left((1+m) \left(-\frac{1}{5+m} (2+m) (3+m) \operatorname{AppellF1}\left[1+\frac{3+m}{2}, n, \right. \right. \right. \right. \\
& \quad \left. \left. 3+m, 1+\frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{5+m} (3+m) n \operatorname{AppellF1}\left[1+\frac{3+m}{2}, 1+n, 2+m, 1+\frac{5+m}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) \right. \\
& \quad \left. n \left(-\frac{1}{5+m} (1+m) (3+m) \operatorname{AppellF1}\left[1+\frac{3+m}{2}, 1+n, 2+m, 1+\frac{5+m}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
& \quad \left. \frac{1}{5+m} (3+m) (1+n) \operatorname{AppellF1}\left[1+\frac{3+m}{2}, 2+n, 1+m, 1+\frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) \right) \right) / \\
& \left((1+m) \left((3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, n, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
& \quad \left. \left. 2 \left((1+m) \operatorname{AppellF1}\left[\frac{3+m}{2}, n, 2+m, \frac{5+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - n \operatorname{AppellF1}\left[\frac{3+m}{2}, 1+n, 1+m, \frac{5+m}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 + \\
& \left(2^n (3+m) n \operatorname{AppellF1}\left[\frac{1+m}{2}, n, 1+m, \frac{3+m}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]\right)^{-1+n} \sin[c+dx]^{1+m} \right. \\
& \quad \left. \left(-\cos\left[\frac{1}{2}(c+dx)\right] \sec[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
& \quad \left. \left. \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \tan[c+dx]\right) \right) \right) /
\end{aligned}$$

$$\begin{aligned} & \left((1+m) \left((3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, n, 1+m, \frac{3+m}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] - \right. \right. \\ & \quad 2 \left((1+m) \operatorname{AppellF1} \left[\frac{3+m}{2}, n, 2+m, \frac{5+m}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] - \right. \\ & \quad \quad n \operatorname{AppellF1} \left[\frac{3+m}{2}, 1+n, 1+m, \frac{5+m}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, \right. \\ & \quad \quad \quad \left. \left. \left. -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \tan \left[\frac{1}{2} (c+dx) \right]^2 \right) \right) \right) \end{aligned}$$

Problem 145: Unable to integrate problem.

$$\int (a + a \operatorname{Sec}[c + dx])^n \operatorname{Sin}[c + dx]^7 dx$$

Optimal (type 5, 180 leaves, 4 steps):

$$\begin{aligned} & - \left(\left((3-n) (8-n) (16-n) \operatorname{Hypergeometric2F1} [6, 4+n, 5+n, 1 + \operatorname{Sec}[c + dx]] \right. \right. \\ & \quad \left. \left. (a + a \operatorname{Sec}[c + dx])^{4+n} \right) / (42 a^4 d (1-n) (4+n)) \right) - \\ & \quad \frac{\operatorname{Cos}[c + dx]^7 (1 - \operatorname{Sec}[c + dx])^2 (a + a \operatorname{Sec}[c + dx])^{4+n}}{a^4 d (1-n)} + \frac{1}{42 a^4 d (1-n)} \\ & \quad \operatorname{Cos}[c + dx]^7 (a + a \operatorname{Sec}[c + dx])^{4+n} (6(8-n) - (108 - 25n + n^2) \operatorname{Sec}[c + dx]) \end{aligned}$$

Result (type 8, 23 leaves):

$$\int (a + a \operatorname{Sec}[c + dx])^n \operatorname{Sin}[c + dx]^7 dx$$

Problem 148: Result more than twice size of optimal antiderivative.

$$\int (a + a \operatorname{Sec}[c + dx])^n \operatorname{Sin}[c + dx] dx$$

Optimal (type 5, 42 leaves, 2 steps):

$$\frac{1}{a d (1+n)} \operatorname{Hypergeometric2F1} [2, 1+n, 2+n, 1 + \operatorname{Sec}[c + dx]] (a + a \operatorname{Sec}[c + dx])^{1+n}$$

Result (type 5, 95 leaves):

$$\begin{aligned} & \frac{1}{d (1+n)} 2^{1+n} (-\operatorname{Cos}[c + dx])^{1+n} \operatorname{Hypergeometric2F1} [n, 1+n, 2+n, 2 \operatorname{Cos} \left[\frac{1}{2} (c + dx) \right]^2] \\ & \quad \left(\operatorname{Cos} \left[\frac{1}{2} (c + dx) \right]^2 \operatorname{Sec}[c + dx] \right)^{1+n} (1 + \operatorname{Sec}[c + dx])^{-n} (a (1 + \operatorname{Sec}[c + dx]))^n \end{aligned}$$

Problem 152: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int (a + a \operatorname{Sec}[c + dx])^n \operatorname{Sin}[c + dx]^4 dx$$

Optimal (type 6, 230 leaves, 11 steps):

$$\begin{aligned}
 & - \left(\left(\text{AppellF1} \left[1 - n, -\frac{1}{2}, \frac{1}{2} - n, 2 - n, \text{Cos}[c + dx], -\text{Cos}[c + dx] \right] (1 + \text{Cos}[c + dx])^{\frac{1}{2} - n} \right. \right. \\
 & \quad \left. \left. (n - n \text{Cos}[c + dx]) \text{Cot}[c + dx] (a + a \text{Sec}[c + dx])^n \right) / \left(d (1 - n) \sqrt{1 - \text{Cos}[c + dx]} \right) \right) - \\
 & \quad \frac{\text{Cos}[c + dx] (a + a \text{Sec}[c + dx])^n \text{Sin}[c + dx]}{d} + \frac{1}{d} 2^{\frac{1}{2} + n} \\
 & \quad \text{AppellF1} \left[\frac{1}{2}, -4 + n, \frac{1}{2} - n, \frac{3}{2}, 1 - \text{Cos}[c + dx], \frac{1}{2} (1 - \text{Cos}[c + dx]) \right] \\
 & \quad \text{Cos}[c + dx]^n (1 + \text{Cos}[c + dx])^{-\frac{1}{2} - n} (a + a \text{Sec}[c + dx])^n \text{Sin}[c + dx]
 \end{aligned}$$

Result (type 6, 7069 leaves):

$$\begin{aligned}
 & \left(2^{5+n} \text{Cos} \left[\frac{1}{2} (c + dx) \right]^9 \left(\text{Cos} \left[\frac{1}{2} (c + dx) \right]^2 \text{Sec}[c + dx] \right)^n \right. \\
 & \quad \left. (1 + \text{Sec}[c + dx])^{-n} (a (1 + \text{Sec}[c + dx]))^n \text{Sin} \left[\frac{1}{2} (c + dx) \right] \left(\text{Cos}[4(c + dx)] \right. \right. \\
 & \quad \left. \left. \left(\frac{1}{16} (1 + \text{Sec}[c + dx])^n + \frac{1}{4} (1 + \text{Sec}[c + dx])^n \text{Sin}[c + dx]^2 + \frac{3}{8} (1 + \text{Sec}[c + dx])^n \right. \right. \right. \\
 & \quad \left. \left. \left. \text{Sin}[c + dx]^4 + \frac{1}{4} (1 + \text{Sec}[c + dx])^n \text{Sin}[c + dx]^6 + \frac{1}{16} (1 + \text{Sec}[c + dx])^n \text{Sin}[c + dx]^8 \right) \right) - \right. \\
 & \quad \frac{1}{16} i (1 + \text{Sec}[c + dx])^n \text{Sin}[4(c + dx)] - \frac{1}{4} i (1 + \text{Sec}[c + dx])^n \text{Sin}[c + dx]^2 \\
 & \quad \left. \text{Sin}[4(c + dx)] - \frac{3}{8} i (1 + \text{Sec}[c + dx])^n \text{Sin}[c + dx]^4 \text{Sin}[4(c + dx)] - \right. \\
 & \quad \left. \frac{1}{4} i (1 + \text{Sec}[c + dx])^n \text{Sin}[c + dx]^6 \text{Sin}[4(c + dx)] - \right. \\
 & \quad \left. \frac{1}{16} i (1 + \text{Sec}[c + dx])^n \text{Sin}[c + dx]^8 \text{Sin}[4(c + dx)] + \text{Cos}[c + dx]^8 \right) + \\
 & \quad \left(\frac{1}{16} \text{Cos}[4(c + dx)] (1 + \text{Sec}[c + dx])^n - \frac{1}{16} i (1 + \text{Sec}[c + dx])^n \text{Sin}[4(c + dx)] \right) + \\
 & \quad \text{Cos}[c + dx]^7 \left(\frac{1}{2} i \text{Cos}[4(c + dx)] (1 + \text{Sec}[c + dx])^n \text{Sin}[c + dx] + \right. \\
 & \quad \left. \frac{1}{2} (1 + \text{Sec}[c + dx])^n \text{Sin}[c + dx] \text{Sin}[4(c + dx)] \right) + \\
 & \quad \text{Cos}[c + dx]^6 \left(\text{Cos}[4(c + dx)] \left(-\frac{1}{4} (1 + \text{Sec}[c + dx])^n - \frac{7}{4} (1 + \text{Sec}[c + dx])^n \text{Sin}[c + dx]^2 \right) + \right. \\
 & \quad \left. \frac{1}{4} i (1 + \text{Sec}[c + dx])^n \text{Sin}[4(c + dx)] + \right. \\
 & \quad \left. \frac{7}{4} i (1 + \text{Sec}[c + dx])^n \text{Sin}[c + dx]^2 \text{Sin}[4(c + dx)] \right) + \\
 & \quad \text{Cos}[c + dx]^5 \left(\text{Cos}[4(c + dx)] \left(-\frac{3}{2} i (1 + \text{Sec}[c + dx])^n \text{Sin}[c + dx] - \right. \right. \\
 & \quad \left. \left. \frac{7}{2} i (1 + \text{Sec}[c + dx])^n \text{Sin}[c + dx]^3 \right) - \frac{3}{2} (1 + \text{Sec}[c + dx])^n \text{Sin}[c + dx] \right. \\
 & \quad \left. \left. \text{Sin}[4(c + dx)] - \frac{7}{2} (1 + \text{Sec}[c + dx])^n \text{Sin}[c + dx]^3 \text{Sin}[4(c + dx)] \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \cos [c+d x]^4 \left(\cos [4(c+d x)] \left(\frac{3}{8} (1+\sec [c+d x])^n + \frac{15}{4} (1+\sec [c+d x])^n \sin [c+d x]^2 + \right. \right. \\
 & \quad \left. \left. \frac{35}{8} (1+\sec [c+d x])^n \sin [c+d x]^4 \right) - \frac{3}{8} i (1+\sec [c+d x])^n \sin [4(c+d x)] - \right. \\
 & \quad \left. \frac{15}{4} i (1+\sec [c+d x])^n \sin [c+d x]^2 \sin [4(c+d x)] - \right. \\
 & \quad \left. \frac{35}{8} i (1+\sec [c+d x])^n \sin [c+d x]^4 \sin [4(c+d x)] \right) + \\
 & \cos [c+d x]^3 \left(\cos [4(c+d x)] \left(\frac{3}{2} i (1+\sec [c+d x])^n \sin [c+d x] + \right. \right. \\
 & \quad \left. \left. 5 i (1+\sec [c+d x])^n \sin [c+d x]^3 + \frac{7}{2} i (1+\sec [c+d x])^n \sin [c+d x]^5 \right) + \right. \\
 & \quad \left. \frac{3}{2} (1+\sec [c+d x])^n \sin [c+d x] \sin [4(c+d x)] + 5 (1+\sec [c+d x])^n \right. \\
 & \quad \left. \sin [c+d x]^3 \sin [4(c+d x)] + \frac{7}{2} (1+\sec [c+d x])^n \sin [c+d x]^5 \sin [4(c+d x)] \right) + \\
 & \cos [c+d x]^2 \left(\cos [4(c+d x)] \left(-\frac{1}{4} (1+\sec [c+d x])^n - \frac{9}{4} (1+\sec [c+d x])^n \sin [c+d x]^2 - \right. \right. \\
 & \quad \left. \left. \frac{15}{4} (1+\sec [c+d x])^n \sin [c+d x]^4 - \frac{7}{4} (1+\sec [c+d x])^n \sin [c+d x]^6 \right) + \right. \\
 & \quad \left. \frac{1}{4} i (1+\sec [c+d x])^n \sin [4(c+d x)] + \frac{9}{4} i (1+\sec [c+d x])^n \sin [c+d x]^2 \right. \\
 & \quad \left. \sin [4(c+d x)] + \frac{15}{4} i (1+\sec [c+d x])^n \sin [c+d x]^4 \sin [4(c+d x)] + \right. \\
 & \quad \left. \frac{7}{4} i (1+\sec [c+d x])^n \sin [c+d x]^6 \sin [4(c+d x)] \right) + \\
 & \cos [c+d x] \left(\cos [4(c+d x)] \left(-\frac{1}{2} i (1+\sec [c+d x])^n \sin [c+d x] - \right. \right. \\
 & \quad \left. \left. \frac{3}{2} i (1+\sec [c+d x])^n \sin [c+d x]^3 - \frac{3}{2} i (1+\sec [c+d x])^n \sin [c+d x]^5 - \frac{1}{2} i \right. \right. \\
 & \quad \left. \left. (1+\sec [c+d x])^n \sin [c+d x]^7 \right) - \frac{1}{2} (1+\sec [c+d x])^n \sin [c+d x] \sin [4(c+d x)] - \right. \\
 & \quad \left. \frac{3}{2} (1+\sec [c+d x])^n \sin [c+d x]^3 \sin [4(c+d x)] - \frac{3}{2} (1+\sec [c+d x])^n \right. \\
 & \quad \left. \sin [c+d x]^5 \sin [4(c+d x)] - \frac{1}{2} (1+\sec [c+d x])^n \sin [c+d x]^7 \sin [4(c+d x)] \right) \Big) \\
 & \left(\left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, 3, \frac{3}{2}, \tan \left[\frac{1}{2} (c+d x) \right]^2, -\tan \left[\frac{1}{2} (c+d x) \right]^2 \right] \sec \left[\frac{1}{2} (c+d x) \right]^4 \right) / \right. \\
 & \quad \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, 3, \frac{3}{2}, \tan \left[\frac{1}{2} (c+d x) \right]^2, -\tan \left[\frac{1}{2} (c+d x) \right]^2 \right] + \right. \\
 & \quad \left. 2 \left(-3 \operatorname{AppellF1} \left[\frac{3}{2}, n, 4, \frac{5}{2}, \tan \left[\frac{1}{2} (c+d x) \right]^2, -\tan \left[\frac{1}{2} (c+d x) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. 1+n, 3, \frac{5}{2}, \tan \left[\frac{1}{2} (c+d x) \right]^2, -\tan \left[\frac{1}{2} (c+d x) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+d x) \right]^2 \right) - \\
 & \quad \left. \left(6 \operatorname{AppellF1} \left[\frac{1}{2}, n, 4, \frac{3}{2}, \tan \left[\frac{1}{2} (c+d x) \right]^2, -\tan \left[\frac{1}{2} (c+d x) \right]^2 \right] \sec \left[\frac{1}{2} (c+d x) \right]^2 \right) / \right)
 \end{aligned}$$

$$\begin{aligned}
& \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, 4, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad 2 \left(-4 \operatorname{AppellF1} \left[\frac{3}{2}, n, 5, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \\
& \quad \quad \left. \left. 1+n, 4, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 + \\
& \operatorname{AppellF1} \left[\frac{1}{2}, n, 5, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] / \\
& \quad \left(\operatorname{AppellF1} \left[\frac{1}{2}, n, 5, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \quad \left. \frac{2}{3} \left(-5 \operatorname{AppellF1} \left[\frac{3}{2}, n, 6, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \right. \\
& \quad \quad \left. \left. 1+n, 5, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 \right) / \\
& \left(d \left(2^{4+n} \cos \left[\frac{1}{2} (c+dx) \right] \right)^{10} \left(\cos \left[\frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^n \right. \\
& \quad \left(\left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, 3, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \sec \left[\frac{1}{2} (c+dx) \right]^4 \right) / \right. \\
& \quad \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, 3, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \quad \left. 2 \left(-3 \operatorname{AppellF1} \left[\frac{3}{2}, n, 4, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \right. \\
& \quad \quad \left. \left. 1+n, 3, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 \right) - \\
& \quad \left(6 \operatorname{AppellF1} \left[\frac{1}{2}, n, 4, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \sec \left[\frac{1}{2} (c+dx) \right]^2 \right) / \\
& \quad \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, 4, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \quad \left. 2 \left(-4 \operatorname{AppellF1} \left[\frac{3}{2}, n, 5, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \right. \\
& \quad \quad \left. \left. 1+n, 4, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 + \\
& \operatorname{AppellF1} \left[\frac{1}{2}, n, 5, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] / \\
& \quad \left(\operatorname{AppellF1} \left[\frac{1}{2}, n, 5, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \quad \left. \frac{2}{3} \left(-5 \operatorname{AppellF1} \left[\frac{3}{2}, n, 6, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \right. \\
& \quad \quad \left. \left. 1+n, 5, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 \right) - \\
& 9 \times 2^{4+n} \cos \left[\frac{1}{2} (c+dx) \right]^8 \left(\cos \left[\frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^n \sin \left[\frac{1}{2} (c+dx) \right]^2 \\
& \quad \left(\left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, 3, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \sec \left[\frac{1}{2} (c+dx) \right]^4 \right) / \right. \\
& \quad \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, 3, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right.
\end{aligned}$$

$$\begin{aligned}
 & 2 \left(-3 \operatorname{AppellF1} \left[\frac{3}{2}, n, 4, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \\
 & \quad \left. \left. 1+n, 3, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 - \\
 & \left(6 \operatorname{AppellF1} \left[\frac{1}{2}, n, 4, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \right) / \\
 & \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, 4, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. 2 \left(-4 \operatorname{AppellF1} \left[\frac{3}{2}, n, 5, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. 1+n, 4, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 + \right. \\
 & \left. \operatorname{AppellF1} \left[\frac{1}{2}, n, 5, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) / \\
 & \left(\operatorname{AppellF1} \left[\frac{1}{2}, n, 5, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. \frac{2}{3} \left(-5 \operatorname{AppellF1} \left[\frac{3}{2}, n, 6, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. 1+n, 5, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 \right) + \\
 & 2^{5+n} \cos \left[\frac{1}{2} (c+dx) \right]^9 \left(\cos \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Sec} [c+dx] \right)^n \sin \left[\frac{1}{2} (c+dx) \right] \\
 & \left(\left(6 \operatorname{AppellF1} \left[\frac{1}{2}, n, 3, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^4 \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{2} (c+dx) \right] \right) \right) / \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, 3, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. 2 \left(-3 \operatorname{AppellF1} \left[\frac{3}{2}, n, 4, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. 1+n, 3, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 + \right. \\
 & \left(3 \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^4 \left(-\operatorname{AppellF1} \left[\frac{3}{2}, n, 4, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] + \frac{1}{3} n \operatorname{AppellF1} \left[\frac{3}{2}, 1+n, 3, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] \right) \right) / \\
 & \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, 3, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \left. 2 \left(-3 \operatorname{AppellF1} \left[\frac{3}{2}, n, 4, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. 1+n, 3, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 - \right. \\
 & \left(6 \operatorname{AppellF1} \left[\frac{1}{2}, n, 4, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \right. \\
 & \quad \left. \tan \left[\frac{1}{2} (c+dx) \right] \right) / \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, 4, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right.
 \end{aligned}$$

$$\begin{aligned}
& 2 \left(-4 \operatorname{AppellF1} \left[\frac{3}{2}, n, 5, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \\
& \quad \left. \left. 1+n, 4, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 - \\
& \left(6 \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \left(-\frac{4}{3} \operatorname{AppellF1} \left[\frac{3}{2}, n, 5, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \right. \\
& \quad \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] + \frac{1}{3} n \operatorname{AppellF1} \left[\frac{3}{2}, 1+n, 4, \frac{5}{2}, \right. \\
& \quad \left. \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] \left. \right) \Big/ \\
& \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, 4, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad 2 \left(-4 \operatorname{AppellF1} \left[\frac{3}{2}, n, 5, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \\
& \quad \left. \left. 1+n, 4, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 + \\
& \left. -\frac{5}{3} \operatorname{AppellF1} \left[\frac{3}{2}, n, 6, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] + \frac{1}{3} n \operatorname{AppellF1} \left[\frac{3}{2}, 1+n, 5, \frac{5}{2}, \right. \\
& \quad \left. \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] \left. \right) \Big/ \\
& \left(\operatorname{AppellF1} \left[\frac{1}{2}, n, 5, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \frac{2}{3} \left(-5 \operatorname{AppellF1} \left[\frac{3}{2}, n, 6, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \\
& \quad \left. \left. 1+n, 5, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 - \\
& \left. \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, 3, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^4 \right) \right. \\
& \quad \left(2 \left(-3 \operatorname{AppellF1} \left[\frac{3}{2}, n, 4, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \right. \\
& \quad \left. \left. 1+n, 3, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} \right. \\
& \quad \left. (c+dx) \right] + 3 \left(-\operatorname{AppellF1} \left[\frac{3}{2}, n, 4, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] + \frac{1}{3} n \operatorname{AppellF1} \left[\frac{3}{2}, 1+n, 3, \frac{5}{2}, \right. \\
& \quad \left. \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] \left. \right) + \\
& \quad 2 \tan \left[\frac{1}{2} (c+dx) \right]^2 \left(-3 \left(-\frac{12}{5} \operatorname{AppellF1} \left[\frac{5}{2}, n, 5, \frac{7}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] + \right. \\
& \quad \left. \frac{3}{5} n \operatorname{AppellF1} \left[\frac{5}{2}, 1+n, 4, \frac{7}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right)
\end{aligned}$$

$$\begin{aligned}
 & \left(\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + n \left(-\frac{9}{5} \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \\
 & \quad \left. \left. 4, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 3, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 3, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. 2 \left(-3 \operatorname{AppellF1}\left[\frac{3}{2}, n, 4, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. 1+n, 3, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 + \\
 & \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, n, 4, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left(2 \left(-4 \operatorname{AppellF1}\left[\frac{3}{2}, n, 5, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. 1+n, 4, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \quad \left. (c+dx) + 3 \left(-\frac{4}{3} \operatorname{AppellF1}\left[\frac{3}{2}, n, 5, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 4, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
 & \quad 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(-4 \left(-3 \operatorname{AppellF1}\left[\frac{5}{2}, n, 6, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 5, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + n \left(-\frac{12}{5} \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, \right. \right. \\
 & \quad \left. \left. 5, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, 4, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Big/ \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, 4, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. 2 \left(-4 \operatorname{AppellF1}\left[\frac{3}{2}, n, 5, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. 1+n, 4, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 -
 \end{aligned}$$

$$\begin{aligned}
& \left(\text{AppellF1}\left[\frac{1}{2}, n, 5, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left(-\frac{5}{3} \text{AppellF1}\left[\frac{3}{2}, n, 6, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \quad \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3} n \text{AppellF1}\left[\frac{3}{2}, 1+n, 5, \frac{5}{2}, \right. \\
& \quad \quad \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \\
& \quad \quad \frac{2}{3} \left(-5 \text{AppellF1}\left[\frac{3}{2}, n, 6, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \quad \quad \left. \left. n \text{AppellF1}\left[\frac{3}{2}, 1+n, 5, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
& \quad \quad \left. \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{3} \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(-5 \left(-\frac{18}{5} \text{AppellF1}\left[\frac{5}{2}, n, 7, \frac{7}{2}, \right. \right. \right. \right. \\
& \quad \quad \quad \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \right. \\
& \quad \quad \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{3}{5} n \text{AppellF1}\left[\frac{5}{2}, 1+n, 6, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \quad \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + n \left(-3 \text{AppellF1}\left[\frac{5}{2}, 1+n, 6, \frac{7}{2}, \right. \right. \\
& \quad \quad \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
& \quad \quad \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{3}{5} (1+n) \text{AppellF1}\left[\frac{5}{2}, 2+n, 5, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \quad \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \Big/ \\
& \quad \left(\text{AppellF1}\left[\frac{1}{2}, n, 5, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \frac{2}{3} \right. \\
& \quad \quad \left(-5 \text{AppellF1}\left[\frac{3}{2}, n, 6, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \text{AppellF1}\left[\frac{3}{2}, \right. \right. \\
& \quad \quad \quad \left. \left. 1+n, 5, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big)^2 + \\
& 2^{5+n} n \cos\left[\frac{1}{2}(c+dx)\right]^9 \left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \text{Sec}[c+dx] \right)^{-1+n} \\
& \sin\left[\frac{1}{2}(c+dx)\right] \\
& \left(\left(3 \text{AppellF1}\left[\frac{1}{2}, n, 3, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^4 \right) \Big/ \right. \\
& \quad \left(3 \text{AppellF1}\left[\frac{1}{2}, n, 3, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \quad 2 \left(-3 \text{AppellF1}\left[\frac{3}{2}, n, 4, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + n \text{AppellF1}\left[\frac{3}{2}, \right. \right. \\
& \quad \quad \quad \left. \left. 1+n, 3, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
& \quad \left(6 \text{AppellF1}\left[\frac{1}{2}, n, 4, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big/
\end{aligned}$$

$$\begin{aligned}
 & \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, 4, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad 2 \left(-4 \operatorname{AppellF1} \left[\frac{3}{2}, n, 5, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \\
 & \quad \quad \left. \left. 1+n, 4, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 \Big) + \\
 & \operatorname{AppellF1} \left[\frac{1}{2}, n, 5, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] / \\
 & \left(\operatorname{AppellF1} \left[\frac{1}{2}, n, 5, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & \quad \frac{2}{3} \left(-5 \operatorname{AppellF1} \left[\frac{3}{2}, n, 6, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \\
 & \quad \quad \left. \left. 1+n, 5, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 \Big) \\
 & \left(-\cos \left[\frac{1}{2} (c+dx) \right] \sec [c+dx] \sin \left[\frac{1}{2} (c+dx) \right] + \cos \left[\frac{1}{2} (c+dx) \right]^2 \right. \\
 & \quad \left. \sec [c+dx] \tan [c+dx] \right) \Big) \Big) \Big)
 \end{aligned}$$

Problem 153: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int (a + a \sec [c + dx])^n \sin [c + dx]^2 dx$$

Optimal (type 6, 95 leaves, 6 steps):

$$\begin{aligned}
 & -\frac{1}{d(1-n)} \operatorname{AppellF1} \left[1-n, -\frac{1}{2}, -\frac{1}{2}-n, 2-n, \cos [c+dx], -\cos [c+dx] \right] \\
 & \sqrt{1-\cos [c+dx]} (1+\cos [c+dx])^{\frac{1}{2}-n} \cot [c+dx] (a+a \sec [c+dx])^n
 \end{aligned}$$

Result (type 6, 4297 leaves):

$$\begin{aligned}
 & \left(2^{3+n} \cos \left[\frac{1}{2} (c+dx) \right]^5 \left(\cos \left[\frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^n (1+\sec [c+dx])^{-n} \right. \\
 & \quad \left(a(1+\sec [c+dx]) \right)^n \sin \left[\frac{1}{2} (c+dx) \right] \left(\cos [2(c+dx)] \left(-\frac{1}{4} (1+\sec [c+dx])^n - \right. \right. \\
 & \quad \quad \left. \left. \frac{1}{2} (1+\sec [c+dx])^n \sin [c+dx]^2 - \frac{1}{4} (1+\sec [c+dx])^n \sin [c+dx]^4 \right) + \right. \\
 & \quad \left. \frac{1}{4} i (1+\sec [c+dx])^n \sin [2(c+dx)] + \frac{1}{2} i (1+\sec [c+dx])^n \sin [c+dx]^2 \sin [2(c+dx)] + \right. \\
 & \quad \left. \frac{1}{4} i (1+\sec [c+dx])^n \sin [c+dx]^4 \sin [2(c+dx)] + \cos [c+dx]^4 \right. \\
 & \quad \left. \left(-\frac{1}{4} \cos [2(c+dx)] (1+\sec [c+dx])^n + \frac{1}{4} i (1+\sec [c+dx])^n \sin [2(c+dx)] \right) + \right. \\
 & \quad \left. \cos [c+dx]^3 (-i \cos [2(c+dx)] (1+\sec [c+dx])^n \sin [c+dx] - \right. \\
 & \quad \quad \left. \left. (1+\sec [c+dx])^n \sin [c+dx] \sin [2(c+dx)] \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
& \cos [c + d x]^2 \left(\cos [2 (c + d x)] \left(\frac{1}{2} (1 + \sec [c + d x])^n + \frac{3}{2} (1 + \sec [c + d x])^n \sin [c + d x]^2 \right) - \right. \\
& \quad \frac{1}{2} i (1 + \sec [c + d x])^n \sin [2 (c + d x)] - \\
& \quad \left. \frac{3}{2} i (1 + \sec [c + d x])^n \sin [c + d x]^2 \sin [2 (c + d x)] \right) + \cos [c + d x] \\
& \quad \left(\cos [2 (c + d x)] \left(i (1 + \sec [c + d x])^n \sin [c + d x] + i (1 + \sec [c + d x])^n \sin [c + d x]^3 \right) + \right. \\
& \quad \left. (1 + \sec [c + d x])^n \sin [c + d x] \sin [2 (c + d x)] + \right. \\
& \quad \left. (1 + \sec [c + d x])^n \sin [c + d x]^3 \sin [2 (c + d x)] \right) \\
& \left(\left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, 2, \frac{3}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] \sec \left[\frac{1}{2} (c + d x) \right]^2 \right) / \right. \\
& \quad \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, 2, \frac{3}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad \left. 2 \left(-2 \operatorname{AppellF1} \left[\frac{3}{2}, n, 3, \frac{5}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. 1 + n, 2, \frac{5}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c + d x) \right]^2 \right) - \\
& \quad \operatorname{AppellF1} \left[\frac{1}{2}, n, 3, \frac{3}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] / \\
& \quad \left(\operatorname{AppellF1} \left[\frac{1}{2}, n, 3, \frac{3}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad \left. \frac{2}{3} \left(-3 \operatorname{AppellF1} \left[\frac{3}{2}, n, 4, \frac{5}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. 1 + n, 3, \frac{5}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c + d x) \right]^2 \right) \right) / \\
& \left(d \left(2^{2+n} \cos \left[\frac{1}{2} (c + d x) \right]^6 \left(\cos \left[\frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \right)^n \right. \right. \\
& \quad \left(\left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, 2, \frac{3}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] \sec \left[\frac{1}{2} (c + d x) \right]^2 \right) / \right. \\
& \quad \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, 2, \frac{3}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad \left. 2 \left(-2 \operatorname{AppellF1} \left[\frac{3}{2}, n, 3, \frac{5}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. 1 + n, 2, \frac{5}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c + d x) \right]^2 \right) - \\
& \quad \operatorname{AppellF1} \left[\frac{1}{2}, n, 3, \frac{3}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] / \\
& \quad \left(\operatorname{AppellF1} \left[\frac{1}{2}, n, 3, \frac{3}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad \left. \frac{2}{3} \left(-3 \operatorname{AppellF1} \left[\frac{3}{2}, n, 4, \frac{5}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. 1 + n, 3, \frac{5}{2}, \tan \left[\frac{1}{2} (c + d x) \right]^2, -\tan \left[\frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c + d x) \right]^2 \right) \right) - \\
& \quad 5 \times 2^{2+n} \cos \left[\frac{1}{2} (c + d x) \right]^4 \left(\cos \left[\frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \right)^n \sin \left[\frac{1}{2} (c + d x) \right]^2
\end{aligned}$$

$$\begin{aligned}
& \frac{2}{3} \left(-3 \operatorname{AppellF1} \left[\frac{3}{2}, n, 4, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \\
& \quad \left. \left. 1+n, 3, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 - \\
& \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, 2, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \right. \\
& \quad \left. \left(2 \left(-2 \operatorname{AppellF1} \left[\frac{3}{2}, n, 3, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[\frac{3}{2}, \right. \right. \right. \right. \\
& \quad \quad \left. \left. 1+n, 2, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} \right. \right. \\
& \quad \left. \left. (c+dx) \right] + 3 \left(-\frac{2}{3} \operatorname{AppellF1} \left[\frac{3}{2}, n, 3, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \right. \\
& \quad \left. \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] + \frac{1}{3} n \operatorname{AppellF1} \left[\frac{3}{2}, 1+n, 2, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] \right) + \\
& 2 \tan \left[\frac{1}{2} (c+dx) \right]^2 \left(-2 \left(-\frac{9}{5} \operatorname{AppellF1} \left[\frac{5}{2}, n, 4, \frac{7}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] + \right. \\
& \quad \left. \frac{3}{5} n \operatorname{AppellF1} \left[\frac{5}{2}, 1+n, 3, \frac{7}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left. \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] \right) + n \left(-\frac{6}{5} \operatorname{AppellF1} \left[\frac{5}{2}, 1+n, \right. \right. \\
& \quad \left. \left. 3, \frac{7}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \right. \\
& \quad \left. \tan \left[\frac{1}{2} (c+dx) \right] + \frac{3}{5} (1+n) \operatorname{AppellF1} \left[\frac{5}{2}, 2+n, 2, \frac{7}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] \right) \right) \Big/ \\
& \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, 2, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \left. 2 \left(-2 \operatorname{AppellF1} \left[\frac{3}{2}, n, 3, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[\right. \right. \right. \\
& \quad \quad \left. \left. \frac{3}{2}, 1+n, 2, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 \right)^2 + \\
& \left(\operatorname{AppellF1} \left[\frac{1}{2}, n, 3, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left(-\operatorname{AppellF1} \left[\frac{3}{2}, n, 4, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left. \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] + \frac{1}{3} n \operatorname{AppellF1} \left[\frac{3}{2}, 1+n, 3, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] + \right. \\
& \quad \left. \frac{2}{3} \left(-3 \operatorname{AppellF1} \left[\frac{3}{2}, n, 4, \frac{5}{2}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + n \operatorname{AppellF1} \left[\right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left(5 \operatorname{AppellF1} \left[\frac{1}{4}, n, \frac{3}{2}, \frac{5}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] + 2 \left(-3 \operatorname{AppellF1} \left[\frac{5}{4}, n, \frac{5}{2}, \frac{9}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] + 2n \operatorname{AppellF1} \left[\frac{5}{4}, 1+n, \frac{3}{2}, \frac{9}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right)^2 + \\
 & \left(\operatorname{AppellF1} \left[\frac{1}{4}, n, \frac{5}{2}, \frac{5}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. \left(2 \left(-5 \operatorname{AppellF1} \left[\frac{5}{4}, n, \frac{7}{2}, \frac{9}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] + 2n \operatorname{AppellF1} \left[\frac{5}{4}, 1+n, \frac{5}{2}, \frac{9}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] + \right. \right. \\
 & \quad \left. \left. 5 \left(-\frac{1}{2} \operatorname{AppellF1} \left[\frac{5}{4}, n, \frac{7}{2}, \frac{9}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] + \frac{1}{5} n \operatorname{AppellF1} \left[\frac{5}{4}, 1+n, \frac{5}{2}, \frac{9}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) \right) \right. \\
 & \quad \left. 2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \left(-5 \left(-\frac{35}{18} \operatorname{AppellF1} \left[\frac{9}{4}, n, \frac{9}{2}, \frac{13}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] + \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{9} n \operatorname{AppellF1} \left[\frac{9}{4}, 1+n, \frac{7}{2}, \frac{13}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) + 2n \left(-\frac{25}{18} \operatorname{AppellF1} \left[\frac{9}{4}, 1+n, \frac{7}{2}, \frac{13}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] + \frac{5}{9} (1+n) \operatorname{AppellF1} \left[\frac{9}{4}, 2+n, \frac{5}{2}, \frac{13}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) \right) \right) \Big/ \\
 & \left(5 \operatorname{AppellF1} \left[\frac{1}{4}, n, \frac{5}{2}, \frac{5}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] + 2 \left(-5 \operatorname{AppellF1} \left[\frac{5}{4}, n, \frac{7}{2}, \frac{9}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] + 2n \operatorname{AppellF1} \left[\frac{5}{4}, 1+n, \frac{5}{2}, \frac{9}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right)^2 + \\
 & 5 \times 2^{1+n} n \operatorname{Cot} \left[\frac{1}{2} (c+dx) \right]^2 \left(\operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Sec} [c+dx] \right)^{-1+n} \\
 & \operatorname{Sin} [c+dx]^{5/2} \\
 & \left(\left(\operatorname{AppellF1} \left[\frac{1}{4}, n, \frac{3}{2}, \frac{5}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \right) \Big/ \right. \\
 & \quad \left. \left(5 \operatorname{AppellF1} \left[\frac{1}{4}, n, \frac{3}{2}, \frac{5}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& 2 \left(-3 \operatorname{AppellF1} \left[\frac{5}{4}, n, \frac{5}{2}, \frac{9}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] + 2n \operatorname{AppellF1} \left[\right. \right. \\
& \quad \left. \left. \frac{5}{4}, 1+n, \frac{3}{2}, \frac{9}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 - \\
& \operatorname{AppellF1} \left[\frac{1}{4}, n, \frac{5}{2}, \frac{5}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] / \\
& \left(5 \operatorname{AppellF1} \left[\frac{1}{4}, n, \frac{5}{2}, \frac{5}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \left. 2 \left(-5 \operatorname{AppellF1} \left[\frac{5}{4}, n, \frac{7}{2}, \frac{9}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] + 2n \operatorname{AppellF1} \left[\right. \right. \right. \\
& \quad \quad \left. \left. \frac{5}{4}, 1+n, \frac{5}{2}, \frac{9}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \\
& \left(-\operatorname{Cos} \left[\frac{1}{2} (c+dx) \right] \operatorname{Sec} [c+dx] \operatorname{Sin} \left[\frac{1}{2} (c+dx) \right] + \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2 \right. \\
& \quad \left. \operatorname{Sec} [c+dx] \operatorname{Tan} [c+dx] \right) \left. \right) \left. \right)
\end{aligned}$$

Problem 157: Result more than twice size of optimal antiderivative.

$$\int (a + a \operatorname{Sec} [c + dx])^n \sqrt{\operatorname{Sin} [c + dx]} dx$$

Optimal (type 6, 105 leaves, 5 steps):

$$\begin{aligned}
& - \left(\left(\operatorname{AppellF1} \left[1-n, \frac{1}{4}, \frac{1}{4}-n, 2-n, \operatorname{Cos} [c+dx], -\operatorname{Cos} [c+dx] \right] (1-\operatorname{Cos} [c+dx])^{1/4} \right. \right. \\
& \quad \left. \left. \operatorname{Cos} [c+dx] (1+\operatorname{Cos} [c+dx])^{1/4-n} (a+a \operatorname{Sec} [c+dx])^n \right) / (d(1-n) \sqrt{\operatorname{Sin} [c+dx]}) \right)
\end{aligned}$$

Result (type 6, 1758 leaves):

$$\begin{aligned}
& \left(7 \times 2^{1+n} \operatorname{AppellF1} \left[\frac{3}{4}, n, \frac{3}{2}, \frac{7}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left. \left(\operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Sec} [c+dx] \right)^n (a(1+\operatorname{Sec} [c+dx]))^n \operatorname{Sin} [c+dx]^2 \right) / \\
& \left(d \left(21 \operatorname{AppellF1} \left[\frac{3}{4}, n, \frac{3}{2}, \frac{7}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
& \quad \left. \left. 6 \left(-3 \operatorname{AppellF1} \left[\frac{7}{4}, n, \frac{5}{2}, \frac{11}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] + 2n \right. \right. \right. \\
& \quad \quad \left. \left. \operatorname{AppellF1} \left[\frac{7}{4}, 1+n, \frac{3}{2}, \frac{11}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \\
& \left(\left(21 \times 2^n \operatorname{AppellF1} \left[\frac{3}{4}, n, \frac{3}{2}, \frac{7}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
& \quad \left. \left. \operatorname{Cos} [c+dx] \left(\operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Sec} [c+dx] \right)^n \sqrt{\operatorname{Sin} [c+dx]} \right) / \right. \\
& \quad \left. \left(21 \operatorname{AppellF1} \left[\frac{3}{4}, n, \frac{3}{2}, \frac{7}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
& \quad \left. \left. 6 \left(-3 \operatorname{AppellF1} \left[\frac{7}{4}, n, \frac{5}{2}, \frac{11}{4}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] + 2n \operatorname{AppellF1} \left[\frac{7}{4}, \right. \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left. \left(1+n, \frac{3}{2}, \frac{11}{4}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
 & \left(7 \times 2^{1+n} \left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^n \sin[c+dx]^{3/2} \right. \\
 & \quad \left(-\frac{9}{14} \operatorname{AppellF1}\left[\frac{7}{4}, n, \frac{5}{2}, \frac{11}{4}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{3}{7} n \operatorname{AppellF1}\left[\frac{7}{4}, 1+n, \frac{3}{2}, \frac{11}{4}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\
 & \left(21 \operatorname{AppellF1}\left[\frac{3}{4}, n, \frac{3}{2}, \frac{7}{4}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \right. \\
 & \quad 6 \left(-3 \operatorname{AppellF1}\left[\frac{7}{4}, n, \frac{5}{2}, \frac{11}{4}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + 2 n \operatorname{AppellF1}\left[\frac{7}{4}, \right. \right. \\
 & \quad \left. \left. 1+n, \frac{3}{2}, \frac{11}{4}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & \left(7 \times 2^{1+n} \operatorname{AppellF1}\left[\frac{3}{4}, n, \frac{3}{2}, \frac{7}{4}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \\
 & \quad \left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^n \sin[c+dx]^{3/2} \\
 & \quad \left(6 \left(-3 \operatorname{AppellF1}\left[\frac{7}{4}, n, \frac{5}{2}, \frac{11}{4}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \right. \right. \\
 & \quad \left. \left. 2 n \operatorname{AppellF1}\left[\frac{7}{4}, 1+n, \frac{3}{2}, \frac{11}{4}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 21 \left(-\frac{9}{14} \operatorname{AppellF1}\left[\frac{7}{4}, n, \frac{5}{2}, \frac{11}{4}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \left. \left. \frac{3}{7} n \operatorname{AppellF1}\left[\frac{7}{4}, 1+n, \frac{3}{2}, \frac{11}{4}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 6 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
 & \quad \left(-3 \left(-\frac{35}{22} \operatorname{AppellF1}\left[\frac{11}{4}, n, \frac{7}{2}, \frac{15}{4}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{7}{11} n \operatorname{AppellF1}\left[\frac{11}{4}, 1+n, \frac{5}{2}, \frac{15}{4}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
 & \quad 2 n \left(-\frac{21}{22} \operatorname{AppellF1}\left[\frac{11}{4}, 1+n, \frac{5}{2}, \frac{15}{4}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{7}{11} (1+n) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{11}{4}, 2+n, \frac{3}{2}, \frac{15}{4}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
& \left(21 \operatorname{AppellF1} \left[\frac{3}{4}, n, \frac{3}{2}, \frac{7}{4}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad 6 \left(-3 \operatorname{AppellF1} \left[\frac{7}{4}, n, \frac{5}{2}, \frac{11}{4}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + 2n \operatorname{AppellF1} \left[\frac{7}{4}, \right. \right. \\
& \quad \quad \left. \left. 1+n, \frac{3}{2}, \frac{11}{4}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 \left. \right)^2 + \\
& \left(7 \times 2^{1+n} n \operatorname{AppellF1} \left[\frac{3}{4}, n, \frac{3}{2}, \frac{7}{4}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left(\cos \left[\frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{-1+n} \sin [c+dx]^{3/2} \\
& \quad \left(-\cos \left[\frac{1}{2} (c+dx) \right] \sec [c+dx] \sin \left[\frac{1}{2} (c+dx) \right] + \right. \\
& \quad \quad \left. \cos \left[\frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \tan [c+dx] \right) \left. \right) / \\
& \left(21 \operatorname{AppellF1} \left[\frac{3}{4}, n, \frac{3}{2}, \frac{7}{4}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad 6 \left(-3 \operatorname{AppellF1} \left[\frac{7}{4}, n, \frac{5}{2}, \frac{11}{4}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + 2n \operatorname{AppellF1} \left[\frac{7}{4}, \right. \right. \\
& \quad \quad \left. \left. 1+n, \frac{3}{2}, \frac{11}{4}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 \left. \right) \left. \right)
\end{aligned}$$

Problem 158: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sec [c + dx])^n}{\sqrt{\sin [c + dx]}} dx$$

Optimal (type 6, 105 leaves, 5 steps):

$$\begin{aligned}
& - \left(\left(\operatorname{AppellF1} \left[1-n, \frac{3}{4}, \frac{3}{4} - n, 2-n, \cos [c+dx], -\cos [c+dx] \right] (1 - \cos [c+dx])^{3/4} \right. \right. \\
& \quad \left. \left. \cos [c+dx] (1 + \cos [c+dx])^{3/4-n} (a + a \sec [c+dx])^n \right) / (d (1-n) \sin [c+dx]^{3/2}) \right)
\end{aligned}$$

Result (type 6, 1735 leaves):

$$\begin{aligned}
& \left(5 \times 2^{1+n} \operatorname{AppellF1} \left[\frac{1}{4}, n, \frac{1}{2}, \frac{5}{4}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left(\cos \left[\frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^n (a (1 + \sec [c+dx]))^n \left. \right) / \\
& \left(d \left(5 \operatorname{AppellF1} \left[\frac{1}{4}, n, \frac{1}{2}, \frac{5}{4}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] - \right. \right. \\
& \quad 2 \left(\operatorname{AppellF1} \left[\frac{5}{4}, n, \frac{3}{2}, \frac{9}{4}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] - \right. \\
& \quad \quad \left. \left. 2n \operatorname{AppellF1} \left[\frac{5}{4}, 1+n, \frac{1}{2}, \frac{9}{4}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 \right) \\
& \left(\left(5 \times 2^n \operatorname{AppellF1} \left[\frac{1}{4}, n, \frac{1}{2}, \frac{5}{4}, \tan \left[\frac{1}{2} (c+dx) \right]^2, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \cos [c+d x] \left(\cos \left[\frac{1}{2} (c+d x) \right]^2 \sec [c+d x] \right)^n / \\
& \left(\sqrt{\sin [c+d x]} \left(5 \operatorname{AppellF1} \left[\frac{1}{4}, n, \frac{1}{2}, \frac{5}{4}, \tan \left[\frac{1}{2} (c+d x) \right]^2, -\tan \left[\frac{1}{2} (c+d x) \right]^2 \right] - \right. \right. \\
& \quad \left. \left. 2 \left(\operatorname{AppellF1} \left[\frac{5}{4}, n, \frac{3}{2}, \frac{9}{4}, \tan \left[\frac{1}{2} (c+d x) \right]^2, -\tan \left[\frac{1}{2} (c+d x) \right]^2 \right] - 2 n \operatorname{AppellF1} \left[\frac{5}{4}, 1+n, \right. \right. \right. \right. \\
& \quad \quad \left. \left. \left. \frac{1}{2}, \frac{9}{4}, \tan \left[\frac{1}{2} (c+d x) \right]^2, -\tan \left[\frac{1}{2} (c+d x) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+d x) \right]^2 \right) \right) + \\
& \left(5 \times 2^{1+n} \left(\cos \left[\frac{1}{2} (c+d x) \right]^2 \sec [c+d x] \right)^n \sqrt{\sin [c+d x]} \left(-\frac{1}{10} \operatorname{AppellF1} \left[\frac{5}{4}, n, \frac{3}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. \frac{9}{4}, \tan \left[\frac{1}{2} (c+d x) \right]^2, -\tan \left[\frac{1}{2} (c+d x) \right]^2 \right] \sec \left[\frac{1}{2} (c+d x) \right]^2 \tan \left[\frac{1}{2} (c+d x) \right] + \right. \right. \\
& \quad \left. \left. \frac{1}{5} n \operatorname{AppellF1} \left[\frac{5}{4}, 1+n, \frac{1}{2}, \frac{9}{4}, \tan \left[\frac{1}{2} (c+d x) \right]^2, -\tan \left[\frac{1}{2} (c+d x) \right]^2 \right] \right. \right. \\
& \quad \left. \left. \sec \left[\frac{1}{2} (c+d x) \right]^2 \tan \left[\frac{1}{2} (c+d x) \right] \right) \right) / \\
& \left(5 \operatorname{AppellF1} \left[\frac{1}{4}, n, \frac{1}{2}, \frac{5}{4}, \tan \left[\frac{1}{2} (c+d x) \right]^2, -\tan \left[\frac{1}{2} (c+d x) \right]^2 \right] - \right. \\
& \quad \left. 2 \left(\operatorname{AppellF1} \left[\frac{5}{4}, n, \frac{3}{2}, \frac{9}{4}, \tan \left[\frac{1}{2} (c+d x) \right]^2, -\tan \left[\frac{1}{2} (c+d x) \right]^2 \right] - 2 n \operatorname{AppellF1} \left[\frac{5}{4}, \right. \right. \right. \right. \\
& \quad \quad \left. \left. \left. 1+n, \frac{1}{2}, \frac{9}{4}, \tan \left[\frac{1}{2} (c+d x) \right]^2, -\tan \left[\frac{1}{2} (c+d x) \right]^2 \right] \right) \tan \left[\frac{1}{2} (c+d x) \right]^2 \right) - \\
& \left(5 \times 2^{1+n} \operatorname{AppellF1} \left[\frac{1}{4}, n, \frac{1}{2}, \frac{5}{4}, \tan \left[\frac{1}{2} (c+d x) \right]^2, -\tan \left[\frac{1}{2} (c+d x) \right]^2 \right] \right. \\
& \quad \left. \left(\cos \left[\frac{1}{2} (c+d x) \right]^2 \sec [c+d x] \right)^n \sqrt{\sin [c+d x]} \right. \\
& \quad \left(-2 \left(\operatorname{AppellF1} \left[\frac{5}{4}, n, \frac{3}{2}, \frac{9}{4}, \tan \left[\frac{1}{2} (c+d x) \right]^2, -\tan \left[\frac{1}{2} (c+d x) \right]^2 \right] - \right. \right. \\
& \quad \quad \left. \left. 2 n \operatorname{AppellF1} \left[\frac{5}{4}, 1+n, \frac{1}{2}, \frac{9}{4}, \tan \left[\frac{1}{2} (c+d x) \right]^2, -\tan \left[\frac{1}{2} (c+d x) \right]^2 \right] \right) \right. \\
& \quad \left. \sec \left[\frac{1}{2} (c+d x) \right]^2 \tan \left[\frac{1}{2} (c+d x) \right] + 5 \left(-\frac{1}{10} \operatorname{AppellF1} \left[\frac{5}{4}, n, \frac{3}{2}, \frac{9}{4}, \right. \right. \right. \\
& \quad \quad \left. \left. \tan \left[\frac{1}{2} (c+d x) \right]^2, -\tan \left[\frac{1}{2} (c+d x) \right]^2 \right] \sec \left[\frac{1}{2} (c+d x) \right]^2 \tan \left[\frac{1}{2} (c+d x) \right] + \right. \\
& \quad \quad \left. \frac{1}{5} n \operatorname{AppellF1} \left[\frac{5}{4}, 1+n, \frac{1}{2}, \frac{9}{4}, \tan \left[\frac{1}{2} (c+d x) \right]^2, -\tan \left[\frac{1}{2} (c+d x) \right]^2 \right] \right. \\
& \quad \quad \left. \sec \left[\frac{1}{2} (c+d x) \right]^2 \tan \left[\frac{1}{2} (c+d x) \right] \right) - 2 \tan \left[\frac{1}{2} (c+d x) \right]^2 \left(-\frac{5}{6} \operatorname{AppellF1} \left[\frac{9}{4}, n, \frac{5}{2}, \right. \right. \\
& \quad \quad \left. \frac{13}{4}, \tan \left[\frac{1}{2} (c+d x) \right]^2, -\tan \left[\frac{1}{2} (c+d x) \right]^2 \right] \sec \left[\frac{1}{2} (c+d x) \right]^2 \tan \left[\frac{1}{2} (c+d x) \right] + \\
& \quad \quad \frac{5}{9} n \operatorname{AppellF1} \left[\frac{9}{4}, 1+n, \frac{3}{2}, \frac{13}{4}, \tan \left[\frac{1}{2} (c+d x) \right]^2, -\tan \left[\frac{1}{2} (c+d x) \right]^2 \right] \\
& \quad \quad \left. \sec \left[\frac{1}{2} (c+d x) \right]^2 \tan \left[\frac{1}{2} (c+d x) \right] - 2 n \left(-\frac{5}{18} \operatorname{AppellF1} \left[\frac{9}{4}, 1+n, \frac{3}{2}, \frac{13}{4}, \right. \right. \right. \\
& \quad \quad \left. \left. \tan \left[\frac{1}{2} (c+d x) \right]^2, -\tan \left[\frac{1}{2} (c+d x) \right]^2 \right) \sec \left[\frac{1}{2} (c+d x) \right]^2 \tan \left[\frac{1}{2} (c+d x) \right] + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{5}{9} (1+n) \operatorname{AppellF1}\left[\frac{9}{4}, 2+n, \frac{1}{2}, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \quad \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \Big/ \\
& \left(5 \operatorname{AppellF1}\left[\frac{1}{4}, n, \frac{1}{2}, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
& \quad 2 \left(\operatorname{AppellF1}\left[\frac{5}{4}, n, \frac{3}{2}, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] - 2n \operatorname{AppellF1}\left[\frac{5}{4}, 1+n, \right. \right. \\
& \quad \left. \left. \frac{1}{2}, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^2 + \\
& \left(5 \times 2^{1+n} n \operatorname{AppellF1}\left[\frac{1}{4}, n, \frac{1}{2}, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx]\right)^{-1+n} \sqrt{\operatorname{Sin}[c+dx]} \\
& \quad \left(-\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \operatorname{Sec}[c+dx] \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \right. \\
& \quad \left. \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx]\right) \Big/ \\
& \left(5 \operatorname{AppellF1}\left[\frac{1}{4}, n, \frac{1}{2}, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
& \quad 2 \left(\operatorname{AppellF1}\left[\frac{5}{4}, n, \frac{3}{2}, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] - 2n \operatorname{AppellF1}\left[\frac{5}{4}, \right. \right. \\
& \quad \left. \left. 1+n, \frac{1}{2}, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \Big)
\end{aligned}$$

Problem 159: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + a \operatorname{Sec}[c + dx])^n}{\operatorname{Sin}[c + dx]^{3/2}} dx$$

Optimal (type 6, 105 leaves, 5 steps):

$$\begin{aligned}
& - \left(\left(\operatorname{AppellF1}\left[1-n, \frac{5}{4}, \frac{5}{4}, -n, 2-n, \operatorname{Cos}[c+dx], -\operatorname{Cos}[c+dx]\right] (1-\operatorname{Cos}[c+dx])^{5/4} \right. \right. \\
& \quad \left. \left. \operatorname{Cos}[c+dx] (1+\operatorname{Cos}[c+dx])^{5/4-n} (a+a \operatorname{Sec}[c+dx])^n \right) \Big/ (d(1-n) \operatorname{Sin}[c+dx]^{5/2}) \right)
\end{aligned}$$

Result (type 6, 1743 leaves):

$$\begin{aligned}
& - \left(\left(3 \times 2^{1+n} \operatorname{AppellF1}\left[-\frac{1}{4}, n, -\frac{1}{2}, \frac{3}{4}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \quad \left. \left. \operatorname{Csc}[c+dx]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx]\right)^n (a(1+\operatorname{Sec}[c+dx]))^n \right) \Big/ \right. \\
& \quad \left(d \left(3 \operatorname{AppellF1}\left[-\frac{1}{4}, n, -\frac{1}{2}, \frac{3}{4}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \quad \left. \left. 2 \left(\operatorname{AppellF1}\left[\frac{3}{4}, n, \frac{1}{2}, \frac{7}{4}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + 2n \operatorname{AppellF1}\left[\frac{3}{4}, \right. \right. \right. \\
& \quad \left. \left. \left. 1+n, -\frac{1}{2}, \frac{7}{4}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right)
\end{aligned}$$

$$\begin{aligned}
& -\tan\left[\frac{1}{2}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{3}{7}(1+n) \\
& \operatorname{AppellF1}\left[\frac{7}{4}, 2+n, -\frac{1}{2}, \frac{11}{4}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\right)\bigg/\left(\sqrt{\sin[c+dx]}\right. \\
& \left.\left(3 \operatorname{AppellF1}\left[-\frac{1}{4}, n, -\frac{1}{2}, \frac{3}{4}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left(\operatorname{AppellF1}\left[\frac{3}{4}, n, \frac{1}{2}, \frac{7}{4}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2n \operatorname{AppellF1}\left[\frac{3}{4}, 1+n, \right.\right.\right.\right. \\
& \left.\left.\left.\left.-\frac{1}{2}, \frac{7}{4}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right) - \right. \\
& \left.\left(3 \times 2^{1+n} n \operatorname{AppellF1}\left[-\frac{1}{4}, n, -\frac{1}{2}, \frac{3}{4}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right.\right. \\
& \left.\left.\left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]\right)^{-1+n} \left(-\cos\left[\frac{1}{2}(c+dx)\right] \sec[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \right.\right.\right. \\
& \left.\left.\left.\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \tan[c+dx]\right)\right)\right)\bigg/\right. \\
& \left.\left(\sqrt{\sin[c+dx]}\left(3 \operatorname{AppellF1}\left[-\frac{1}{4}, n, -\frac{1}{2}, \frac{3}{4}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.\right.\right. \\
& \left.\left.\left.2 \left(\operatorname{AppellF1}\left[\frac{3}{4}, n, \frac{1}{2}, \frac{7}{4}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2n \operatorname{AppellF1}\left[\frac{3}{4}, \right.\right.\right.\right. \right. \\
& \left.\left.\left.\left.1+n, -\frac{1}{2}, \frac{7}{4}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\right)\right)
\end{aligned}$$

Problem 164: Result more than twice size of optimal antiderivative.

$$\int \csc[c+dx] (a+b \sec[c+dx]) dx$$

Optimal (type 3, 26 leaves, 5 steps):

$$-\frac{a \operatorname{ArcTanh}[\cos[c+dx]]}{d} + \frac{b \operatorname{Log}[\tan[c+dx]]}{d}$$

Result (type 3, 65 leaves):

$$-\frac{a \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} - \frac{b \operatorname{Log}[\cos[c+dx]]}{d} + \frac{a \operatorname{Log}\left[\sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \frac{b \operatorname{Log}[\sin[c+dx]]}{d}$$

Problem 171: Result more than twice size of optimal antiderivative.

$$\int \csc[c+dx]^2 (a+b \sec[c+dx]) dx$$

Optimal (type 3, 37 leaves, 7 steps):

$$\frac{b \operatorname{ArcTanh}[\sin[c+dx]]}{d} - \frac{a \operatorname{Cot}[c+dx]}{d} - \frac{b \operatorname{Csc}[c+dx]}{d}$$

Result (type 3, 106 leaves):

$$\begin{aligned}
 & - \frac{b \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{2d} - \frac{a \operatorname{Cot}[c+dx]}{d} - \frac{b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{d} + \\
 & \frac{b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{d} - \frac{b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{2d}
 \end{aligned}$$

Problem 172: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+dx]^4 (a+b \operatorname{Sec}[c+dx]) dx$$

Optimal (type 3, 69 leaves, 8 steps):

$$\frac{b \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{d} - \frac{a \operatorname{Cot}[c+dx]}{d} - \frac{a \operatorname{Cot}[c+dx]^3}{3d} - \frac{b \operatorname{Csc}[c+dx]}{d} - \frac{b \operatorname{Csc}[c+dx]^3}{3d}$$

Result (type 3, 190 leaves):

$$\begin{aligned}
 & - \frac{7b \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{12d} - \frac{2a \operatorname{Cot}[c+dx]}{3d} - \\
 & \frac{b \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{24d} - \frac{a \operatorname{Cot}[c+dx] \operatorname{Csc}[c+dx]^2}{3d} - \\
 & \frac{b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{d} + \frac{b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]}{d} - \\
 & \frac{7b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{12d} - \frac{b \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{24d}
 \end{aligned}$$

Problem 173: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+dx]^6 (a+b \operatorname{Sec}[c+dx]) dx$$

Optimal (type 3, 101 leaves, 8 steps):

$$\begin{aligned}
 & \frac{b \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{d} - \frac{a \operatorname{Cot}[c+dx]}{d} - \frac{2a \operatorname{Cot}[c+dx]^3}{3d} - \\
 & \frac{a \operatorname{Cot}[c+dx]^5}{5d} - \frac{b \operatorname{Csc}[c+dx]}{d} - \frac{b \operatorname{Csc}[c+dx]^3}{3d} - \frac{b \operatorname{Csc}[c+dx]^5}{5d}
 \end{aligned}$$

Result (type 3, 272 leaves):

$$\begin{aligned}
& - \frac{149 b \cot\left[\frac{1}{2}(c+dx)\right]}{240 d} - \frac{8 a \cot[c+dx]}{15 d} - \frac{29 b \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2}{480 d} \\
& - \frac{b \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^4}{160 d} - \frac{4 a \cot[c+dx] \operatorname{Csc}[c+dx]^2}{15 d} \\
& + \frac{a \cot[c+dx] \operatorname{Csc}[c+dx]^4}{5 d} - \frac{b \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right]}{d} \\
& + \frac{b \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right]}{d} - \frac{149 b \tan\left[\frac{1}{2}(c+dx)\right]}{240 d} \\
& - \frac{29 b \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]}{480 d} - \frac{b \sec\left[\frac{1}{2}(c+dx)\right]^4 \tan\left[\frac{1}{2}(c+dx)\right]}{160 d}
\end{aligned}$$

Problem 178: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+dx]^3 (a+b \operatorname{Sec}[c+dx])^2 dx$$

Optimal (type 3, 114 leaves, 6 steps):

$$\begin{aligned}
& - \frac{(2 a b + (a^2 + b^2) \cos[c+dx]) \operatorname{Csc}[c+dx]^2}{2 d} + \frac{(a+b)(a+3 b) \operatorname{Log}[1-\cos[c+dx]]}{4 d} \\
& - \frac{2 a b \operatorname{Log}[\cos[c+dx]]}{d} - \frac{(a-3 b)(a-b) \operatorname{Log}[1+\cos[c+dx]]}{4 d} + \frac{b^2 \operatorname{Sec}[c+dx]}{d}
\end{aligned}$$

Result (type 3, 329 leaves):

$$\begin{aligned}
& - \frac{1}{2 d \left(\operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 - \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right)} \operatorname{Csc}[c+dx]^4 \\
& \left(2 a^2 - 2 b^2 + 2 (a^2 + 3 b^2) \cos[2(c+dx)] - a^2 \cos[3(c+dx)] \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right]\right] + \right. \\
& 4 a b \cos[3(c+dx)] \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right]\right] - 3 b^2 \cos[3(c+dx)] \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right]\right] - \\
& 4 a b \cos[3(c+dx)] \operatorname{Log}[\cos[c+dx]] + a^2 \cos[3(c+dx)] \operatorname{Log}\left[\sin\left[\frac{1}{2}(c+dx)\right]\right] + \\
& 4 a b \cos[3(c+dx)] \operatorname{Log}\left[\sin\left[\frac{1}{2}(c+dx)\right]\right] + 3 b^2 \cos[3(c+dx)] \operatorname{Log}\left[\sin\left[\frac{1}{2}(c+dx)\right]\right] + \\
& \left. \cos[c+dx] \left(8 a b + (a^2 - 4 a b + 3 b^2) \operatorname{Log}\left[\cos\left[\frac{1}{2}(c+dx)\right]\right] + 4 a b \operatorname{Log}[\cos[c+dx]] - \right. \right. \\
& \left. \left. a^2 \operatorname{Log}\left[\sin\left[\frac{1}{2}(c+dx)\right]\right] - 4 a b \operatorname{Log}\left[\sin\left[\frac{1}{2}(c+dx)\right]\right] - 3 b^2 \operatorname{Log}\left[\sin\left[\frac{1}{2}(c+dx)\right]\right] \right) \right)
\end{aligned}$$

Problem 182: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+dx]^2 (a+b \operatorname{Sec}[c+dx])^2 dx$$

Optimal (type 3, 59 leaves, 8 steps):

$$\frac{2 a b \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{d} - \frac{(a^2+b^2) \operatorname{Cot}[c+d x]}{d} - \frac{2 a b \operatorname{Csc}[c+d x]}{d} + \frac{b^2 \operatorname{Tan}[c+d x]}{d}$$

Result (type 3, 138 leaves):

$$-\left(\left(\operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]\right)^3 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]\left(4 a b \operatorname{Cos}[c+d x]+(a^2+2 b^2) \operatorname{Cos}[2(c+d x)]\right)+\right. \\ \left.a\left(a+2 b\left(\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]-\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]\right)\right) \operatorname{Sin}[2(c+d x)]\right) / \left(4 d\left(-1+\operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]\right)^2\right)$$

Problem 183: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+d x]^4 (a+b \operatorname{Sec}[c+d x])^2 dx$$

Optimal (type 3, 100 leaves, 9 steps):

$$\frac{2 a b \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{d} - \frac{(a^2+2 b^2) \operatorname{Cot}[c+d x]}{d} - \\ \frac{(a^2+b^2) \operatorname{Cot}[c+d x]^3}{3 d} - \frac{2 a b \operatorname{Csc}[c+d x]}{d} - \frac{2 a b \operatorname{Csc}[c+d x]^3}{3 d} + \frac{b^2 \operatorname{Tan}[c+d x]}{d}$$

Result (type 3, 259 leaves):

$$\frac{1}{96 d\left(-1+\operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]\right)^2} \\ \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^5 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^3\left(-3 a^2-14 a b \operatorname{Cos}[c+d x]-2\left(a^2+4 b^2\right) \operatorname{Cos}[2(c+d x)]+\right. \\ \left.6 a b \operatorname{Cos}[3(c+d x)]+a^2 \operatorname{Cos}[4(c+d x)]+4 b^2 \operatorname{Cos}[4(c+d x)]-\right. \\ \left.6 a b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \operatorname{Sin}[2(c+d x)]+\right. \\ \left.6 a b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \operatorname{Sin}[2(c+d x)]+\right. \\ \left.3 a b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \operatorname{Sin}[4(c+d x)]-\right. \\ \left.3 a b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \operatorname{Sin}[4(c+d x)]\right)$$

Problem 184: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+d x]^6 (a+b \operatorname{Sec}[c+d x])^2 dx$$

Optimal (type 3, 143 leaves, 9 steps):

$$\frac{2 a b \operatorname{ArcTanh}[\sin [c+d x]]}{d} - \frac{\left(a^2+3 b^2\right) \cot [c+d x]}{d} - \frac{\left(2 a^2+3 b^2\right) \cot [c+d x]^3}{3 d} -$$

$$\frac{\left(a^2+b^2\right) \cot [c+d x]^5}{5 d} - \frac{2 a b \operatorname{Csc}[c+d x]}{d} - \frac{2 a b \operatorname{Csc}[c+d x]^3}{3 d} - \frac{2 a b \operatorname{Csc}[c+d x]^5}{5 d} + \frac{b^2 \tan [c+d x]}{d}$$

Result (type 3, 368 leaves):

$$-\frac{1}{7680 d \left(-1+\cot \left[\frac{1}{2}(c+d x)\right]^2\right)} \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^7 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^5$$

$$\left(40 a^2+196 a b \cos [c+d x]+20\left(a^2+6 b^2\right) \cos [2(c+d x)]-130 a b \cos [3(c+d x)]-\right.$$

$$16 a^2 \cos [4(c+d x)]-96 b^2 \cos [4(c+d x)]+30 a b \cos [5(c+d x)]+4 a^2 \cos [6(c+d x)]+$$

$$24 b^2 \cos [6(c+d x)]+75 a b \log \left[\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right] \sin [2(c+d x)]-$$

$$75 a b \log \left[\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right] \sin [2(c+d x)]-$$

$$60 a b \log \left[\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right] \sin [4(c+d x)]+$$

$$60 a b \log \left[\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right] \sin [4(c+d x)]+$$

$$15 a b \log \left[\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right] \sin [6(c+d x)]-$$

$$\left.15 a b \log \left[\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right] \sin [6(c+d x)]\right)$$

Problem 189: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+d x]^3 (a+b \operatorname{Sec}[c+d x])^3 dx$$

Optimal (type 3, 162 leaves, 6 steps):

$$-\frac{a^2\left(b\left(3+\frac{b^2}{a^2}\right)+a\left(1+\frac{3 b^2}{a^2}\right) \cos [c+d x]\right) \operatorname{Csc}[c+d x]^2}{2 d} +$$

$$\frac{(a+b)^2(a+4 b) \log [1-\cos [c+d x]]}{4 d} - \frac{b\left(3 a^2+2 b^2\right) \log [\cos [c+d x]]}{d} -$$

$$\frac{(a-4 b)(a-b)^2 \log [1+\cos [c+d x]]}{4 d} + \frac{3 a b^2 \operatorname{Sec}[c+d x]}{d} + \frac{b^3 \operatorname{Sec}[c+d x]^2}{2 d}$$

Result (type 3, 669 leaves):

$$\frac{3 a b^2 \cos [c+d x]^3 (a+b \sec [c+d x])^3}{d (b+a \cos [c+d x])^3} +$$

$$\left((-a^3 - 3 a^2 b - 3 a b^2 - b^3) \cos [c+d x]^3 \operatorname{Csc}\left[\frac{1}{2}(c+d x)\right]^2 (a+b \sec [c+d x])^3 \right) /$$

$$(8 d (b+a \cos [c+d x])^3) +$$

$$\left((-a^3 + 6 a^2 b - 9 a b^2 + 4 b^3) \cos [c+d x]^3 \operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right]\right] (a+b \sec [c+d x])^3 \right) /$$

$$(2 d (b+a \cos [c+d x])^3) + \frac{(-3 a^2 b - 2 b^3) \cos [c+d x]^3 \operatorname{Log}[\cos [c+d x]] (a+b \sec [c+d x])^3}{d (b+a \cos [c+d x])^3} +$$

$$\left((a^3 + 6 a^2 b + 9 a b^2 + 4 b^3) \cos [c+d x]^3 \operatorname{Log}\left[\sin \left[\frac{1}{2}(c+d x)\right]\right] (a+b \sec [c+d x])^3 \right) /$$

$$(2 d (b+a \cos [c+d x])^3) +$$

$$\left((a^3 - 3 a^2 b + 3 a b^2 - b^3) \cos [c+d x]^3 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 (a+b \sec [c+d x])^3 \right) /$$

$$(8 d (b+a \cos [c+d x])^3) + \frac{b^3 \cos [c+d x]^3 (a+b \sec [c+d x])^3}{4 d (b+a \cos [c+d x])^3 \left(\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right)^2} +$$

$$\frac{3 a b^2 \cos [c+d x]^3 (a+b \sec [c+d x])^3 \sin \left[\frac{1}{2}(c+d x)\right]}{d (b+a \cos [c+d x])^3 \left(\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right)} +$$

$$\frac{b^3 \cos [c+d x]^3 (a+b \sec [c+d x])^3}{4 d (b+a \cos [c+d x])^3 \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^2} -$$

$$\frac{3 a b^2 \cos [c+d x]^3 (a+b \sec [c+d x])^3 \sin \left[\frac{1}{2}(c+d x)\right]}{d (b+a \cos [c+d x])^3 \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)}$$

Problem 190: Result more than twice size of optimal antiderivative.

$$\int (a+b \sec [c+d x])^3 \sin [c+d x]^6 dx$$

Optimal (type 3, 299 leaves, 21 steps):

$$\frac{5 a^3 x}{16} - \frac{45}{8} a b^2 x + \frac{3 a^2 b \operatorname{ArcTanh}[\sin [c+d x]]}{d} - \frac{5 b^3 \operatorname{ArcTanh}[\sin [c+d x]]}{2 d} -$$

$$\frac{3 a^2 b \sin [c+d x]}{d} + \frac{5 b^3 \sin [c+d x]}{2 d} - \frac{5 a^3 \cos [c+d x] \sin [c+d x]}{16 d} - \frac{a^2 b \sin [c+d x]^3}{d} +$$

$$\frac{5 b^3 \sin [c+d x]^3}{6 d} - \frac{5 a^3 \cos [c+d x] \sin [c+d x]^3}{24 d} - \frac{3 a^2 b \sin [c+d x]^5}{5 d} -$$

$$\frac{a^3 \cos [c+d x] \sin [c+d x]^5}{6 d} + \frac{45 a b^2 \tan [c+d x]}{8 d} - \frac{15 a b^2 \sin [c+d x]^2 \tan [c+d x]}{8 d} -$$

$$\frac{3 a b^2 \sin [c+d x]^4 \tan [c+d x]}{4 d} + \frac{b^3 \sin [c+d x]^3 \tan [c+d x]^2}{2 d}$$

Result (type 3, 818 leaves):

$$\begin{aligned}
 & \frac{5 a (a^2 - 18 b^2) (c + d x) \operatorname{Cos}[c + d x]^3 (a + b \operatorname{Sec}[c + d x])^3}{16 d (b + a \operatorname{Cos}[c + d x])^3} + \\
 & \left((-6 a^2 b + 5 b^3) \operatorname{Cos}[c + d x]^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] (a + b \operatorname{Sec}[c + d x])^3 \right) / \\
 & \left(2 d (b + a \operatorname{Cos}[c + d x])^3 \right) + \\
 & \left((6 a^2 b - 5 b^3) \operatorname{Cos}[c + d x]^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] (a + b \operatorname{Sec}[c + d x])^3 \right) / \\
 & \left(2 d (b + a \operatorname{Cos}[c + d x])^3 \right) + \frac{b^3 \operatorname{Cos}[c + d x]^3 (a + b \operatorname{Sec}[c + d x])^3}{4 d (b + a \operatorname{Cos}[c + d x])^3 \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} + \\
 & \frac{3 a b^2 \operatorname{Cos}[c + d x]^3 (a + b \operatorname{Sec}[c + d x])^3 \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]}{d (b + a \operatorname{Cos}[c + d x])^3 \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)} - \\
 & \frac{b^3 \operatorname{Cos}[c + d x]^3 (a + b \operatorname{Sec}[c + d x])^3}{4 d (b + a \operatorname{Cos}[c + d x])^3 \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} + \\
 & \frac{3 a b^2 \operatorname{Cos}[c + d x]^3 (a + b \operatorname{Sec}[c + d x])^3 \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]}{d (b + a \operatorname{Cos}[c + d x])^3 \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)} + \\
 & \frac{3 b (-11 a^2 + 6 b^2) \operatorname{Cos}[c + d x]^3 (a + b \operatorname{Sec}[c + d x])^3 \operatorname{Sin}[c + d x]}{8 d (b + a \operatorname{Cos}[c + d x])^3} - \\
 & \frac{3 a (5 a^2 - 32 b^2) \operatorname{Cos}[c + d x]^3 (a + b \operatorname{Sec}[c + d x])^3 \operatorname{Sin}[2(c + d x)]}{64 d (b + a \operatorname{Cos}[c + d x])^3} - \\
 & \frac{b (-21 a^2 + 4 b^2) \operatorname{Cos}[c + d x]^3 (a + b \operatorname{Sec}[c + d x])^3 \operatorname{Sin}[3(c + d x)]}{48 d (b + a \operatorname{Cos}[c + d x])^3} + \\
 & \frac{3 a (a^2 - 2 b^2) \operatorname{Cos}[c + d x]^3 (a + b \operatorname{Sec}[c + d x])^3 \operatorname{Sin}[4(c + d x)]}{64 d (b + a \operatorname{Cos}[c + d x])^3} - \\
 & \frac{3 a^2 b \operatorname{Cos}[c + d x]^3 (a + b \operatorname{Sec}[c + d x])^3 \operatorname{Sin}[5(c + d x)]}{80 d (b + a \operatorname{Cos}[c + d x])^3} - \\
 & \frac{a^3 \operatorname{Cos}[c + d x]^3 (a + b \operatorname{Sec}[c + d x])^3 \operatorname{Sin}[6(c + d x)]}{192 d (b + a \operatorname{Cos}[c + d x])^3}
 \end{aligned}$$

Problem 191: Result more than twice size of optimal antiderivative.

$$\int (a + b \operatorname{Sec}[c + d x])^3 \operatorname{Sin}[c + d x]^4 dx$$

Optimal (type 3, 236 leaves, 8 steps):

$$\frac{3}{8} a (a^2 - 12 b^2) x + \frac{3 b (2 a^2 - b^2) \text{ArcTanh}[\text{Sin}[c + d x]]}{2 d} -$$

$$\frac{b (17 a^2 - b^2) \text{Sin}[c + d x]}{2 d} - \frac{a (21 a^2 - 2 b^2) \text{Cos}[c + d x] \text{Sin}[c + d x]}{8 d} -$$

$$\frac{(6 a^2 - b^2) (b + a \text{Cos}[c + d x])^2 \text{Sin}[c + d x]}{4 b d} - \frac{(4 a^2 - b^2) (b + a \text{Cos}[c + d x])^3 \text{Sin}[c + d x]}{4 b^2 d} +$$

$$\frac{a (b + a \text{Cos}[c + d x])^4 \text{Tan}[c + d x]}{b^2 d} + \frac{(b + a \text{Cos}[c + d x])^4 \text{Sec}[c + d x] \text{Tan}[c + d x]}{2 b d}$$

Result (type 3, 696 leaves):

$$\frac{3 a (a^2 - 12 b^2) (c + d x) \text{Cos}[c + d x]^3 (a + b \text{Sec}[c + d x])^3}{8 d (b + a \text{Cos}[c + d x])^3} +$$

$$\left(\frac{3 (-2 a^2 b + b^3) \text{Cos}[c + d x]^3 \text{Log}\left[\text{Cos}\left[\frac{1}{2} (c + d x)\right] - \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right] (a + b \text{Sec}[c + d x])^3}{2 d (b + a \text{Cos}[c + d x])^3} - \right.$$

$$\left. \frac{3 (-2 a^2 b + b^3) \text{Cos}[c + d x]^3 \text{Log}\left[\text{Cos}\left[\frac{1}{2} (c + d x)\right] + \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right] (a + b \text{Sec}[c + d x])^3}{2 d (b + a \text{Cos}[c + d x])^3} + \frac{b^3 \text{Cos}[c + d x]^3 (a + b \text{Sec}[c + d x])^3}{4 d (b + a \text{Cos}[c + d x])^3 \left(\text{Cos}\left[\frac{1}{2} (c + d x)\right] - \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right)^2} + \right.$$

$$\frac{3 a b^2 \text{Cos}[c + d x]^3 (a + b \text{Sec}[c + d x])^3 \text{Sin}\left[\frac{1}{2} (c + d x)\right]}{d (b + a \text{Cos}[c + d x])^3 \left(\text{Cos}\left[\frac{1}{2} (c + d x)\right] - \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right)} -$$

$$\frac{b^3 \text{Cos}[c + d x]^3 (a + b \text{Sec}[c + d x])^3}{4 d (b + a \text{Cos}[c + d x])^3 \left(\text{Cos}\left[\frac{1}{2} (c + d x)\right] + \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right)^2} +$$

$$\frac{3 a b^2 \text{Cos}[c + d x]^3 (a + b \text{Sec}[c + d x])^3 \text{Sin}\left[\frac{1}{2} (c + d x)\right]}{d (b + a \text{Cos}[c + d x])^3 \left(\text{Cos}\left[\frac{1}{2} (c + d x)\right] + \text{Sin}\left[\frac{1}{2} (c + d x)\right]\right)} +$$

$$\frac{b (-15 a^2 + 4 b^2) \text{Cos}[c + d x]^3 (a + b \text{Sec}[c + d x])^3 \text{Sin}[c + d x]}{4 d (b + a \text{Cos}[c + d x])^3} -$$

$$\frac{a (a^2 - 3 b^2) \text{Cos}[c + d x]^3 (a + b \text{Sec}[c + d x])^3 \text{Sin}[2 (c + d x)]}{4 d (b + a \text{Cos}[c + d x])^3} +$$

$$\frac{a^2 b \text{Cos}[c + d x]^3 (a + b \text{Sec}[c + d x])^3 \text{Sin}[3 (c + d x)]}{4 d (b + a \text{Cos}[c + d x])^3} +$$

$$\frac{a^3 \text{Cos}[c + d x]^3 (a + b \text{Sec}[c + d x])^3 \text{Sin}[4 (c + d x)]}{32 d (b + a \text{Cos}[c + d x])^3}$$

Problem 192: Result more than twice size of optimal antiderivative.

$$\int (a + b \operatorname{Sec}[c + dx])^3 \operatorname{Sin}[c + dx]^2 dx$$

Optimal (type 3, 138 leaves, 8 steps):

$$\frac{1}{2} a (a^2 - 6 b^2) x + \frac{b (6 a^2 - b^2) \operatorname{ArcTanh}[\operatorname{Sin}[c + dx]]}{2 d} - \frac{15 a^2 b \operatorname{Sin}[c + dx]}{2 d} - \frac{5 a^3 \operatorname{Cos}[c + dx] \operatorname{Sin}[c + dx]}{2 d} + \frac{3 a (b + a \operatorname{Cos}[c + dx])^2 \operatorname{Tan}[c + dx]}{2 d} + \frac{(b + a \operatorname{Cos}[c + dx])^3 \operatorname{Sec}[c + dx] \operatorname{Tan}[c + dx]}{2 d}$$

Result (type 3, 327 leaves):

$$\frac{1}{4 d} \operatorname{Sec}[c + dx]^2 \left(a^3 c - 6 a b^2 c + a^3 dx - 6 a b^2 dx - 6 a^2 b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] \right) + b^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] + 6 a^2 b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] - b^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] + \operatorname{Cos}[2(c + dx)] \left(a (a^2 - 6 b^2) (c + dx) + (-6 a^2 b + b^3) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] - b (-6 a^2 + b^2) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]\right] \right) + (-3 a^2 b + 2 b^3) \operatorname{Sin}[c + dx] - \frac{1}{2} a^3 \operatorname{Sin}[2(c + dx)] + 6 a b^2 \operatorname{Sin}[2(c + dx)] - 3 a^2 b \operatorname{Sin}[3(c + dx)] - \frac{1}{4} a^3 \operatorname{Sin}[4(c + dx)] \right)$$

Problem 193: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c + dx]^2 (a + b \operatorname{Sec}[c + dx])^3 dx$$

Optimal (type 3, 133 leaves, 15 steps):

$$\frac{3 a^2 b \operatorname{ArcTanh}[\operatorname{Sin}[c + dx]]}{d} + \frac{3 b^3 \operatorname{ArcTanh}[\operatorname{Sin}[c + dx]]}{2 d} - \frac{a^3 \operatorname{Cot}[c + dx]}{d} - \frac{3 a b^2 \operatorname{Cot}[c + dx]}{d} - \frac{3 a^2 b \operatorname{Csc}[c + dx]}{d} - \frac{3 b^3 \operatorname{Csc}[c + dx]}{2 d} + \frac{b^3 \operatorname{Csc}[c + dx] \operatorname{Sec}[c + dx]^2}{2 d} + \frac{3 a b^2 \operatorname{Tan}[c + dx]}{d}$$

Result (type 3, 406 leaves):

$$\begin{aligned}
 & - \frac{1}{16 d \left(-1 + \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]^2\right)^2} \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^5 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \\
 & \left(12 a^2 b + 2 b^3 + 6 a (a^2 + 2 b^2) \operatorname{Cos}[c+dx] + 6 (2 a^2 b + b^3) \operatorname{Cos}[2(c+dx)] + 2 a^3 \operatorname{Cos}[3(c+dx)] + \right. \\
 & \quad 12 a b^2 \operatorname{Cos}[3(c+dx)] + 6 a^2 b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[c+dx] + \\
 & \quad 3 b^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[c+dx] - \\
 & \quad 6 a^2 b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[c+dx] - \\
 & \quad 3 b^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[c+dx] + \\
 & \quad 6 a^2 b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[3(c+dx)] + \\
 & \quad 3 b^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[3(c+dx)] - \\
 & \quad 6 a^2 b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[3(c+dx)] - \\
 & \quad \left. 3 b^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[3(c+dx)]\right)
 \end{aligned}$$

Problem 194: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+dx]^4 (a+b \operatorname{Sec}[c+dx])^3 dx$$

Optimal (type 3, 205 leaves, 17 steps):

$$\begin{aligned}
 & \frac{3 a^2 b \operatorname{ArcTanh}\left[\operatorname{Sin}[c+dx]\right]}{d} + \frac{5 b^3 \operatorname{ArcTanh}\left[\operatorname{Sin}[c+dx]\right]}{2 d} - \frac{a^3 \operatorname{Cot}[c+dx]}{d} - \frac{6 a b^2 \operatorname{Cot}[c+dx]}{d} \\
 & \frac{a^3 \operatorname{Cot}[c+dx]^3}{3 d} - \frac{a b^2 \operatorname{Cot}[c+dx]^3}{d} - \frac{3 a^2 b \operatorname{Csc}[c+dx]}{d} - \frac{5 b^3 \operatorname{Csc}[c+dx]}{2 d} \\
 & \frac{a^2 b \operatorname{Csc}[c+dx]^3}{d} - \frac{5 b^3 \operatorname{Csc}[c+dx]^3}{6 d} + \frac{b^3 \operatorname{Csc}[c+dx]^3 \operatorname{Sec}[c+dx]^2}{2 d} + \frac{3 a b^2 \operatorname{Tan}[c+dx]}{d}
 \end{aligned}$$

Result (type 3, 610 leaves):

$$\begin{aligned}
& - \frac{1}{768 d \left(-1 + \operatorname{Cot} \left[\frac{1}{2} (c + d x) \right] \right)^2} \\
& \operatorname{Csc} \left[\frac{1}{2} (c + d x) \right]^7 \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right]^3 \left(84 a^2 b + 22 b^3 + 32 a (a^2 + 3 b^2) \operatorname{Cos} [c + d x] + \right. \\
& 8 (6 a^2 b + 5 b^3) \operatorname{Cos} [2 (c + d x)] + 4 a^3 \operatorname{Cos} [3 (c + d x)] + 48 a b^2 \operatorname{Cos} [3 (c + d x)] - \\
& 36 a^2 b \operatorname{Cos} [4 (c + d x)] - 30 b^3 \operatorname{Cos} [4 (c + d x)] - 4 a^3 \operatorname{Cos} [5 (c + d x)] - \\
& 48 a b^2 \operatorname{Cos} [5 (c + d x)] + 36 a^2 b \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] \operatorname{Sin} [c + d x] + \\
& 30 b^3 \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] \operatorname{Sin} [c + d x] - \\
& 36 a^2 b \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] \operatorname{Sin} [c + d x] - \\
& 30 b^3 \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] \operatorname{Sin} [c + d x] + \\
& 18 a^2 b \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] \operatorname{Sin} [3 (c + d x)] + \\
& 15 b^3 \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] \operatorname{Sin} [3 (c + d x)] - \\
& 18 a^2 b \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] \operatorname{Sin} [3 (c + d x)] - \\
& 15 b^3 \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] \operatorname{Sin} [3 (c + d x)] - \\
& 18 a^2 b \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] \operatorname{Sin} [5 (c + d x)] - \\
& 15 b^3 \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] \operatorname{Sin} [5 (c + d x)] + \\
& 18 a^2 b \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] \operatorname{Sin} [5 (c + d x)] + \\
& \left. 15 b^3 \operatorname{Log} \left[\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right] \operatorname{Sin} [5 (c + d x)] \right)
\end{aligned}$$

Problem 195: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Csc} [c + d x]^6 (a + b \operatorname{Sec} [c + d x])^3 dx$$

Optimal (type 3, 279 leaves, 17 steps):

$$\begin{aligned}
& \frac{3 a^2 b \operatorname{ArcTanh} [\operatorname{Sin} [c + d x]]}{d} + \frac{7 b^3 \operatorname{ArcTanh} [\operatorname{Sin} [c + d x]]}{2 d} - \frac{a^3 \operatorname{Cot} [c + d x]}{d} - \frac{9 a b^2 \operatorname{Cot} [c + d x]}{d} \\
& - \frac{2 a^3 \operatorname{Cot} [c + d x]^3}{3 d} - \frac{3 a b^2 \operatorname{Cot} [c + d x]^3}{d} - \frac{a^3 \operatorname{Cot} [c + d x]^5}{5 d} - \frac{3 a b^2 \operatorname{Cot} [c + d x]^5}{5 d} \\
& - \frac{3 a^2 b \operatorname{Csc} [c + d x]}{d} - \frac{7 b^3 \operatorname{Csc} [c + d x]}{2 d} - \frac{a^2 b \operatorname{Csc} [c + d x]^3}{d} - \frac{7 b^3 \operatorname{Csc} [c + d x]^3}{6 d} \\
& - \frac{3 a^2 b \operatorname{Csc} [c + d x]^5}{5 d} - \frac{7 b^3 \operatorname{Csc} [c + d x]^5}{10 d} + \frac{b^3 \operatorname{Csc} [c + d x]^5 \operatorname{Sec} [c + d x]^2}{2 d} + \frac{3 a b^2 \operatorname{Tan} [c + d x]}{d}
\end{aligned}$$

Result (type 3, 812 leaves):

$$\begin{aligned}
 & - \frac{1}{61440 d \left(-1 + \cot\left[\frac{1}{2}(c+dx)\right]\right)^2} \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^9 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 \\
 & \left(1176 a^2 b + 412 b^3 + 80 a (5 a^2 + 18 b^2) \operatorname{Cos}[c+dx] + 66 (6 a^2 b + 7 b^3) \operatorname{Cos}[2(c+dx)] + \right. \\
 & \quad 16 a^3 \operatorname{Cos}[3(c+dx)] + 288 a b^2 \operatorname{Cos}[3(c+dx)] - 600 a^2 b \operatorname{Cos}[4(c+dx)] - \\
 & \quad 700 b^3 \operatorname{Cos}[4(c+dx)] - 48 a^3 \operatorname{Cos}[5(c+dx)] - 864 a b^2 \operatorname{Cos}[5(c+dx)] + \\
 & \quad 180 a^2 b \operatorname{Cos}[6(c+dx)] + 210 b^3 \operatorname{Cos}[6(c+dx)] + 16 a^3 \operatorname{Cos}[7(c+dx)] + \\
 & \quad 288 a b^2 \operatorname{Cos}[7(c+dx)] + 450 a^2 b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[c+dx] + \\
 & \quad 525 b^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[c+dx] - \\
 & \quad 450 a^2 b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[c+dx] - \\
 & \quad 525 b^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[c+dx] + \\
 & \quad 90 a^2 b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[3(c+dx)] + \\
 & \quad 105 b^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[3(c+dx)] - \\
 & \quad 90 a^2 b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[3(c+dx)] - \\
 & \quad 105 b^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[3(c+dx)] - \\
 & \quad 270 a^2 b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[5(c+dx)] - \\
 & \quad 315 b^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[5(c+dx)] + \\
 & \quad 270 a^2 b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[5(c+dx)] + \\
 & \quad 315 b^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[5(c+dx)] + \\
 & \quad 90 a^2 b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[7(c+dx)] + \\
 & \quad 105 b^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[7(c+dx)] - \\
 & \quad 90 a^2 b \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[7(c+dx)] - \\
 & \quad \left. 105 b^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sin}[7(c+dx)] \right)
 \end{aligned}$$

Problem 202: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Csc}[c+dx]^5}{a+b \operatorname{Sec}[c+dx]} dx$$

Optimal (type 3, 179 leaves, 7 steps):

$$\frac{(4 a^2 b - a (3 a^2 + b^2) \cos [c + d x]) \operatorname{Csc}[c + d x]^2}{8 (a^2 - b^2)^2 d} + \frac{(b - a \cos [c + d x]) \operatorname{Csc}[c + d x]^4}{4 (a^2 - b^2) d} +$$

$$\frac{a (3 a + b) \operatorname{Log}[1 - \cos [c + d x]]}{16 (a + b)^3 d} - \frac{a (3 a - b) \operatorname{Log}[1 + \cos [c + d x]]}{16 (a - b)^3 d} + \frac{a^4 b \operatorname{Log}[b + a \cos [c + d x]]}{(a^2 - b^2)^3 d}$$

Result (type 3, 409 leaves):

$$\frac{(-3 a - b) (b + a \cos [c + d x]) \operatorname{Csc}\left[\frac{1}{2}(c + d x)\right]^2 \operatorname{Sec}[c + d x]}{32 (a + b)^2 d (a + b \operatorname{Sec}[c + d x])} -$$

$$\frac{(b + a \cos [c + d x]) \operatorname{Csc}\left[\frac{1}{2}(c + d x)\right]^4 \operatorname{Sec}[c + d x]}{64 (a + b) d (a + b \operatorname{Sec}[c + d x])} +$$

$$\frac{(3 a^2 - a b) (b + a \cos [c + d x]) \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + d x)\right]\right] \operatorname{Sec}[c + d x]}{8 (-a + b)^3 d (a + b \operatorname{Sec}[c + d x])} -$$

$$\frac{a^4 b (b + a \cos [c + d x]) \operatorname{Log}[b + a \cos [c + d x]] \operatorname{Sec}[c + d x]}{(-a^2 + b^2)^3 d (a + b \operatorname{Sec}[c + d x])} +$$

$$\frac{(3 a^2 + a b) (b + a \cos [c + d x]) \operatorname{Log}\left[\sin\left[\frac{1}{2}(c + d x)\right]\right] \operatorname{Sec}[c + d x]}{8 (a + b)^3 d (a + b \operatorname{Sec}[c + d x])} +$$

$$\frac{(3 a - b) (b + a \cos [c + d x]) \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \operatorname{Sec}[c + d x]}{32 (-a + b)^2 d (a + b \operatorname{Sec}[c + d x])} -$$

$$\frac{(b + a \cos [c + d x]) \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^4 \operatorname{Sec}[c + d x]}{64 (-a + b) d (a + b \operatorname{Sec}[c + d x])}$$

Problem 226: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Csc}[c + d x]^3}{(a + b \operatorname{Sec}[c + d x])^3} dx$$

Optimal (type 3, 229 leaves, 5 steps):

$$-\frac{b^3}{2 (a^2 - b^2)^2 d (b + a \cos [c + d x])^2} + \frac{b^2 (3 a^2 + b^2)}{(a^2 - b^2)^3 d (b + a \cos [c + d x])} +$$

$$\frac{(b (3 a^2 + b^2) - a (a^2 + 3 b^2) \cos [c + d x]) \operatorname{Csc}[c + d x]^2}{2 (a^2 - b^2)^3 d} + \frac{(a - 2 b) \operatorname{Log}[1 - \cos [c + d x]]}{4 (a + b)^4 d} -$$

$$\frac{(a + 2 b) \operatorname{Log}[1 + \cos [c + d x]]}{4 (a - b)^4 d} + \frac{b (3 a^4 + 8 a^2 b^2 + b^4) \operatorname{Log}[b + a \cos [c + d x]]}{(a^2 - b^2)^4 d}$$

Result (type 3, 332 leaves):

$$\begin{aligned}
 & - \frac{2 i (3 a^4 b + 8 a^2 b^3 + b^5) (c + d x)}{(a - b)^4 (a + b)^4 d} - \frac{i (-a - 2 b) \text{ArcTan}[\text{Tan}[c + d x]]}{2 (-a + b)^4 d} - \\
 & \frac{i (a - 2 b) \text{ArcTan}[\text{Tan}[c + d x]]}{2 (a + b)^4 d} - \frac{b^3}{2 (-a + b)^2 (a + b)^2 d (b + a \text{Cos}[c + d x])^2} - \\
 & \frac{b^2 (3 a^2 + b^2)}{(-a + b)^3 (a + b)^3 d (b + a \text{Cos}[c + d x])} - \frac{\text{Csc}\left[\frac{1}{2} (c + d x)\right]^2}{8 (a + b)^3 d} + \frac{(-a - 2 b) \text{Log}\left[\text{Cos}\left[\frac{1}{2} (c + d x)\right]^2\right]}{4 (-a + b)^4 d} + \\
 & \frac{(3 a^4 b + 8 a^2 b^3 + b^5) \text{Log}[b + a \text{Cos}[c + d x]]}{(-a^2 + b^2)^4 d} + \frac{(a - 2 b) \text{Log}\left[\text{Sin}\left[\frac{1}{2} (c + d x)\right]^2\right]}{4 (a + b)^4 d} - \frac{\text{Sec}\left[\frac{1}{2} (c + d x)\right]^2}{8 (-a + b)^3 d}
 \end{aligned}$$

Problem 227: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\text{Csc}[c + d x]^5}{(a + b \text{Sec}[c + d x])^3} dx$$

Optimal (type 3, 313 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{a^2 b^3}{2 (a^2 - b^2)^3 d (b + a \text{Cos}[c + d x])^2} + \frac{3 a^2 b^2 (a^2 + b^2)}{(a^2 - b^2)^4 d (b + a \text{Cos}[c + d x])} + \frac{1}{8 (a^2 - b^2)^4 d} \\
 & \frac{(4 b (3 a^4 + 8 a^2 b^2 + b^4) - 3 a (a^4 + 10 a^2 b^2 + 5 b^4) \text{Cos}[c + d x]) \text{Csc}[c + d x]^2 +}{(b (3 a^2 + b^2) - a (a^2 + 3 b^2) \text{Cos}[c + d x]) \text{Csc}[c + d x]^4} + \frac{3 a (a - 3 b) \text{Log}[1 - \text{Cos}[c + d x]]}{16 (a + b)^5 d} - \\
 & \frac{3 a (a + 3 b) \text{Log}[1 + \text{Cos}[c + d x]]}{16 (a - b)^5 d} + \frac{3 a^2 b (a^4 + 5 a^2 b^2 + 2 b^4) \text{Log}[b + a \text{Cos}[c + d x]]}{(a^2 - b^2)^5 d}
 \end{aligned}$$

Result (type 3, 780 leaves):

$$\begin{aligned}
& \frac{a^2 b^3 (b + a \cos [c + d x]) \sec [c + d x]^3}{2 (-a + b)^3 (a + b)^3 d (a + b \sec [c + d x])^3} + \\
& \frac{3 a^2 b^2 (-i a + b) (i a + b) (b + a \cos [c + d x])^2 \sec [c + d x]^3}{(-a + b)^4 (a + b)^4 d (a + b \sec [c + d x])^3} - \\
& \left(\frac{6 i (a^6 b + 5 a^4 b^3 + 2 a^2 b^5) (c + d x) (b + a \cos [c + d x])^3 \sec [c + d x]^3}{((a - b)^5 (a + b)^5 d (a + b \sec [c + d x])^3)} + \right. \\
& \left. \frac{3 i (-a^2 + 3 a b) \operatorname{ArcTan}[\tan [c + d x]] (b + a \cos [c + d x])^3 \sec [c + d x]^3}{(8 (a + b)^5 d (a + b \sec [c + d x])^3)} - \right. \\
& \left. \frac{3 i (a^2 + 3 a b) \operatorname{ArcTan}[\tan [c + d x]] (b + a \cos [c + d x])^3 \sec [c + d x]^3}{(8 (-a + b)^5 d (a + b \sec [c + d x])^3)} + \right. \\
& \left. \frac{3 (-a + b) (b + a \cos [c + d x])^3 \operatorname{Csc}\left[\frac{1}{2} (c + d x)\right]^2 \sec [c + d x]^3}{32 (a + b)^4 d (a + b \sec [c + d x])^3} - \right. \\
& \left. \frac{(b + a \cos [c + d x])^3 \operatorname{Csc}\left[\frac{1}{2} (c + d x)\right]^4 \sec [c + d x]^3}{64 (a + b)^3 d (a + b \sec [c + d x])^3} + \right. \\
& \left(\frac{3 (a^2 + 3 a b) (b + a \cos [c + d x])^3 \operatorname{Log}\left[\cos\left[\frac{1}{2} (c + d x)\right]^2\right] \sec [c + d x]^3}{(16 (-a + b)^5 d (a + b \sec [c + d x])^3)} - \right. \\
& \left. \frac{3 (a^6 b + 5 a^4 b^3 + 2 a^2 b^5) (b + a \cos [c + d x])^3 \operatorname{Log}[b + a \cos [c + d x]] \sec [c + d x]^3}{((-a^2 + b^2)^5 d (a + b \sec [c + d x])^3)} - \right. \\
& \left. \frac{3 (-a^2 + 3 a b) (b + a \cos [c + d x])^3 \operatorname{Log}\left[\sin\left[\frac{1}{2} (c + d x)\right]^2\right] \sec [c + d x]^3}{(16 (a + b)^5 d (a + b \sec [c + d x])^3)} + \right. \\
& \left. \frac{3 (a + b) (b + a \cos [c + d x])^3 \sec\left[\frac{1}{2} (c + d x)\right]^2 \sec [c + d x]^3}{32 (-a + b)^4 d (a + b \sec [c + d x])^3} - \right. \\
& \left. \frac{(b + a \cos [c + d x])^3 \sec\left[\frac{1}{2} (c + d x)\right]^4 \sec [c + d x]^3}{64 (-a + b)^3 d (a + b \sec [c + d x])^3} \right)
\end{aligned}$$

Problem 228: Result more than twice size of optimal antiderivative.

$$\int \frac{\sin [c + d x]^6}{(a + b \sec [c + d x])^3} dx$$

Optimal (type 3, 539 leaves, 11 steps):

$$\begin{aligned}
 & \frac{(5 a^6 - 180 a^4 b^2 + 600 a^2 b^4 - 448 b^6) x}{16 a^9} - \\
 & \frac{\sqrt{a-b} b \sqrt{a+b} (6 a^4 - 47 a^2 b^2 + 56 b^4) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a+b}}\right]}{a^9 d} + \\
 & \frac{b (213 a^4 - 985 a^2 b^2 + 840 b^4) \operatorname{Sin}[c+dx]}{30 a^8 d} - \frac{(43 a^4 - 244 a^2 b^2 + 224 b^4) \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{16 a^7 d} + \\
 & \frac{(45 a^4 - 291 a^2 b^2 + 280 b^4) \operatorname{Cos}[c+dx]^2 \operatorname{Sin}[c+dx]}{30 a^6 b d} - \\
 & \frac{(24 a^4 - 169 a^2 b^2 + 168 b^4) \operatorname{Cos}[c+dx]^3 \operatorname{Sin}[c+dx]}{24 a^5 b^2 d} - \\
 & \frac{\operatorname{Cos}[c+dx]^4 \operatorname{Sin}[c+dx]}{4 b d (b+a \operatorname{Cos}[c+dx])^2} + \frac{a \operatorname{Cos}[c+dx]^5 \operatorname{Sin}[c+dx]}{10 b^2 d (b+a \operatorname{Cos}[c+dx])^2} + \\
 & \frac{(9 a^4 - 60 a^2 b^2 + 56 b^4) \operatorname{Cos}[c+dx]^5 \operatorname{Sin}[c+dx]}{60 a^3 b^2 d (b+a \operatorname{Cos}[c+dx])^2} + \frac{4 b \operatorname{Cos}[c+dx]^6 \operatorname{Sin}[c+dx]}{15 a^2 d (b+a \operatorname{Cos}[c+dx])^2} - \\
 & \frac{\operatorname{Cos}[c+dx]^7 \operatorname{Sin}[c+dx]}{6 a d (b+a \operatorname{Cos}[c+dx])^2} + \frac{(15 a^4 - 110 a^2 b^2 + 112 b^4) \operatorname{Cos}[c+dx]^4 \operatorname{Sin}[c+dx]}{20 a^4 b^2 d (b+a \operatorname{Cos}[c+dx])}
 \end{aligned}$$

Result (type 3, 2091 leaves):

$$\begin{aligned}
 & - \left(\left((b+a \operatorname{Cos}[c+dx])^3 \operatorname{Sec}[c+dx]^3 \right. \right. \\
 & \left. \left. \left(8 (c+dx) + \frac{2 b (15 a^4 - 20 a^2 b^2 + 8 b^4) \operatorname{ArcTanh}\left[\frac{(-a+b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2-b^2}}\right]}{(a^2-b^2)^{5/2}} + \right. \right. \right. \\
 & \left. \left. \left. \frac{a b (3 a^2 - 4 b^2) \operatorname{Sin}[c+dx]}{(a-b)(a+b)(b+a \operatorname{Cos}[c+dx])^2} - \frac{3 a (2 a^4 - 7 a^2 b^2 + 4 b^4) \operatorname{Sin}[c+dx]}{(a-b)^2 (a+b)^2 (b+a \operatorname{Cos}[c+dx])} \right) \right) \right) / \\
 & \left(64 a^3 d (a+b \operatorname{Sec}[c+dx])^3 \right) + \left(3 (b+a \operatorname{Cos}[c+dx])^3 \operatorname{Sec}[c+dx]^3 \right. \\
 & \left. \left(\frac{6 a b \operatorname{ArcTanh}\left[\frac{(-a+b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2-b^2}}\right]}{\sqrt{a^2-b^2}} + \frac{(b(a^2+2b^2) + a(2a^2+b^2) \operatorname{Cos}[c+dx]) \operatorname{Sin}[c+dx]}{(b+a \operatorname{Cos}[c+dx])^2} \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \frac{(256 (a - b)^2 (a + b)^2 d (a + b \operatorname{Sec}[c + d x])^3) +}{1} \\
 & 1024 a^7 d (a + b \operatorname{Sec}[c + d x])^3 \\
 & 3 (b + a \operatorname{Cos}[c + d x])^3 \operatorname{Sec}[c + d x]^3 \\
 & \left(\frac{1}{(a^2 - b^2)^{5/2}} 12 b (105 a^8 - 840 a^6 b^2 + 2016 a^4 b^4 - 1920 a^2 b^6 + 640 b^8) \right. \\
 & \operatorname{ArcTanh} \left[\frac{(-a + b) \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right]}{\sqrt{a^2 - b^2}} \right] + \frac{1}{(a^2 - b^2)^2 (b + a \operatorname{Cos}[c + d x])^2} \\
 & \left. \left(48 a^{10} c - 960 a^8 b^2 c + 1776 a^6 b^4 c + 2976 a^4 b^6 c - 7680 a^2 b^8 c + 3840 b^{10} c + 48 a^{10} d x - \right. \right. \\
 & 960 a^8 b^2 d x + 1776 a^6 b^4 d x + 2976 a^4 b^6 d x - 7680 a^2 b^8 d x + 3840 b^{10} d x + 192 a b (a^2 - b^2)^2 \\
 & (a^4 - 20 a^2 b^2 + 40 b^4) (c + d x) \operatorname{Cos}[c + d x] + 48 (a^3 - a b^2)^2 (a^4 - 20 a^2 b^2 + 40 b^4) (c + d x) \\
 & \operatorname{Cos}[2 (c + d x)] + 114 a^9 b \operatorname{Sin}[c + d x] + 788 a^7 b^3 \operatorname{Sin}[c + d x] - 5696 a^5 b^5 \operatorname{Sin}[c + d x] + \\
 & 8640 a^3 b^7 \operatorname{Sin}[c + d x] - 3840 a b^9 \operatorname{Sin}[c + d x] - 36 a^{10} \operatorname{Sin}[2 (c + d x)] + \\
 & 1221 a^8 b^2 \operatorname{Sin}[2 (c + d x)] - 5182 a^6 b^4 \operatorname{Sin}[2 (c + d x)] + 6880 a^4 b^6 \operatorname{Sin}[2 (c + d x)] - \\
 & 2880 a^2 b^8 \operatorname{Sin}[2 (c + d x)] + 120 a^9 b \operatorname{Sin}[3 (c + d x)] - 560 a^7 b^3 \operatorname{Sin}[3 (c + d x)] + \\
 & 760 a^5 b^5 \operatorname{Sin}[3 (c + d x)] - 320 a^3 b^7 \operatorname{Sin}[3 (c + d x)] - 8 a^{10} \operatorname{Sin}[4 (c + d x)] + \\
 & 56 a^8 b^2 \operatorname{Sin}[4 (c + d x)] - 88 a^6 b^4 \operatorname{Sin}[4 (c + d x)] + 40 a^4 b^6 \operatorname{Sin}[4 (c + d x)] - \\
 & 8 a^9 b \operatorname{Sin}[5 (c + d x)] + 16 a^7 b^3 \operatorname{Sin}[5 (c + d x)] - 8 a^5 b^5 \operatorname{Sin}[5 (c + d x)] + \\
 & \left. \left. 2 a^{10} \operatorname{Sin}[6 (c + d x)] - 4 a^8 b^2 \operatorname{Sin}[6 (c + d x)] + 2 a^6 b^4 \operatorname{Sin}[6 (c + d x)] \right) \right) + \\
 & \frac{1}{256 (a + b \operatorname{Sec}[c + d x])^3} (b + a \operatorname{Cos}[c + d x])^3 \operatorname{Sec}[c + d x]^3 \\
 & \left(- \left(\left(b (-693 a^{10} + 9240 a^8 b^2 - 36960 a^6 b^4 + 63360 a^4 b^6 - 49280 a^2 b^8 + 14336 b^{10}) \right. \right. \right. \\
 & \left. \left. \operatorname{ArcTanh} \left[\frac{(-a + b) \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right]}{\sqrt{a^2 - b^2}} \right] \right) / \left(a^9 \sqrt{a^2 - b^2} (-a^2 + b^2)^2 d \right) \right) - \\
 & \frac{1}{60 a^9 (a^2 - b^2)^2 d (b + a \operatorname{Cos}[c + d x])^2} (-1200 a^{12} (c + d x) + 43200 a^{10} b^2 (c + d x) - \\
 & 198000 a^8 b^4 (c + d x) + 83040 a^6 b^6 (c + d x) + 691200 a^4 b^8 (c + d x) - \\
 & 1048320 a^2 b^{10} (c + d x) + 430080 b^{12} (c + d x) - 4800 a^{11} b (c + d x) \operatorname{Cos}[c + d x] + \\
 & 182400 a^9 b^3 (c + d x) \operatorname{Cos}[c + d x] - 1156800 a^7 b^5 (c + d x) \operatorname{Cos}[c + d x] + \\
 & 2645760 a^5 b^7 (c + d x) \operatorname{Cos}[c + d x] - 2526720 a^3 b^9 (c + d x) \operatorname{Cos}[c + d x] + \\
 & 860160 a b^{11} (c + d x) \operatorname{Cos}[c + d x] - 1200 a^{12} (c + d x) \operatorname{Cos}[2 (c + d x)] + \\
 & 45600 a^{10} b^2 (c + d x) \operatorname{Cos}[2 (c + d x)] - 289200 a^8 b^4 (c + d x) \operatorname{Cos}[2 (c + d x)] + \\
 & 661440 a^6 b^6 (c + d x) \operatorname{Cos}[2 (c + d x)] - 631680 a^4 b^8 (c + d x) \operatorname{Cos}[2 (c + d x)] + \\
 & 215040 a^2 b^{10} (c + d x) \operatorname{Cos}[2 (c + d x)] - 4530 a^{11} b \operatorname{Sin}[c + d x] - \\
 & 11060 a^9 b^3 \operatorname{Sin}[c + d x] + 332800 a^7 b^5 \operatorname{Sin}[c + d x] - 1042880 a^5 b^7 \operatorname{Sin}[c + d x] + \\
 & 1155840 a^3 b^9 \operatorname{Sin}[c + d x] - 430080 a b^{11} \operatorname{Sin}[c + d x] + 900 a^{12} \operatorname{Sin}[2 (c + d x)] - \\
 & 49125 a^{10} b^2 \operatorname{Sin}[2 (c + d x)] + 362830 a^8 b^4 \operatorname{Sin}[2 (c + d x)] - 903680 a^6 b^6 \operatorname{Sin}[2 (c + d x)] + \\
 & 911680 a^4 b^8 \operatorname{Sin}[2 (c + d x)] - 322560 a^2 b^{10} \operatorname{Sin}[2 (c + d x)] -
 \end{aligned}$$

$$\begin{aligned}
 & 4344 a^{11} b \sin[3(c+dx)] + 37808 a^9 b^3 \sin[3(c+dx)] - 98424 a^7 b^5 \sin[3(c+dx)] + \\
 & 100800 a^5 b^7 \sin[3(c+dx)] - 35840 a^3 b^9 \sin[3(c+dx)] + 200 a^{12} \sin[4(c+dx)] - \\
 & 3256 a^{10} b^2 \sin[4(c+dx)] + 10392 a^8 b^4 \sin[4(c+dx)] - 11816 a^6 b^6 \sin[4(c+dx)] + \\
 & 4480 a^4 b^8 \sin[4(c+dx)] + 392 a^{11} b \sin[5(c+dx)] - 1680 a^9 b^3 \sin[5(c+dx)] + \\
 & 2184 a^7 b^5 \sin[5(c+dx)] - 896 a^5 b^7 \sin[5(c+dx)] - 50 a^{12} \sin[6(c+dx)] + \\
 & 324 a^{10} b^2 \sin[6(c+dx)] - 498 a^8 b^4 \sin[6(c+dx)] + 224 a^6 b^6 \sin[6(c+dx)] - \\
 & 64 a^{11} b \sin[7(c+dx)] + 128 a^9 b^3 \sin[7(c+dx)] - 64 a^7 b^5 \sin[7(c+dx)] + \\
 & \left. 20 a^{12} \sin[8(c+dx)] - 40 a^{10} b^2 \sin[8(c+dx)] + 20 a^8 b^4 \sin[8(c+dx)] \right)
 \end{aligned}$$

Problem 229: Result more than twice size of optimal antiderivative.

$$\int \frac{\sin[c+dx]^4}{(a+b \sec[c+dx])^3} dx$$

Optimal (type 3, 333 leaves, 9 steps):

$$\begin{aligned}
 & \frac{3(a^4 - 24a^2b^2 + 40b^4)x}{8a^7} - \frac{3b(2a^4 - 11a^2b^2 + 10b^4) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a+b}}\right]}{a^7 \sqrt{a-b} \sqrt{a+b} d} + \\
 & \frac{b(13a^2 - 30b^2) \sin[c+dx]}{2a^6 d} - \frac{3(7a^2 - 20b^2) \cos[c+dx] \sin[c+dx]}{8a^5 d} + \\
 & \frac{(3a^2 - 10b^2) \cos[c+dx]^2 \sin[c+dx]}{2a^4 b d} - \frac{(4a^2 - 15b^2) \cos[c+dx]^3 \sin[c+dx]}{4a^3 b^2 d} - \\
 & \frac{(a^2 - b^2) \cos[c+dx]^4 \sin[c+dx]}{2a^2 b d (b + a \cos[c+dx])^2} + \frac{(2a^2 - 7b^2) \cos[c+dx]^4 \sin[c+dx]}{2a^2 b^2 d (b + a \cos[c+dx])}
 \end{aligned}$$

Result (type 3, 1320 leaves):

$$\begin{aligned}
 & - \left(\left(3(b + a \cos[c+dx])^3 \sec[c+dx]^3 \right. \right. \\
 & \left. \left(8(c+dx) + \frac{2b(15a^4 - 20a^2b^2 + 8b^4) \operatorname{ArcTanh}\left[\frac{(-a+b) \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2-b^2}}\right]}{(a^2 - b^2)^{5/2}} + \right. \right. \\
 & \left. \left. \frac{ab(3a^2 - 4b^2) \sin[c+dx]}{(a-b)(a+b)(b + a \cos[c+dx])^2} - \frac{3a(2a^4 - 7a^2b^2 + 4b^4) \sin[c+dx]}{(a-b)^2(a+b)^2(b + a \cos[c+dx])} \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
& \left. \left(128 a^3 d (a + b \operatorname{Sec}[c + d x])^3 \right) + \left(3 (b + a \operatorname{Cos}[c + d x])^3 \operatorname{Sec}[c + d x]^3 \right. \right. \\
& \left. \left. \frac{6 a b \operatorname{ArcTanh}\left[\frac{(-a+b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{\sqrt{a^2-b^2}} + \frac{(b(a^2+2b^2) + a(2a^2+b^2) \operatorname{Cos}[c+d x]) \operatorname{Sin}[c+d x]}{(b+a \operatorname{Cos}[c+d x])^2} \right) \right) / \\
& \left(128 (a-b)^2 (a+b)^2 d (a+b \operatorname{Sec}[c+d x])^3 \right) - \\
& \left((b+a \operatorname{Cos}[c+d x])^3 \operatorname{Sec}[c+d x]^3 \left(-24 (a^2-8b^2)(c+d x) + \frac{1}{(a^2-b^2)^{5/2}} \right. \right. \\
& \left. \left. 6 b (-35 a^6 + 140 a^4 b^2 - 168 a^2 b^4 + 64 b^6) \operatorname{ArcTanh}\left[\frac{(-a+b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right] - \right. \right. \\
& \left. \left. 96 a b \operatorname{Sin}[c+d x] + \frac{a b (-5 a^4 + 20 a^2 b^2 - 16 b^4) \operatorname{Sin}[c+d x]}{(a-b)(a+b)(b+a \operatorname{Cos}[c+d x])^2} + \right. \right. \\
& \left. \left. \frac{a(10 a^6 - 115 a^4 b^2 + 220 a^2 b^4 - 112 b^6) \operatorname{Sin}[c+d x]}{(a-b)^2 (a+b)^2 (b+a \operatorname{Cos}[c+d x])} + 8 a^2 \operatorname{Sin}[2(c+d x)] \right) \right) / \\
& \left(128 a^5 d (a+b \operatorname{Sec}[c+d x])^3 \right) + \frac{1}{256 a^7 d (a+b \operatorname{Sec}[c+d x])^3} \\
& (b+a \operatorname{Cos}[c+d x])^3 \operatorname{Sec}[c+d x]^3 \\
& \left(\frac{1}{(a^2-b^2)^{5/2}} 12 b (105 a^8 - 840 a^6 b^2 + 2016 a^4 b^4 - 1920 a^2 b^6 + 640 b^8) \right. \\
& \left. \operatorname{ArcTanh}\left[\frac{(-a+b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right] + \frac{1}{(a^2-b^2)^2 (b+a \operatorname{Cos}[c+d x])^2} \right. \\
& \left. \left(48 a^{10} c - 960 a^8 b^2 c + 1776 a^6 b^4 c + 2976 a^4 b^6 c - 7680 a^2 b^8 c + 3840 b^{10} c + 48 a^{10} d x - \right. \right. \\
& \left. \left. 960 a^8 b^2 d x + 1776 a^6 b^4 d x + 2976 a^4 b^6 d x - 7680 a^2 b^8 d x + 3840 b^{10} d x + 192 a b (a^2 - b^2)^2 \right. \right. \\
& \left. \left. (a^4 - 20 a^2 b^2 + 40 b^4) (c+d x) \operatorname{Cos}[c+d x] + 48 (a^3 - a b^2)^2 (a^4 - 20 a^2 b^2 + 40 b^4) (c+d x) \right. \right. \\
& \left. \left. \operatorname{Cos}[2(c+d x)] + 114 a^9 b \operatorname{Sin}[c+d x] + 788 a^7 b^3 \operatorname{Sin}[c+d x] - 5696 a^5 b^5 \operatorname{Sin}[c+d x] + \right. \right. \\
& \left. \left. 8640 a^3 b^7 \operatorname{Sin}[c+d x] - 3840 a b^9 \operatorname{Sin}[c+d x] - 36 a^{10} \operatorname{Sin}[2(c+d x)] + \right. \right. \\
& \left. \left. 1221 a^8 b^2 \operatorname{Sin}[2(c+d x)] - 5182 a^6 b^4 \operatorname{Sin}[2(c+d x)] + 6880 a^4 b^6 \operatorname{Sin}[2(c+d x)] - \right. \right. \\
& \left. \left. 2880 a^2 b^8 \operatorname{Sin}[2(c+d x)] + 120 a^9 b \operatorname{Sin}[3(c+d x)] - 560 a^7 b^3 \operatorname{Sin}[3(c+d x)] + \right. \right. \\
& \left. \left. 760 a^5 b^5 \operatorname{Sin}[3(c+d x)] - 320 a^3 b^7 \operatorname{Sin}[3(c+d x)] - 8 a^{10} \operatorname{Sin}[4(c+d x)] + \right. \right. \\
& \left. \left. 56 a^8 b^2 \operatorname{Sin}[4(c+d x)] - 88 a^6 b^4 \operatorname{Sin}[4(c+d x)] + 40 a^4 b^6 \operatorname{Sin}[4(c+d x)] - \right. \right. \\
& \left. \left. 8 a^9 b \operatorname{Sin}[5(c+d x)] + 16 a^7 b^3 \operatorname{Sin}[5(c+d x)] - 8 a^5 b^5 \operatorname{Sin}[5(c+d x)] + \right. \right. \\
& \left. \left. 2 a^{10} \operatorname{Sin}[6(c+d x)] - 4 a^8 b^2 \operatorname{Sin}[6(c+d x)] + 2 a^6 b^4 \operatorname{Sin}[6(c+d x)] \right) \right)
\end{aligned}$$

Problem 233: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \sin [c + d x])^{7/2}}{a + b \sec [c + d x]} dx$$

Optimal (type 4, 516 leaves, 15 steps):

$$\begin{aligned} & \frac{b (a^2 - b^2)^{5/4} e^{7/2} \operatorname{ArcTan} \left[\frac{\sqrt{a} \sqrt{e \sin [c + d x]}}{(a^2 - b^2)^{1/4} \sqrt{e}} \right]}{a^{9/2} d} - \frac{b (a^2 - b^2)^{5/4} e^{7/2} \operatorname{ArcTanh} \left[\frac{\sqrt{a} \sqrt{e \sin [c + d x]}}{(a^2 - b^2)^{1/4} \sqrt{e}} \right]}{a^{9/2} d} + \\ & \left(2 (5 a^4 - 28 a^2 b^2 + 21 b^4) e^4 \operatorname{EllipticF} \left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x \right), 2 \right] \sqrt{\sin [c + d x]} \right) / \\ & \left(21 a^5 d \sqrt{e \sin [c + d x]} \right) + \\ & \left(b^2 (a^2 - b^2)^2 e^4 \operatorname{EllipticPi} \left[\frac{2 a}{a - \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + d x \right), 2 \right] \sqrt{\sin [c + d x]} \right) / \\ & \left(a^5 (a^2 - b^2 - a \sqrt{a^2 - b^2}) d \sqrt{e \sin [c + d x]} \right) + \\ & \left(b^2 (a^2 - b^2)^2 e^4 \operatorname{EllipticPi} \left[\frac{2 a}{a + \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + d x \right), 2 \right] \sqrt{\sin [c + d x]} \right) / \\ & \left(a^5 (a^2 - b^2 + a \sqrt{a^2 - b^2}) d \sqrt{e \sin [c + d x]} \right) + \\ & \frac{2 e^3 (21 b (a^2 - b^2) - a (5 a^2 - 7 b^2) \cos [c + d x]) \sqrt{e \sin [c + d x]}}{21 a^4 d} + \\ & \frac{2 e (7 b - 5 a \cos [c + d x]) (e \sin [c + d x])^{5/2}}{35 a^2 d} \end{aligned}$$

Result (type 6, 2249 leaves):

$$\begin{aligned} & \left((b + a \cos [c + d x]) \left(-\frac{(23 a^2 - 28 b^2) \cos [c + d x]}{42 a^3} - \frac{b \cos [2 (c + d x)]}{5 a^2} + \frac{\cos [3 (c + d x)]}{14 a} \right) \right) \\ & \operatorname{Csc} [c + d x]^3 \operatorname{Sec} [c + d x] (e \sin [c + d x])^{7/2} \Big/ (d (a + b \sec [c + d x])) - \\ & \frac{1}{420 a^3 d (a + b \sec [c + d x]) \sin [c + d x]^{7/2}} (b + a \cos [c + d x]) \operatorname{Sec} [c + d x] \\ & (e \sin [c + d x])^{7/2} \left(\frac{1}{(b + a \cos [c + d x]) (1 - \sin [c + d x]^2)} \right) \\ & 2 (-100 a^3 + 98 a b^2) \cos [c + d x]^2 \left(b + a \sqrt{1 - \sin [c + d x]^2} \right) \\ & \left(\left(b \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{a} \sqrt{\sin [c + d x]}}{(-a^2 + b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{a} \sqrt{\sin [c + d x]}}{(-a^2 + b^2)^{1/4}} \right] \right) - \right. \end{aligned}$$

$$\begin{aligned}
 & \left. \left(\begin{aligned}
 & \text{Log} \left[\sqrt{-a^2 + b^2} - \sqrt{2} \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\text{Sin}[c + dx]} + a \text{Sin}[c + dx] \right] + \right. \\
 & \left. \text{Log} \left[\sqrt{-a^2 + b^2} + \sqrt{2} \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\text{Sin}[c + dx]} + a \text{Sin}[c + dx] \right] \right) \right) / \\
 & \left(4 \sqrt{2} \sqrt{a} (-a^2 + b^2)^{3/4} \right) - \left(5 a (a^2 - b^2) \text{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \right. \right. \\
 & \left. \left. \text{Sin}[c + dx]^2, \frac{a^2 \text{Sin}[c + dx]^2}{a^2 - b^2} \right] \sqrt{\text{Sin}[c + dx]} \sqrt{1 - \text{Sin}[c + dx]^2} \right) / \\
 & \left(\left(5 (a^2 - b^2) \text{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \text{Sin}[c + dx]^2, \frac{a^2 \text{Sin}[c + dx]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \left. \left. 2 \left(2 a^2 \text{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \text{Sin}[c + dx]^2, \frac{a^2 \text{Sin}[c + dx]^2}{a^2 - b^2} \right] + (-a^2 + b^2) \right. \right. \right. \\
 & \left. \left. \left. \text{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \text{Sin}[c + dx]^2, \frac{a^2 \text{Sin}[c + dx]^2}{a^2 - b^2} \right] \right) \text{Sin}[c + dx]^2 \right) \right) \\
 & \left. \left. \left. (b^2 + a^2 (-1 + \text{Sin}[c + dx]^2)) \right) \right) \right) + \frac{1}{(b + a \text{Cos}[c + dx]) \sqrt{1 - \text{Sin}[c + dx]^2}} \\
 & 2 (89 a^2 b - 70 b^3) \text{Cos}[c + dx] \left(b + a \sqrt{1 - \text{Sin}[c + dx]^2} \right) \left(-\frac{1}{(a^2 - b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{a} \right. \\
 & \left. \left(2 \text{ArcTan} \left[1 - \frac{(1 + i) \sqrt{a} \sqrt{\text{Sin}[c + dx]}}{(a^2 - b^2)^{1/4}} \right] - 2 \text{ArcTan} \left[1 + \frac{(1 + i) \sqrt{a} \sqrt{\text{Sin}[c + dx]}}{(a^2 - b^2)^{1/4}} \right] \right) + \right. \\
 & \left. \text{Log} \left[\sqrt{a^2 - b^2} - (1 + i) \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\text{Sin}[c + dx]} + i a \text{Sin}[c + dx] \right] - \right. \\
 & \left. \text{Log} \left[\sqrt{a^2 - b^2} + (1 + i) \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\text{Sin}[c + dx]} + i a \text{Sin}[c + dx] \right] \right) + \\
 & \left(5 b (a^2 - b^2) \text{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \text{Sin}[c + dx]^2, \frac{a^2 \text{Sin}[c + dx]^2}{a^2 - b^2} \right] \sqrt{\text{Sin}[c + dx]} \right) / \\
 & \left(\sqrt{1 - \text{Sin}[c + dx]^2} \left(5 (a^2 - b^2) \text{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \text{Sin}[c + dx]^2, \right. \right. \right. \\
 & \left. \left. \frac{a^2 \text{Sin}[c + dx]^2}{a^2 - b^2} \right] + 2 \left(2 a^2 \text{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \text{Sin}[c + dx]^2, \right. \right. \right. \\
 & \left. \left. \frac{a^2 \text{Sin}[c + dx]^2}{a^2 - b^2} \right] + (a^2 - b^2) \text{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \text{Sin}[c + dx]^2, \right. \right. \\
 & \left. \left. \frac{a^2 \text{Sin}[c + dx]^2}{a^2 - b^2} \right] \right) \text{Sin}[c + dx]^2 \right) (b^2 + a^2 (-1 + \text{Sin}[c + dx]^2)) \right) \right) + \\
 & \frac{1}{(b + a \text{Cos}[c + dx]) (1 - 2 \text{Sin}[c + dx]^2) \sqrt{1 - \text{Sin}[c + dx]^2}} (-231 a^2 b + 210 b^3) \\
 & \text{Cos}[c + dx] \text{Cos}[2(c + dx)] \\
 & \left(b + a \sqrt{1 - \text{Sin}[c + dx]^2} \right)
 \end{aligned}$$

$$\left(\frac{\left(\frac{1}{2} - \frac{i}{2}\right) (a^2 - 2b^2) \operatorname{ArcTan}\left[1 - \frac{(1+i)\sqrt{a}\sqrt{\sin[c+dx]}}{(a^2-b^2)^{1/4}}\right]}{a^{3/2} (a^2 - b^2)^{3/4}} - \frac{\left(\frac{1}{2} - \frac{i}{2}\right) (a^2 - 2b^2) \operatorname{ArcTan}\left[1 + \frac{(1+i)\sqrt{a}\sqrt{\sin[c+dx]}}{(a^2-b^2)^{1/4}}\right]}{a^{3/2} (a^2 - b^2)^{3/4}} + \left(\frac{1}{4} - \frac{i}{4}\right) (a^2 - 2b^2) \operatorname{Log}\left[\sqrt{a^2 - b^2} - (1+i)\sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\sin[c+dx]} + i a \sin[c+dx]\right]}{a^{3/2} (a^2 - b^2)^{3/4}} - \left(\frac{1}{4} - \frac{i}{4}\right) (a^2 - 2b^2) \operatorname{Log}\left[\sqrt{a^2 - b^2} + (1+i)\sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\sin[c+dx]} + i a \sin[c+dx]\right]}{a^{3/2} (a^2 - b^2)^{3/4}} + \frac{4\sqrt{\sin[c+dx]}}{a} + \left(10b (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2 - b^2}\right] \sqrt{\sin[c+dx]}\right) / \left(\sqrt{1 - \sin[c+dx]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2 - b^2}\right] + 2 \left(2 a^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2 - b^2}\right] + (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2 - b^2}\right]\right) \sin[c+dx]^2\right) (b^2 + a^2 (-1 + \sin[c+dx]^2))\right) + \left(36b (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2 - b^2}\right] \sin[c+dx]^{5/2}\right) / \left(5 \sqrt{1 - \sin[c+dx]^2} \left(9 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2 - b^2}\right] + 2 \left(2 a^2 \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2 - b^2}\right] + (a^2 - b^2) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2 - b^2}\right]\right) \sin[c+dx]^2\right) (b^2 + a^2 (-1 + \sin[c+dx]^2))\right) \right)$$

Problem 234: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \sin[c+dx])^{5/2}}{a+b \sec[c+dx]} dx$$

Optimal (type 4, 430 leaves, 14 steps):

$$\frac{b (a^2 - b^2)^{3/4} e^{5/2} \text{ArcTan}\left[\frac{\sqrt{a} \sqrt{e \text{Sin}[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{a^{7/2} d} - \frac{b (a^2 - b^2)^{3/4} e^{5/2} \text{ArcTanh}\left[\frac{\sqrt{a} \sqrt{e \text{Sin}[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{a^{7/2} d} -$$

$$\left(\frac{b^2 (a^2 - b^2) e^3 \text{EllipticPi}\left[\frac{2a}{a - \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\text{Sin}[c+dx]}}{\left(a^4 \left(a - \sqrt{a^2 - b^2}\right) d \sqrt{e \text{Sin}[c+dx]}\right)} - \right.$$

$$\left. \frac{b^2 (a^2 - b^2) e^3 \text{EllipticPi}\left[\frac{2a}{a + \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\text{Sin}[c+dx]}}{\left(a^4 \left(a + \sqrt{a^2 - b^2}\right) d \sqrt{e \text{Sin}[c+dx]}\right)} \right) /$$

$$\frac{2 (3 a^2 - 5 b^2) e^2 \text{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{e \text{Sin}[c+dx]}}{5 a^3 d \sqrt{\text{Sin}[c+dx]}} +$$

$$\frac{2 e (5 b - 3 a \text{Cos}[c+dx]) (e \text{Sin}[c+dx])^{3/2}}{15 a^2 d}$$

Result (type 6, 1247 leaves):

$$-\frac{1}{5 a^2 d (a + b \text{Sec}[c+dx]) \text{Sin}[c+dx]^{5/2}} (b + a \text{Cos}[c+dx]) \text{Sec}[c+dx] (e \text{Sin}[c+dx])^{5/2}$$

$$\left(\frac{1}{(b + a \text{Cos}[c+dx]) (1 - \text{Sin}[c+dx]^2)} 2 (-3 a^2 + 5 b^2) \text{Cos}[c+dx]^2 \left(b + a \sqrt{1 - \text{Sin}[c+dx]^2}\right) \right.$$

$$\left(\left(b \left(-2 \text{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{a} \sqrt{\text{Sin}[c+dx]}}{(-a^2 + b^2)^{1/4}}\right] + 2 \text{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{a} \sqrt{\text{Sin}[c+dx]}}{(-a^2 + b^2)^{1/4}}\right] + \text{Log}\left[\frac{\sqrt{-a^2 + b^2} - \sqrt{2} \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\text{Sin}[c+dx]} + a \text{Sin}[c+dx]}{\sqrt{-a^2 + b^2} + \sqrt{2} \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\text{Sin}[c+dx]} + a \text{Sin}[c+dx]}\right] \right) \right) /$$

$$\left(4 \sqrt{2} a^{3/2} (-a^2 + b^2)^{1/4} - \left(7 a (a^2 - b^2) \text{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \text{Sin}[c+dx]^2, \frac{a^2 \text{Sin}[c+dx]^2}{a^2 - b^2}\right] \text{Sin}[c+dx]^{3/2} \sqrt{1 - \text{Sin}[c+dx]^2} \right) \right) /$$

$$\left(3 \left(7 (a^2 - b^2) \text{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \text{Sin}[c+dx]^2, \frac{a^2 \text{Sin}[c+dx]^2}{a^2 - b^2}\right] + 2 \left(2 a^2 \text{AppellF1}\left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \text{Sin}[c+dx]^2, \frac{a^2 \text{Sin}[c+dx]^2}{a^2 - b^2}\right] + \right. \right.$$

$$\left. \left. (-a^2 + b^2) \text{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \text{Sin}[c+dx]^2, \frac{a^2 \text{Sin}[c+dx]^2}{a^2 - b^2}\right] \right) \text{Sin}[c+dx]^2 \right) (b^2 + a^2 (-1 + \text{Sin}[c+dx]^2)) \right) \left. \right) +$$

$$\frac{1}{6 (b + a \text{Cos}[c+dx]) \sqrt{1 - \text{Sin}[c+dx]^2}} a b \text{Cos}[c+dx] \left(b + a \sqrt{1 - \text{Sin}[c+dx]^2}\right)$$

$$\begin{aligned}
 & \left(\left((3 + 3i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{a} \sqrt{\sin[c+dx]}}{(a^2 - b^2)^{1/4}} \right] - 2 \right. \right. \right. \\
 & \quad \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{a} \sqrt{\sin[c+dx]}}{(a^2 - b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{a^2 - b^2} - (1+i) \sqrt{a} \right. \\
 & \quad \left. \left. \left. (a^2 - b^2)^{1/4} \sqrt{\sin[c+dx]} + i a \sin[c+dx] \right] + \operatorname{Log} \left[\sqrt{a^2 - b^2} + (1+i) \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\sin[c+dx]} + i a \sin[c+dx] \right] \right) \right) / \left(\sqrt{a} (a^2 - b^2)^{1/4} \right) + \\
 & \left(56 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2 - b^2} \right] \sin[c+dx]^{3/2} \right) / \\
 & \left(\sqrt{1 - \sin[c+dx]^2} \left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \sin[c+dx]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{a^2 \sin[c+dx]^2}{a^2 - b^2} \right] + 2 \left(2 a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \sin[c+dx]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{a^2 \sin[c+dx]^2}{a^2 - b^2} \right] + (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \sin[c+dx]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{a^2 \sin[c+dx]^2}{a^2 - b^2} \right] \right) \sin[c+dx]^2 \right) (b^2 + a^2 (-1 + \sin[c+dx]^2)) \right) \right) + \\
 & \left((b + a \cos[c+dx]) \operatorname{Csc}[c+dx]^2 \operatorname{Sec}[c+dx] (e \sin[c+dx])^{5/2} \right. \\
 & \quad \left(\frac{2 b \sin[c+dx]}{3 a^2} - \right. \\
 & \quad \left. \left. \frac{\sin[2(c+dx)]}{5 a} \right) \right) / (d (a + \\
 & \quad b \\
 & \quad \operatorname{Sec}[c+dx]))
 \end{aligned}$$

Problem 235: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \sin[c+dx])^{3/2}}{a + b \operatorname{Sec}[c+dx]} dx$$

Optimal (type 4, 444 leaves, 14 steps):

$$\begin{aligned}
 & - \frac{b (a^2 - b^2)^{1/4} e^{3/2} \text{ArcTan} \left[\frac{\sqrt{a} \sqrt{e \text{Sin}[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}} \right]}{a^{5/2} d} - \frac{b (a^2 - b^2)^{1/4} e^{3/2} \text{ArcTanh} \left[\frac{\sqrt{a} \sqrt{e \text{Sin}[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}} \right]}{a^{5/2} d} + \\
 & \frac{2 (a^2 - 3 b^2) e^2 \text{EllipticF} \left[\frac{1}{2} \left(c - \frac{\pi}{2} + dx \right), 2 \right] \sqrt{\text{Sin}[c+dx]}}{3 a^3 d \sqrt{e \text{Sin}[c+dx]}} + \\
 & \left(b^2 (a^2 - b^2) e^2 \text{EllipticPi} \left[\frac{2 a}{a - \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + dx \right), 2 \right] \sqrt{\text{Sin}[c+dx]} \right) / \\
 & \left(a^3 \left(a^2 - b^2 - a \sqrt{a^2 - b^2} \right) d \sqrt{e \text{Sin}[c+dx]} \right) + \\
 & \left(b^2 (a^2 - b^2) e^2 \text{EllipticPi} \left[\frac{2 a}{a + \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + dx \right), 2 \right] \sqrt{\text{Sin}[c+dx]} \right) / \\
 & \left(a^3 \left(a^2 - b^2 + a \sqrt{a^2 - b^2} \right) d \sqrt{e \text{Sin}[c+dx]} \right) + \frac{2 e (3 b - a \text{Cos}[c+dx]) \sqrt{e \text{Sin}[c+dx]}}{3 a^2 d}
 \end{aligned}$$

Result (type 6, 2159 leaves):

$$\begin{aligned}
 & - \frac{2 (b + a \text{Cos}[c+dx]) \text{Csc}[c+dx] (e \text{Sin}[c+dx])^{3/2}}{3 a d (a + b \text{Sec}[c+dx])} + \\
 & \frac{1}{6 a d (a + b \text{Sec}[c+dx]) \text{Sin}[c+dx]^{3/2}} (b + a \text{Cos}[c+dx]) \text{Sec}[c+dx] (e \text{Sin}[c+dx])^{3/2} \\
 & \left(\frac{1}{(b + a \text{Cos}[c+dx]) (1 - \text{Sin}[c+dx])^2} 4 a \text{Cos}[c+dx]^2 (b + a \sqrt{1 - \text{Sin}[c+dx]^2}) \right. \\
 & \left. \left(\left(b \left(-2 \text{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{a} \sqrt{\text{Sin}[c+dx]}}{(-a^2 + b^2)^{1/4}} \right] + 2 \text{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{a} \sqrt{\text{Sin}[c+dx]}}{(-a^2 + b^2)^{1/4}} \right] \right) - \right. \right. \\
 & \quad \left. \left. \text{Log} \left[\sqrt{-a^2 + b^2} - \sqrt{2} \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\text{Sin}[c+dx]} + a \text{Sin}[c+dx] \right] + \right. \right. \\
 & \quad \left. \left. \text{Log} \left[\sqrt{-a^2 + b^2} + \sqrt{2} \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\text{Sin}[c+dx]} + a \text{Sin}[c+dx] \right] \right) \right) / \\
 & \left(4 \sqrt{2} \sqrt{a} (-a^2 + b^2)^{3/4} \right) - \left(5 a (a^2 - b^2) \text{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \right. \right. \\
 & \quad \left. \left. \text{Sin}[c+dx]^2, \frac{a^2 \text{Sin}[c+dx]^2}{a^2 - b^2} \right] \sqrt{\text{Sin}[c+dx]} \sqrt{1 - \text{Sin}[c+dx]^2} \right) / \\
 & \left(\left(5 (a^2 - b^2) \text{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \text{Sin}[c+dx]^2, \frac{a^2 \text{Sin}[c+dx]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \quad \left. \left. 2 \left(2 a^2 \text{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \text{Sin}[c+dx]^2, \frac{a^2 \text{Sin}[c+dx]^2}{a^2 - b^2} \right] + (-a^2 + b^2) \right. \right. \right. \\
 & \quad \left. \left. \left. \text{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \text{Sin}[c+dx]^2, \frac{a^2 \text{Sin}[c+dx]^2}{a^2 - b^2} \right] \right) \text{Sin}[c+dx]^2 \right) \right) \\
 & \left. \left. \left. \left(b^2 + a^2 (-1 + \text{Sin}[c+dx]^2) \right) \right) \right) - \frac{1}{(b + a \text{Cos}[c+dx]) \sqrt{1 - \text{Sin}[c+dx]^2}}
 \end{aligned}$$

$$\begin{aligned}
 & 2 b \cos [c+d x] \left(b+a \sqrt{1-\sin [c+d x]^2} \right) \left(-\frac{1}{\left(a^2-b^2\right)^{3 / 4}}\left(\frac{1}{8}-\frac{i}{8}\right) \sqrt{a} \right. \\
 & \left. \left(2 \operatorname{ArcTan}\left[1-\frac{(1+i) \sqrt{a} \sqrt{\sin [c+d x]}}{\left(a^2-b^2\right)^{1 / 4}}\right]-2 \operatorname{ArcTan}\left[1+\frac{(1+i) \sqrt{a} \sqrt{\sin [c+d x]}}{\left(a^2-b^2\right)^{1 / 4}}\right] \right)+\right. \\
 & \left. \operatorname{Log}\left[\sqrt{a^2-b^2}-(1+i) \sqrt{a}\left(a^2-b^2\right)^{1 / 4} \sqrt{\sin [c+d x]}+i a \sin [c+d x]\right]-\right. \\
 & \left. \operatorname{Log}\left[\sqrt{a^2-b^2}+(1+i) \sqrt{a}\left(a^2-b^2\right)^{1 / 4} \sqrt{\sin [c+d x]}+i a \sin [c+d x]\right] \right)+ \\
 & \left(5 b\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \sin [c+d x]^2, \frac{a^2 \sin [c+d x]^2}{a^2-b^2}\right] \sqrt{\sin [c+d x]} \right) / \\
 & \left(\sqrt{1-\sin [c+d x]^2} \left(5\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \sin [c+d x]^2, \right. \right. \right. \\
 & \left. \left. \frac{a^2 \sin [c+d x]^2}{a^2-b^2}\right]+2\left(2 a^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \sin [c+d x]^2, \right. \right. \right. \\
 & \left. \left. \frac{a^2 \sin [c+d x]^2}{a^2-b^2}\right]+\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \sin [c+d x]^2, \right. \right. \\
 & \left. \left. \frac{a^2 \sin [c+d x]^2}{a^2-b^2}\right] \right) \sin [c+d x]^2\left(b^2+a^2(-1+\sin [c+d x]^2)\right) \right) \Bigg) + \\
 & \frac{1}{\left(b+a \cos [c+d x]\right)\left(1-2 \sin [c+d x]^2\right) \sqrt{1-\sin [c+d x]^2}} 3 b \cos [c+d x] \\
 & \cos [2(c+d x)] \\
 & \left(b+a \sqrt{1-\sin [c+d x]^2} \right) \\
 & \left(\frac{\left(\frac{1}{2}-\frac{i}{2}\right)\left(a^2-2 b^2\right) \operatorname{ArcTan}\left[1-\frac{(1+i) \sqrt{a} \sqrt{\sin [c+d x]}}{\left(a^2-b^2\right)^{1 / 4}}\right]}{a^{3 / 2}\left(a^2-b^2\right)^{3 / 4}}-\right. \\
 & \left. \frac{\left(\frac{1}{2}-\frac{i}{2}\right)\left(a^2-2 b^2\right) \operatorname{ArcTan}\left[1+\frac{(1+i) \sqrt{a} \sqrt{\sin [c+d x]}}{\left(a^2-b^2\right)^{1 / 4}}\right]}{a^{3 / 2}\left(a^2-b^2\right)^{3 / 4}}+\left(\left(\frac{1}{4}-\frac{i}{4}\right)\left(a^2-2 b^2\right) \right. \right. \\
 & \left. \left. \operatorname{Log}\left[\sqrt{a^2-b^2}-(1+i) \sqrt{a}\left(a^2-b^2\right)^{1 / 4} \sqrt{\sin [c+d x]}+i a \sin [c+d x]\right] \right) \right) / \\
 & \left(a^{3 / 2}\left(a^2-b^2\right)^{3 / 4}-\left(\left(\frac{1}{4}-\frac{i}{4}\right)\left(a^2-2 b^2\right) \operatorname{Log}\left[\sqrt{a^2-b^2}+(1+i) \sqrt{a}\left(a^2-b^2\right)^{1 / 4} \right. \right. \right. \\
 & \left. \left. \sqrt{\sin [c+d x]}+i a \sin [c+d x]\right] \right) \Bigg) / \left(a^{3 / 2}\left(a^2-b^2\right)^{3 / 4}+\frac{4 \sqrt{\sin [c+d x]}}{a}+\right. \\
 & \left. \left(10 b\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \sin [c+d x]^2, \frac{a^2 \sin [c+d x]^2}{a^2-b^2}\right] \sqrt{\sin [c+d x]} \right) \right) / \\
 & \left(\sqrt{1-\sin [c+d x]^2} \left(5\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \sin [c+d x]^2, \right. \right. \right.
 \end{aligned}$$

$$\left(\frac{a^2 \operatorname{Sin}[c + d x]^2}{a^2 - b^2} \right) + 2 \left(2 a^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \operatorname{Sin}[c + d x]^2, \right. \right. \\ \left. \frac{a^2 \operatorname{Sin}[c + d x]^2}{a^2 - b^2} \right] + (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \operatorname{Sin}[c + d x]^2, \right. \\ \left. \frac{a^2 \operatorname{Sin}[c + d x]^2}{a^2 - b^2} \right] \operatorname{Sin}[c + d x]^2 \left(b^2 + a^2 (-1 + \operatorname{Sin}[c + d x]^2) \right) \right) + \\ \left(36 b (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \operatorname{Sin}[c + d x]^2, \frac{a^2 \operatorname{Sin}[c + d x]^2}{a^2 - b^2} \right] \operatorname{Sin}[c + d x]^{5/2} \right) / \\ \left(5 \sqrt{1 - \operatorname{Sin}[c + d x]^2} \left(9 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \operatorname{Sin}[c + d x]^2, \right. \right. \right. \\ \left. \frac{a^2 \operatorname{Sin}[c + d x]^2}{a^2 - b^2} \right] + 2 \left(2 a^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \operatorname{Sin}[c + d x]^2, \right. \right. \\ \left. \frac{a^2 \operatorname{Sin}[c + d x]^2}{a^2 - b^2} \right] + (a^2 - b^2) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \operatorname{Sin}[c + d x]^2, \right. \\ \left. \frac{a^2 \operatorname{Sin}[c + d x]^2}{a^2 - b^2} \right] \operatorname{Sin}[c + d x]^2 \left(b^2 + a^2 (-1 + \operatorname{Sin}[c + d x]^2) \right) \right) \right)$$

Problem 236: Result unnecessarily involves higher level functions.

$$\int \frac{\sqrt{e \operatorname{Sin}[c + d x]}}{a + b \operatorname{Sec}[c + d x]} dx$$

Optimal (type 4, 356 leaves, 13 steps):

$$\frac{b \sqrt{e} \operatorname{ArcTan} \left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c + d x]}}{(a^2 - b^2)^{1/4} \sqrt{e}} \right]}{a^{3/2} (a^2 - b^2)^{1/4} d} - \frac{b \sqrt{e} \operatorname{ArcTanh} \left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c + d x]}}{(a^2 - b^2)^{1/4} \sqrt{e}} \right]}{a^{3/2} (a^2 - b^2)^{1/4} d} - \\ \frac{b^2 e \operatorname{EllipticPi} \left[\frac{2a}{a - \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + d x \right), 2 \right] \sqrt{\operatorname{Sin}[c + d x]}}{a^2 \left(a - \sqrt{a^2 - b^2} \right) d \sqrt{e \operatorname{Sin}[c + d x]}} - \\ \frac{b^2 e \operatorname{EllipticPi} \left[\frac{2a}{a + \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + d x \right), 2 \right] \sqrt{\operatorname{Sin}[c + d x]}}{a^2 \left(a + \sqrt{a^2 - b^2} \right) d \sqrt{e \operatorname{Sin}[c + d x]}} + \\ \frac{2 \operatorname{EllipticE} \left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x \right), 2 \right] \sqrt{e \operatorname{Sin}[c + d x]}}{a d \sqrt{\operatorname{Sin}[c + d x]}}$$

Result (type 6, 548 leaves):

$$\frac{1}{d (b + a \cos [c + d x]) \sqrt{\sin [c + d x]}} 2 \left(b + a \sqrt{\cos [c + d x]^2} \right) \sqrt{e \sin [c + d x]}$$

$$\left(\left(b \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{a} \sqrt{\sin [c + d x]}}{(-a^2 + b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{a} \sqrt{\sin [c + d x]}}{(-a^2 + b^2)^{1/4}} \right] + \right. \right. \right.$$

$$\left. \left. \left. \begin{aligned} & \operatorname{Log} \left[\sqrt{-a^2 + b^2} - \sqrt{2} \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\sin [c + d x]} + a \sin [c + d x] \right] - \right. \\ & \left. \left. \operatorname{Log} \left[\sqrt{-a^2 + b^2} + \sqrt{2} \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\sin [c + d x]} + a \sin [c + d x] \right] \right) \right) / \right.$$

$$\left(4 \sqrt{2} a^{3/2} (-a^2 + b^2)^{1/4} - \left(7 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \sin [c + d x]^2, \right. \right. \right.$$

$$\left. \left. \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] \sqrt{\cos [c + d x]^2 \sin [c + d x]^{3/2}} \right) / \left(3 (-a^2 + b^2 + a^2 \sin [c + d x]^2) \right.$$

$$\left. \left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \sin [c + d x]^2, \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] + \right. \right.$$

$$\left. \left. 2 \left(2 a^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \sin [c + d x]^2, \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] + \right. \right. \right.$$

$$\left. \left. \left. (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \sin [c + d x]^2, \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] \right) \sin [c + d x]^2 \right) \right)$$

Problem 237: Result unnecessarily involves higher level functions.

$$\int \frac{1}{(a + b \sec [c + d x]) \sqrt{e \sin [c + d x]}} dx$$

Optimal (type 4, 370 leaves, 13 steps):

$$-\frac{b \operatorname{ArcTan} \left[\frac{\sqrt{a} \sqrt{e \sin [c + d x]}}{(a^2 - b^2)^{1/4} \sqrt{e}} \right]}{\sqrt{a} (a^2 - b^2)^{3/4} d \sqrt{e}} - \frac{b \operatorname{ArcTanh} \left[\frac{\sqrt{a} \sqrt{e \sin [c + d x]}}{(a^2 - b^2)^{1/4} \sqrt{e}} \right]}{\sqrt{a} (a^2 - b^2)^{3/4} d \sqrt{e}} +$$

$$\frac{2 \operatorname{EllipticF} \left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x \right), 2 \right] \sqrt{\sin [c + d x]}}{a d \sqrt{e \sin [c + d x]}} +$$

$$\frac{b^2 \operatorname{EllipticPi} \left[\frac{-2a}{a - \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + d x \right), 2 \right] \sqrt{\sin [c + d x]}}{a \left(a^2 - b^2 - a \sqrt{a^2 - b^2} \right) d \sqrt{e \sin [c + d x]}} +$$

$$\frac{b^2 \operatorname{EllipticPi} \left[\frac{-2a}{a + \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + d x \right), 2 \right] \sqrt{\sin [c + d x]}}{a \left(a^2 - b^2 + a \sqrt{a^2 - b^2} \right) d \sqrt{e \sin [c + d x]}}$$

Result (type 6, 546 leaves):

$$\frac{1}{d (b + a \cos [c + d x]) \sqrt{e \sin [c + d x]}} 2 \left(b + a \sqrt{\cos [c + d x]^2} \right) \sqrt{\sin [c + d x]} \left(\left(b \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{a} \sqrt{\sin [c + d x]}}{(-a^2 + b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{a} \sqrt{\sin [c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{-a^2 + b^2} - \sqrt{2} \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\sin [c + d x]} + a \sin [c + d x] \right] + \operatorname{Log} \left[\sqrt{-a^2 + b^2} + \sqrt{2} \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\sin [c + d x]} + a \sin [c + d x] \right] \right) / \left(4 \sqrt{2} \sqrt{a} (-a^2 + b^2)^{3/4} - \left(5 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \sin [c + d x]^2, \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] \sqrt{\cos [c + d x]^2} \sqrt{\sin [c + d x]} \right) / \left((-a^2 + b^2 + a^2 \sin [c + d x]^2) \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \sin [c + d x]^2, \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] + 2 \left(2 a^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \sin [c + d x]^2, \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \sin [c + d x]^2, \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] \right) \sin [c + d x]^2 \right) \right) \right)$$

Problem 238: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{(a + b \sec [c + d x]) (e \sin [c + d x])^{3/2}} dx$$

Optimal (type 4, 430 leaves, 14 steps):

$$\frac{\sqrt{a} b \operatorname{ArcTan} \left[\frac{\sqrt{a} \sqrt{e \sin [c + d x]}}{(a^2 - b^2)^{1/4} \sqrt{e}} \right]}{(a^2 - b^2)^{5/4} d e^{3/2}} - \frac{\sqrt{a} b \operatorname{ArcTanh} \left[\frac{\sqrt{a} \sqrt{e \sin [c + d x]}}{(a^2 - b^2)^{1/4} \sqrt{e}} \right]}{(a^2 - b^2)^{5/4} d e^{3/2}} + \frac{2 (b - a \cos [c + d x])}{(a^2 - b^2) d e \sqrt{e \sin [c + d x]}} - \frac{b^2 \operatorname{EllipticPi} \left[\frac{2 a}{a - \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + d x \right), 2 \right] \sqrt{\sin [c + d x]}}{(a^2 - b^2) (a - \sqrt{a^2 - b^2}) d e \sqrt{e \sin [c + d x]}} - \frac{b^2 \operatorname{EllipticPi} \left[\frac{2 a}{a + \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + d x \right), 2 \right] \sqrt{\sin [c + d x]}}{(a^2 - b^2) (a + \sqrt{a^2 - b^2}) d e \sqrt{e \sin [c + d x]}} - \frac{2 a \operatorname{EllipticE} \left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x \right), 2 \right] \sqrt{e \sin [c + d x]}}{(a^2 - b^2) d e^2 \sqrt{\sin [c + d x]}}$$

Result (type 6, 1229 leaves):

$$-\frac{1}{(a - b) (a + b) d (a + b \sec [c + d x]) (e \sin [c + d x])^{3/2}}$$

$$\begin{aligned}
 & a (b + a \cos [c + d x]) \sec [c + d x] \sin [c + d x]^{3/2} \\
 & \left(\frac{1}{(b + a \cos [c + d x]) (1 - \sin [c + d x])^2} 2 a \cos [c + d x]^2 (b + a \sqrt{1 - \sin [c + d x]^2}) \right. \\
 & \left. \left(\left(b \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{a} \sqrt{\sin [c + d x]}}{(-a^2 + b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{a} \sqrt{\sin [c + d x]}}{(-a^2 + b^2)^{1/4}} \right] + \operatorname{Log} \left[\right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \sqrt{-a^2 + b^2} - \sqrt{2} \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\sin [c + d x]} + a \sin [c + d x] \right] - \operatorname{Log} \left[\right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \sqrt{-a^2 + b^2} + \sqrt{2} \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\sin [c + d x]} + a \sin [c + d x] \right] \right) \right) \right) / \\
 & \left(4 \sqrt{2} a^{3/2} (-a^2 + b^2)^{1/4} \right) - \left(7 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \right. \right. \\
 & \left. \left. \sin [c + d x]^2, \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] \sin [c + d x]^{3/2} \sqrt{1 - \sin [c + d x]^2} \right) / \\
 & \left(3 \left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \sin [c + d x]^2, \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] + 2 \right. \right. \\
 & \left. \left(2 a^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \sin [c + d x]^2, \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \left. \left. (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \sin [c + d x]^2, \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] \right) \right) \\
 & \left. \sin [c + d x]^2 \right) (b^2 + a^2 (-1 + \sin [c + d x]^2)) \Big) + \\
 & \frac{1}{6 (b + a \cos [c + d x]) \sqrt{1 - \sin [c + d x]^2}} b \cos [c + d x] (b + a \sqrt{1 - \sin [c + d x]^2}) \\
 & \left(\left((3 + 3 i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1 + i) \sqrt{a} \sqrt{\sin [c + d x]}}{(a^2 - b^2)^{1/4}} \right] - 2 \right. \right. \right. \\
 & \left. \left. \operatorname{ArcTan} \left[1 + \frac{(1 + i) \sqrt{a} \sqrt{\sin [c + d x]}}{(a^2 - b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{a^2 - b^2} - (1 + i) \sqrt{a} \right. \right. \right. \\
 & \left. \left. (a^2 - b^2)^{1/4} \sqrt{\sin [c + d x]} + i a \sin [c + d x] \right] + \operatorname{Log} \left[\sqrt{a^2 - b^2} + (1 + i) \right. \right. \\
 & \left. \left. \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\sin [c + d x]} + i a \sin [c + d x] \right] \right) \right) / (\sqrt{a} (a^2 - b^2)^{1/4}) + \\
 & \left(56 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \sin [c + d x]^2, \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] \sin [c + d x]^{3/2} \right) / \\
 & \left(\sqrt{1 - \sin [c + d x]^2} \left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \sin [c + d x]^2, \right. \right. \right. \\
 & \left. \left. \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] + 2 \left(2 a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \sin [c + d x]^2, \right. \right. \right. \\
 & \left. \left. \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] + (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \sin [c + d x]^2, \right. \right. \right.
 \end{aligned}$$

$$\left. \left. \left. \left. \frac{a^2 \operatorname{Sin}[c + d x]^2}{a^2 - b^2} \right) \operatorname{Sin}[c + d x]^2 \left(b^2 + a^2 (-1 + \operatorname{Sin}[c + d x]^2) \right) \right) \right) \right) -$$

$$\frac{2 (b - a \operatorname{Cos}[c + d x]) (b + a \operatorname{Cos}[c + d x]) \operatorname{Tan}[c + d x]}{(-a^2 + b^2) d (a + b \operatorname{Sec}[c + d x]) (e \operatorname{Sin}[c + d x])^{3/2}}$$

Problem 239: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{(a + b \operatorname{Sec}[c + d x]) (e \operatorname{Sin}[c + d x])^{5/2}} dx$$

Optimal (type 4, 452 leaves, 14 steps):

$$-\frac{a^{3/2} b \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c + d x]}}{(a^2 - b^2)^{1/4} \sqrt{e}}\right]}{(a^2 - b^2)^{7/4} d e^{5/2}} - \frac{a^{3/2} b \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c + d x]}}{(a^2 - b^2)^{1/4} \sqrt{e}}\right]}{(a^2 - b^2)^{7/4} d e^{5/2}} +$$

$$\frac{2 (b - a \operatorname{Cos}[c + d x])}{3 (a^2 - b^2) d e (e \operatorname{Sin}[c + d x])^{3/2}} + \frac{2 a \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), 2\right] \sqrt{\operatorname{Sin}[c + d x]}}{3 (a^2 - b^2) d e^2 \sqrt{e \operatorname{Sin}[c + d x]}} +$$

$$\frac{a b^2 \operatorname{EllipticPi}\left[\frac{-2 a}{a - \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), 2\right] \sqrt{\operatorname{Sin}[c + d x]}}{(a^2 - b^2) (a^2 - b^2 - a \sqrt{a^2 - b^2}) d e^2 \sqrt{e \operatorname{Sin}[c + d x]}} +$$

$$\frac{a b^2 \operatorname{EllipticPi}\left[\frac{-2 a}{a + \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right), 2\right] \sqrt{\operatorname{Sin}[c + d x]}}{(a^2 - b^2) (a^2 - b^2 + a \sqrt{a^2 - b^2}) d e^2 \sqrt{e \operatorname{Sin}[c + d x]}}$$

Result (type 6, 1233 leaves):

$$-\frac{1}{3 (a - b) (a + b) d (a + b \operatorname{Sec}[c + d x]) (e \operatorname{Sin}[c + d x])^{5/2}}$$

$$\frac{a (b + a \operatorname{Cos}[c + d x]) \operatorname{Sec}[c + d x] \operatorname{Sin}[c + d x]^{5/2}}{\left(-\frac{1}{(b + a \operatorname{Cos}[c + d x]) (1 - \operatorname{Sin}[c + d x])^2} 2 a \operatorname{Cos}[c + d x]^2 (b + a \sqrt{1 - \operatorname{Sin}[c + d x]^2}) \right.$$

$$\left. \left(\left(b \left(-2 \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{a} \sqrt{\operatorname{Sin}[c + d x]}}{(-a^2 + b^2)^{1/4}}\right] + 2 \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{a} \sqrt{\operatorname{Sin}[c + d x]}}{(-a^2 + b^2)^{1/4}}\right] \right) - \right.$$

$$\left. \left. \operatorname{Log}\left[\sqrt{-a^2 + b^2} - \sqrt{2} \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\operatorname{Sin}[c + d x]} + a \operatorname{Sin}[c + d x]\right] + \right.$$

$$\left. \left. \operatorname{Log}\left[\sqrt{-a^2 + b^2} + \sqrt{2} \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\operatorname{Sin}[c + d x]} + a \operatorname{Sin}[c + d x]\right] \right) \right) /$$

$$\left(4 \sqrt{2} \sqrt{a} (-a^2 + b^2)^{3/4} \right) - \left(5 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \right.$$

$$\frac{a^{5/2} b \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{(a^2-b^2)^{9/4} d e^{7/2}} - \frac{a^{5/2} b \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{(a^2-b^2)^{9/4} d e^{7/2}} +$$

$$\frac{2(b-a \operatorname{Cos}[c+dx])}{5(a^2-b^2) d e (e \operatorname{Sin}[c+dx])^{5/2}} + \frac{2(5a^2 b - a(3a^2 + 2b^2) \operatorname{Cos}[c+dx])}{5(a^2-b^2)^2 d e^3 \sqrt{e \operatorname{Sin}[c+dx]}}$$

$$\frac{a^2 b^2 \operatorname{EllipticPi}\left[\frac{2a}{a-\sqrt{a^2-b^2}}, \frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\operatorname{Sin}[c+dx]}}{(a^2-b^2)^2 (a-\sqrt{a^2-b^2}) d e^3 \sqrt{e \operatorname{Sin}[c+dx]}} -$$

$$\frac{a^2 b^2 \operatorname{EllipticPi}\left[\frac{2a}{a+\sqrt{a^2-b^2}}, \frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\operatorname{Sin}[c+dx]}}{(a^2-b^2)^2 (a+\sqrt{a^2-b^2}) d e^3 \sqrt{e \operatorname{Sin}[c+dx]}} -$$

$$\frac{2a(3a^2 + 2b^2) \operatorname{EllipticE}\left[\frac{1}{2}\left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{e \operatorname{Sin}[c+dx]}}{5(a^2-b^2)^2 d e^4 \sqrt{\operatorname{Sin}[c+dx]}}$$

Result (type 6, 1324 leaves):

$$\frac{1}{5(a-b)^2 (a+b)^2 d (a+b \operatorname{Sec}[c+dx]) (e \operatorname{Sin}[c+dx])^{7/2}}$$

$$a (b+a \operatorname{Cos}[c+dx]) \operatorname{Sec}[c+dx] \operatorname{Sin}[c+dx]^{7/2}$$

$$\left(\frac{1}{(b+a \operatorname{Cos}[c+dx]) (1-\operatorname{Sin}[c+dx])^2} 2(3a^3 + 2ab^2) \operatorname{Cos}[c+dx]^2 (b+a \sqrt{1-\operatorname{Sin}[c+dx]^2}) \right.$$

$$\left. \left(\left(b \left(-2 \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{a} \sqrt{\operatorname{Sin}[c+dx]}}{(-a^2+b^2)^{1/4}}\right] + 2 \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{a} \sqrt{\operatorname{Sin}[c+dx]}}{(-a^2+b^2)^{1/4}}\right] \right) + \operatorname{Log}\left[\right. \right. \right.$$

$$\left. \left. \left. \frac{\sqrt{-a^2+b^2} - \sqrt{2} \sqrt{a} (-a^2+b^2)^{1/4} \sqrt{\operatorname{Sin}[c+dx]} + a \operatorname{Sin}[c+dx]}{\sqrt{-a^2+b^2} + \sqrt{2} \sqrt{a} (-a^2+b^2)^{1/4} \sqrt{\operatorname{Sin}[c+dx]} + a \operatorname{Sin}[c+dx]} \right] - \operatorname{Log}\left[\right. \right. \right.$$

$$\left. \left. \left. \frac{4\sqrt{2} a^{3/2} (-a^2+b^2)^{1/4}}{\operatorname{Sin}[c+dx]^2, \frac{a^2 \operatorname{Sin}[c+dx]^2}{a^2-b^2}} \operatorname{Sin}[c+dx]^{3/2} \sqrt{1-\operatorname{Sin}[c+dx]^2} \right] \right) /$$

$$\left(3 \left(7(a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \operatorname{Sin}[c+dx]^2, \frac{a^2 \operatorname{Sin}[c+dx]^2}{a^2-b^2}\right] + 2 \right. \right.$$

$$\left. \left(2a^2 \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \operatorname{Sin}[c+dx]^2, \frac{a^2 \operatorname{Sin}[c+dx]^2}{a^2-b^2}\right] + \right. \right.$$

$$\left. \left. (-a^2+b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \operatorname{Sin}[c+dx]^2, \frac{a^2 \operatorname{Sin}[c+dx]^2}{a^2-b^2}\right] \right) \right) \operatorname{Sin}[c+dx]^2 (b^2+a^2(-1+\operatorname{Sin}[c+dx]^2)) \right) +$$

$$\begin{aligned}
 & \frac{1}{12 (b + a \cos [c + d x]) \sqrt{1 - \sin [c + d x]^2}} (8 a^2 b + 2 b^3) \cos [c + d x] \\
 & \left(b + a \sqrt{1 - \sin [c + d x]^2} \right) \\
 & \left(\left((3 + 3 i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1 + i) \sqrt{a} \sqrt{\sin [c + d x]}}{(a^2 - b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[1 + \frac{(1 + i) \sqrt{a} \sqrt{\sin [c + d x]}}{(a^2 - b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{a^2 - b^2} - (1 + i) \sqrt{a} \right. \right. \right. \right. \\
 & \left. \left. \left. (a^2 - b^2)^{1/4} \sqrt{\sin [c + d x]} + i a \sin [c + d x] \right] + \operatorname{Log} \left[\sqrt{a^2 - b^2} + (1 + i) \sqrt{a} \right. \right. \right. \\
 & \left. \left. \left. \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\sin [c + d x]} + i a \sin [c + d x] \right] \right) \right) / \left(\sqrt{a} (a^2 - b^2)^{1/4} + \right. \\
 & \left. \left(56 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \sin [c + d x]^2, \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] \sin [c + d x]^{3/2} \right) / \right. \\
 & \left. \left(\sqrt{1 - \sin [c + d x]^2} \left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \sin [c + d x]^2, \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] + 2 \left(2 a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \sin [c + d x]^2, \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] + (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \sin [c + d x]^2, \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] \right) \sin [c + d x]^2 \right) (b^2 + a^2 (-1 + \sin [c + d x]^2)) \right) \right) \right) + \\
 & \left((b + a \cos [c + d x]) \left(- \frac{2 (-5 a^2 b + 3 a^3 \cos [c + d x] + 2 a b^2 \cos [c + d x]) \operatorname{Csc} [c + d x]}{5 (-a^2 + b^2)^2} - \frac{2 (b - a \cos [c + d x]) \operatorname{Csc} [c + d x]^3}{5 (-a^2 + b^2)} \right) \right. \\
 & \left. \sin [c + d x]^3 \tan [c + d x] \right) / \\
 & \left(d (a + b \sec [c + d x]) (e \sin [c + d x])^{7/2} \right)
 \end{aligned}$$

Problem 241: Result unnecessarily involves higher level functions.

$$\int \frac{(e \sin [c + d x])^{9/2}}{(a + b \sec [c + d x])^2} dx$$

Optimal (type 4, 1070 leaves, 35 steps):

$$\begin{aligned}
 & - \frac{7 b^3 (a^2 - b^2)^{3/4} e^{9/2} \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{2 a^{13/2} d} + \frac{2 b (a^2 - b^2)^{7/4} e^{9/2} \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{a^{13/2} d} + \\
 & \frac{7 b^3 (a^2 - b^2)^{3/4} e^{9/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{2 a^{13/2} d} - \frac{2 b (a^2 - b^2)^{7/4} e^{9/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{a^{13/2} d} + \\
 & \left(7 b^4 (a^2 - b^2) e^5 \operatorname{EllipticPi}\left[\frac{2 a}{a - \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\operatorname{Sin}[c+dx]}\right) / \\
 & \left(2 a^7 \left(a - \sqrt{a^2 - b^2}\right) d \sqrt{e \operatorname{Sin}[c+dx]}\right) - \\
 & \left(2 b^2 (a^2 - b^2)^2 e^5 \operatorname{EllipticPi}\left[\frac{2 a}{a - \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\operatorname{Sin}[c+dx]}\right) / \\
 & \left(a^7 \left(a - \sqrt{a^2 - b^2}\right) d \sqrt{e \operatorname{Sin}[c+dx]}\right) + \\
 & \left(7 b^4 (a^2 - b^2) e^5 \operatorname{EllipticPi}\left[\frac{2 a}{a + \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\operatorname{Sin}[c+dx]}\right) / \\
 & \left(2 a^7 \left(a + \sqrt{a^2 - b^2}\right) d \sqrt{e \operatorname{Sin}[c+dx]}\right) - \\
 & \left(2 b^2 (a^2 - b^2)^2 e^5 \operatorname{EllipticPi}\left[\frac{2 a}{a + \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\operatorname{Sin}[c+dx]}\right) / \\
 & \left(a^7 \left(a + \sqrt{a^2 - b^2}\right) d \sqrt{e \operatorname{Sin}[c+dx]}\right) + \frac{14 e^4 \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{e \operatorname{Sin}[c+dx]}}{15 a^2 d \sqrt{\operatorname{Sin}[c+dx]}} - \\
 & \frac{7 b^2 (3 a^2 - 5 b^2) e^4 \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{e \operatorname{Sin}[c+dx]}}{5 a^6 d \sqrt{\operatorname{Sin}[c+dx]}} - \\
 & \frac{4 b^2 (8 a^2 - 5 b^2) e^4 \operatorname{EllipticE}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{e \operatorname{Sin}[c+dx]}}{5 a^6 d \sqrt{\operatorname{Sin}[c+dx]}} - \\
 & \frac{14 e^3 \operatorname{Cos}[c+dx] (e \operatorname{Sin}[c+dx])^{3/2}}{45 a^2 d} - \frac{7 b^2 e^3 (5 b - 3 a \operatorname{Cos}[c+dx]) (e \operatorname{Sin}[c+dx])^{3/2}}{15 a^5 d} + \\
 & \frac{4 b e^3 (5 (a^2 - b^2) + 3 a b \operatorname{Cos}[c+dx]) (e \operatorname{Sin}[c+dx])^{3/2}}{15 a^5 d} + \frac{4 b e (e \operatorname{Sin}[c+dx])^{7/2}}{7 a^3 d} - \\
 & \frac{2 e \operatorname{Cos}[c+dx] (e \operatorname{Sin}[c+dx])^{7/2}}{9 a^2 d} + \frac{b^2 e (e \operatorname{Sin}[c+dx])^{7/2}}{a^3 d (b + a \operatorname{Cos}[c+dx])}
 \end{aligned}$$

Result (type 6, 1368 leaves):

$$\begin{aligned}
 & \frac{1}{30 a^5 d (a + b \operatorname{Sec}[c+dx])^2 \operatorname{Sin}[c+dx]^{9/2}} \\
 & (b + a \operatorname{Cos}[c+dx])^2 \operatorname{Sec}[c+dx]^2 (e \operatorname{Sin}[c+dx])^{9/2} \left(\frac{1}{(b + a \operatorname{Cos}[c+dx]) (1 - \operatorname{Sin}[c+dx]^2)} \right. \\
 & \left. 2 (14 a^4 - 159 a^2 b^2 + 165 b^4) \operatorname{Cos}[c+dx]^2 (b + a \sqrt{1 - \operatorname{Sin}[c+dx]^2}) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(\left(b \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{a} \sqrt{\sin[c+dx]}}{(-a^2+b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{a} \sqrt{\sin[c+dx]}}{(-a^2+b^2)^{1/4}} \right] + \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[\sqrt{-a^2+b^2} - \sqrt{2} \sqrt{a} (-a^2+b^2)^{1/4} \sqrt{\sin[c+dx]} + a \sin[c+dx] \right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[\sqrt{-a^2+b^2} + \sqrt{2} \sqrt{a} (-a^2+b^2)^{1/4} \sqrt{\sin[c+dx]} + a \sin[c+dx] \right] \right) \right) / \\
 & \quad \left(4 \sqrt{2} a^{3/2} (-a^2+b^2)^{1/4} - \left(7 a (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \right. \right. \right. \\
 & \quad \left. \left. \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2-b^2} \right] \sin[c+dx]^{3/2} \sqrt{1-\sin[c+dx]^2} \right) / \\
 & \quad \left(3 \left(7 (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2-b^2} \right] + \right. \right. \\
 & \quad \left. \left. 2 \left(2 a^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2-b^2} \right] + \right. \right. \right. \\
 & \quad \left. \left. \left. (-a^2+b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2-b^2} \right] \right) \right) \right) \\
 & \quad \left. \left. \sin[c+dx]^2 \right) (b^2+a^2(-1+\sin[c+dx]^2)) \right) \right) + \\
 & \quad \frac{1}{12 (b+a \cos[c+dx]) \sqrt{1-\sin[c+dx]^2}} (-46 a^3 b + 66 a b^3) \cos[c+dx] \\
 & \quad \left(b+a \sqrt{1-\sin[c+dx]^2} \right) \\
 & \quad \left(\left((3+3i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{a} \sqrt{\sin[c+dx]}}{(a^2-b^2)^{1/4}} \right] - \right. \right. \right. \\
 & \quad \left. \left. 2 \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{a} \sqrt{\sin[c+dx]}}{(a^2-b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{a^2-b^2} - \right. \right. \right. \\
 & \quad \left. \left. \left. (1+i) \sqrt{a} (a^2-b^2)^{1/4} \sqrt{\sin[c+dx]} + i a \sin[c+dx] \right] + \operatorname{Log} \left[\sqrt{a^2-b^2} + \right. \right. \right. \\
 & \quad \left. \left. \left. (1+i) \sqrt{a} (a^2-b^2)^{1/4} \sqrt{\sin[c+dx]} + i a \sin[c+dx] \right] \right) \right) / \left(\sqrt{a} (a^2-b^2)^{1/4} \right) + \\
 & \quad \left(56 b (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2-b^2} \right] \sin[c+dx]^{3/2} \right) / \\
 & \quad \left(\sqrt{1-\sin[c+dx]^2} \left(7 (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \sin[c+dx]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{a^2 \sin[c+dx]^2}{a^2-b^2} \right] + 2 \left(2 a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \sin[c+dx]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{a^2 \sin[c+dx]^2}{a^2-b^2} \right] + (a^2-b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \sin[c+dx]^2, \right. \right. \\
 & \quad \left. \left. \frac{a^2 \sin[c+dx]^2}{a^2-b^2} \right] \right) \sin[c+dx]^2 \right) (b^2+a^2(-1+\sin[c+dx]^2)) \right) \right) \right) +
 \end{aligned}$$

$$\left((b + a \cos [c + d x])^2 \operatorname{Csc}[c + d x]^4 \operatorname{Sec}[c + d x]^2 (e \sin [c + d x])^{9/2} \right. \\ \left(- \frac{b (-37 a^2 + 56 b^2) \sin [c + d x]}{21 a^5} + \frac{a^2 b^2 \sin [c + d x] - b^4 \sin [c + d x]}{a^5 (b + a \cos [c + d x])} - \frac{(19 a^2 - 54 b^2) \sin [2 (c + d x)]}{90 a^4} - \frac{b \sin [3 (c + d x)]}{7 a^3} + \frac{\sin [4 (c + d x)]}{36 a^2} \right) \Big) / (d (a + b \operatorname{Sec}[c + d x])^2)$$

Problem 242: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \sin [c + d x])^{7/2}}{(a + b \operatorname{Sec}[c + d x])^2} dx$$

Optimal (type 4, 1101 leaves, 35 steps):

$$\begin{aligned}
 & \frac{5 b^3 (a^2 - b^2)^{1/4} e^{7/2} \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{e \sin[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{2 a^{11/2} d} - \\
 & \frac{2 b (a^2 - b^2)^{5/4} e^{7/2} \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{e \sin[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{a^{11/2} d} + \frac{5 b^3 (a^2 - b^2)^{1/4} e^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{e \sin[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{2 a^{11/2} d} - \\
 & \frac{2 b (a^2 - b^2)^{5/4} e^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{e \sin[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{a^{11/2} d} + \frac{10 e^4 \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\sin[c+dx]}}{21 a^2 d \sqrt{e \sin[c+dx]}} - \\
 & \frac{5 b^2 (a^2 - 3 b^2) e^4 \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\sin[c+dx]}}{3 a^6 d \sqrt{e \sin[c+dx]}} - \\
 & \frac{4 b^2 (4 a^2 - 3 b^2) e^4 \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\sin[c+dx]}}{3 a^6 d \sqrt{e \sin[c+dx]}} - \\
 & \left(\frac{5 b^4 (a^2 - b^2) e^4 \operatorname{EllipticPi}\left[\frac{2 a}{a - \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\sin[c+dx]}}{\left(2 a^6 (a^2 - b^2 - a \sqrt{a^2 - b^2}) d \sqrt{e \sin[c+dx]}\right)} \right) / \\
 & \left(\frac{2 b^2 (a^2 - b^2)^2 e^4 \operatorname{EllipticPi}\left[\frac{2 a}{a - \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\sin[c+dx]}}{\left(a^6 (a^2 - b^2 - a \sqrt{a^2 - b^2}) d \sqrt{e \sin[c+dx]}\right)} \right) - \\
 & \left(\frac{5 b^4 (a^2 - b^2) e^4 \operatorname{EllipticPi}\left[\frac{2 a}{a + \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\sin[c+dx]}}{\left(2 a^6 (a^2 - b^2 + a \sqrt{a^2 - b^2}) d \sqrt{e \sin[c+dx]}\right)} \right) + \\
 & \left(\frac{2 b^2 (a^2 - b^2)^2 e^4 \operatorname{EllipticPi}\left[\frac{2 a}{a + \sqrt{a^2 - b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\sin[c+dx]}}{\left(a^6 (a^2 - b^2 + a \sqrt{a^2 - b^2}) d \sqrt{e \sin[c+dx]}\right)} \right) - \\
 & \frac{10 e^3 \cos[c+dx] \sqrt{e \sin[c+dx]}}{21 a^2 d} - \frac{5 b^2 e^3 (3 b - a \cos[c+dx]) \sqrt{e \sin[c+dx]}}{3 a^5 d} + \\
 & \frac{4 b e^3 (3 (a^2 - b^2) + a b \cos[c+dx]) \sqrt{e \sin[c+dx]}}{3 a^5 d} + \frac{4 b e (e \sin[c+dx])^{5/2}}{5 a^3 d} - \\
 & \frac{2 e \cos[c+dx] (e \sin[c+dx])^{5/2}}{7 a^2 d} + \frac{b^2 e (e \sin[c+dx])^{5/2}}{a^3 d (b + a \cos[c+dx])}
 \end{aligned}$$

Result (type 6, 2295 leaves):

$$\left((b + a \cos[c+dx])^2 \left(-\frac{(23 a^2 - 84 b^2) \cos[c+dx]}{42 a^4} - \frac{b^2 (-a^2 + b^2)}{a^5 (b + a \cos[c+dx])} \right) - \right.$$

$$\begin{aligned}
 & \left. \frac{2 b \operatorname{Cos}[2(c+d x)]}{5 a^3} + \frac{\operatorname{Cos}[3(c+d x)]}{14 a^2} \right) \operatorname{Csc}[c+d x]^3 \operatorname{Sec}[c+d x]^2 (e \operatorname{Sin}[c+d x])^{7/2} \Big/ \\
 & \left(d (a+b \operatorname{Sec}[c+d x])^2 \right) + \frac{1}{210 a^5 d (a+b \operatorname{Sec}[c+d x])^2 \operatorname{Sin}[c+d x]^{7/2}} \\
 & (b+a \operatorname{Cos}[c+d x])^2 \operatorname{Sec}[c+d x]^2 (e \operatorname{Sin}[c+d x])^{7/2} \left(\frac{1}{(b+a \operatorname{Cos}[c+d x]) (1-\operatorname{Sin}[c+d x])^2} \right. \\
 & 2 (50 a^4 - 273 a^2 b^2 + 105 b^4) \operatorname{Cos}[c+d x]^2 (b+a \sqrt{1-\operatorname{Sin}[c+d x]^2}) \\
 & \left. \left(\left(b \left(-2 \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{a} \sqrt{\operatorname{Sin}[c+d x]}}{(-a^2+b^2)^{1/4}}\right] + 2 \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{a} \sqrt{\operatorname{Sin}[c+d x]}}{(-a^2+b^2)^{1/4}}\right] - \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Log}\left[\sqrt{-a^2+b^2} - \sqrt{2} \sqrt{a} (-a^2+b^2)^{1/4} \sqrt{\operatorname{Sin}[c+d x]} + a \operatorname{Sin}[c+d x]\right] + \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Log}\left[\sqrt{-a^2+b^2} + \sqrt{2} \sqrt{a} (-a^2+b^2)^{1/4} \sqrt{\operatorname{Sin}[c+d x]} + a \operatorname{Sin}[c+d x]\right] \right) \right) \right) \Big/ \\
 & \left(4 \sqrt{2} \sqrt{a} (-a^2+b^2)^{3/4} \right) - \left(5 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \right. \right. \\
 & \quad \left. \left. \operatorname{Sin}[c+d x]^2, \frac{a^2 \operatorname{Sin}[c+d x]^2}{a^2-b^2} \right] \sqrt{\operatorname{Sin}[c+d x]} \sqrt{1-\operatorname{Sin}[c+d x]^2} \right) \Big/ \\
 & \left(\left(5 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \operatorname{Sin}[c+d x]^2, \frac{a^2 \operatorname{Sin}[c+d x]^2}{a^2-b^2} \right] + \right. \right. \\
 & \quad \left. \left(2 a^2 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \operatorname{Sin}[c+d x]^2, \frac{a^2 \operatorname{Sin}[c+d x]^2}{a^2-b^2} \right] + (-a^2+b^2) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \operatorname{Sin}[c+d x]^2, \frac{a^2 \operatorname{Sin}[c+d x]^2}{a^2-b^2} \right] \right) \operatorname{Sin}[c+d x]^2 \right) \\
 & \left. \left. \left. (b^2+a^2(-1+\operatorname{Sin}[c+d x]^2)) \right) \right) \right) + \frac{1}{(b+a \operatorname{Cos}[c+d x]) \sqrt{1-\operatorname{Sin}[c+d x]^2}} \\
 & 2 (-139 a^3 b + 210 a b^3) \operatorname{Cos}[c+d x] (b+a \sqrt{1-\operatorname{Sin}[c+d x]^2}) \left(-\frac{1}{(a^2-b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{a} \right. \\
 & \left. \left(2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{a} \sqrt{\operatorname{Sin}[c+d x]}}{(a^2-b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{a} \sqrt{\operatorname{Sin}[c+d x]}}{(a^2-b^2)^{1/4}}\right] \right) + \right. \\
 & \quad \left. \operatorname{Log}\left[\sqrt{a^2-b^2} - (1+i) \sqrt{a} (a^2-b^2)^{1/4} \sqrt{\operatorname{Sin}[c+d x]} + i a \operatorname{Sin}[c+d x]\right] - \right. \\
 & \quad \left. \operatorname{Log}\left[\sqrt{a^2-b^2} + (1+i) \sqrt{a} (a^2-b^2)^{1/4} \sqrt{\operatorname{Sin}[c+d x]} + i a \operatorname{Sin}[c+d x]\right] \right) + \\
 & \left(5 b (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \operatorname{Sin}[c+d x]^2, \frac{a^2 \operatorname{Sin}[c+d x]^2}{a^2-b^2} \right] \sqrt{\operatorname{Sin}[c+d x]} \right) \Big/ \\
 & \left(\sqrt{1-\operatorname{Sin}[c+d x]^2} \left(5 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \operatorname{Sin}[c+d x]^2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{a^2 \operatorname{Sin}[c+dx]^2}{a^2-b^2} \right] + 2 \left(2 a^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \operatorname{Sin}[c+dx]^2, \right. \right. \\
 & \left. \left. \frac{a^2 \operatorname{Sin}[c+dx]^2}{a^2-b^2} \right] + (a^2-b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \operatorname{Sin}[c+dx]^2, \right. \right. \\
 & \left. \left. \frac{a^2 \operatorname{Sin}[c+dx]^2}{a^2-b^2} \right] \right) \operatorname{Sin}[c+dx]^2 \left(b^2 + a^2 (-1 + \operatorname{Sin}[c+dx]^2) \right) \Bigg) + \\
 & \frac{1}{(b+a \operatorname{Cos}[c+dx]) (1-2 \operatorname{Sin}[c+dx]^2) \sqrt{1-\operatorname{Sin}[c+dx]^2}} (231 a^3 b - 420 a b^3) \\
 & \operatorname{Cos}[c+dx] \operatorname{Cos}[2(c+dx)] \\
 & \left(b + a \sqrt{1-\operatorname{Sin}[c+dx]^2} \right) \\
 & \left(\frac{\left(\frac{1}{2} - \frac{i}{2} \right) (a^2 - 2 b^2) \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{a} \sqrt{\operatorname{Sin}[c+dx]}}{(a^2-b^2)^{1/4}} \right]}{a^{3/2} (a^2-b^2)^{3/4}} - \right. \\
 & \left. \frac{\left(\frac{1}{2} - \frac{i}{2} \right) (a^2 - 2 b^2) \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{a} \sqrt{\operatorname{Sin}[c+dx]}}{(a^2-b^2)^{1/4}} \right]}{a^{3/2} (a^2-b^2)^{3/4}} + \left(\left(\frac{1}{4} - \frac{i}{4} \right) (a^2 - 2 b^2) \right. \right. \\
 & \left. \left. \operatorname{Log}\left[\sqrt{a^2-b^2} - (1+i) \sqrt{a} (a^2-b^2)^{1/4} \sqrt{\operatorname{Sin}[c+dx]} + i a \operatorname{Sin}[c+dx] \right] \right) \right) / \\
 & \left(a^{3/2} (a^2-b^2)^{3/4} - \left(\left(\frac{1}{4} - \frac{i}{4} \right) (a^2 - 2 b^2) \operatorname{Log}\left[\sqrt{a^2-b^2} + (1+i) \sqrt{a} (a^2-b^2)^{1/4} \right. \right. \right. \\
 & \left. \left. \left. \sqrt{\operatorname{Sin}[c+dx]} + i a \operatorname{Sin}[c+dx] \right] \right) \right) / \left(a^{3/2} (a^2-b^2)^{3/4} + \frac{4 \sqrt{\operatorname{Sin}[c+dx]}}{a} + \right. \\
 & \left. \left(10 b (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \operatorname{Sin}[c+dx]^2, \frac{a^2 \operatorname{Sin}[c+dx]^2}{a^2-b^2} \right] \sqrt{\operatorname{Sin}[c+dx]} \right) \right) / \\
 & \left(\sqrt{1-\operatorname{Sin}[c+dx]^2} \left(5 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \operatorname{Sin}[c+dx]^2, \right. \right. \right. \\
 & \left. \left. \frac{a^2 \operatorname{Sin}[c+dx]^2}{a^2-b^2} \right] + 2 \left(2 a^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \operatorname{Sin}[c+dx]^2, \right. \right. \right. \\
 & \left. \left. \frac{a^2 \operatorname{Sin}[c+dx]^2}{a^2-b^2} \right] + (a^2-b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \operatorname{Sin}[c+dx]^2, \right. \right. \\
 & \left. \left. \frac{a^2 \operatorname{Sin}[c+dx]^2}{a^2-b^2} \right] \right) \operatorname{Sin}[c+dx]^2 \left(b^2 + a^2 (-1 + \operatorname{Sin}[c+dx]^2) \right) \Bigg) + \\
 & \left(36 b (-a^2+b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \operatorname{Sin}[c+dx]^2, \frac{a^2 \operatorname{Sin}[c+dx]^2}{a^2-b^2} \right] \operatorname{Sin}[c+dx]^{5/2} \right) / \\
 & \left(5 \sqrt{1-\operatorname{Sin}[c+dx]^2} \left(9 (a^2-b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \operatorname{Sin}[c+dx]^2, \right. \right. \right. \\
 & \left. \left. \frac{a^2 \operatorname{Sin}[c+dx]^2}{a^2-b^2} \right] + 2 \left(2 a^2 \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \operatorname{Sin}[c+dx]^2, \right. \right. \right. \\
 & \left. \left. \frac{a^2 \operatorname{Sin}[c+dx]^2}{a^2-b^2} \right] + (a^2-b^2) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \operatorname{Sin}[c+dx]^2, \right. \right.
 \end{aligned}$$

$$\left. \left. \left. \left. \frac{a^2 \operatorname{Sin}[c + d x]^2}{a^2 - b^2} \right) \operatorname{Sin}[c + d x]^2 \left(b^2 + a^2 (-1 + \operatorname{Sin}[c + d x]^2) \right) \right) \right) \right)$$

Problem 243: Result unnecessarily involves higher level functions.

$$\int \frac{(e \operatorname{Sin}[c + d x])^{5/2}}{(a + b \operatorname{Sec}[c + d x])^2} dx$$

Optimal (type 4, 850 leaves, 32 steps):

$$\begin{aligned} & - \frac{3 b^3 e^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c+d x]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{2 a^{9/2} (a^2-b^2)^{1/4} d} + \frac{2 b (a^2-b^2)^{3/4} e^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c+d x]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{a^{9/2} d} + \\ & \frac{3 b^3 e^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c+d x]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{2 a^{9/2} (a^2-b^2)^{1/4} d} - \frac{2 b (a^2-b^2)^{3/4} e^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c+d x]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{a^{9/2} d} + \\ & \frac{3 b^4 e^3 \operatorname{EllipticPi}\left[\frac{2 a}{a-\sqrt{a^2-b^2}}, \frac{1}{2} \left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{\operatorname{Sin}[c+d x]}}{2 a^5 \left(a-\sqrt{a^2-b^2}\right) d \sqrt{e \operatorname{Sin}[c+d x]}} - \\ & \left(2 b^2 (a^2-b^2) e^3 \operatorname{EllipticPi}\left[\frac{2 a}{a-\sqrt{a^2-b^2}}, \frac{1}{2} \left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{\operatorname{Sin}[c+d x]}\right) / \\ & \left(a^5 \left(a-\sqrt{a^2-b^2}\right) d \sqrt{e \operatorname{Sin}[c+d x]}\right) + \\ & \frac{3 b^4 e^3 \operatorname{EllipticPi}\left[\frac{2 a}{a+\sqrt{a^2-b^2}}, \frac{1}{2} \left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{\operatorname{Sin}[c+d x]}}{2 a^5 \left(a+\sqrt{a^2-b^2}\right) d \sqrt{e \operatorname{Sin}[c+d x]}} - \\ & \left(2 b^2 (a^2-b^2) e^3 \operatorname{EllipticPi}\left[\frac{2 a}{a+\sqrt{a^2-b^2}}, \frac{1}{2} \left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{\operatorname{Sin}[c+d x]}\right) / \\ & \left(a^5 \left(a+\sqrt{a^2-b^2}\right) d \sqrt{e \operatorname{Sin}[c+d x]}\right) + \frac{6 e^2 \operatorname{EllipticE}\left[\frac{1}{2} \left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{e \operatorname{Sin}[c+d x]}}{5 a^2 d \sqrt{\operatorname{Sin}[c+d x]}} - \\ & \frac{7 b^2 e^2 \operatorname{EllipticE}\left[\frac{1}{2} \left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{e \operatorname{Sin}[c+d x]}}{a^4 d \sqrt{\operatorname{Sin}[c+d x]}} + \frac{4 b e (e \operatorname{Sin}[c+d x])^{3/2}}{3 a^3 d} - \\ & \frac{2 e \operatorname{Cos}[c+d x] (e \operatorname{Sin}[c+d x])^{3/2}}{5 a^2 d} + \frac{b^2 e (e \operatorname{Sin}[c+d x])^{3/2}}{a^3 d (b+a \operatorname{Cos}[c+d x])} \end{aligned}$$

Result (type 6, 1280 leaves):

$$- \frac{1}{10 a^3 d (a + b \operatorname{Sec}[c + d x])^2 \operatorname{Sin}[c + d x]^{5/2}}$$

$$\begin{aligned}
 & (b + a \cos [c + d x])^2 \sec [c + d x]^2 (e \sin [c + d x])^{5/2} \left(\frac{1}{(b + a \cos [c + d x]) (1 - \sin [c + d x]^2)} \right. \\
 & 2 (-6 a^2 + 35 b^2) \cos [c + d x]^2 \left(b + a \sqrt{1 - \sin [c + d x]^2} \right) \\
 & \left. \left(\left(b \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{a} \sqrt{\sin [c + d x]}}{(-a^2 + b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{a} \sqrt{\sin [c + d x]}}{(-a^2 + b^2)^{1/4}} \right] \right) + \operatorname{Log} \left[\right. \right. \right. \\
 & \left. \left. \left. \frac{\sqrt{-a^2 + b^2} - \sqrt{2} \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\sin [c + d x]} + a \sin [c + d x]}{\sqrt{-a^2 + b^2} + \sqrt{2} \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\sin [c + d x]} + a \sin [c + d x]} \right] \right) \right) \Bigg/ \\
 & \left(4 \sqrt{2} a^{3/2} (-a^2 + b^2)^{1/4} \right) - \left(7 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \right. \right. \\
 & \left. \left. \sin [c + d x]^2, \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] \sin [c + d x]^{3/2} \sqrt{1 - \sin [c + d x]^2} \right) \Bigg/ \\
 & \left(3 \left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \sin [c + d x]^2, \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] + 2 \right. \right. \\
 & \left. \left(2 a^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \sin [c + d x]^2, \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \left. \left. (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \sin [c + d x]^2, \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] \right) \right) \\
 & \left. \sin [c + d x]^2 \right) (b^2 + a^2 (-1 + \sin [c + d x]^2)) \Bigg) + \\
 & \frac{1}{6 (b + a \cos [c + d x]) \sqrt{1 - \sin [c + d x]^2}} 7 a b \cos [c + d x] \left(b + a \sqrt{1 - \sin [c + d x]^2} \right) \\
 & \left(\left((3 + 3 i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1 + i) \sqrt{a} \sqrt{\sin [c + d x]}}{(a^2 - b^2)^{1/4}} \right] - 2 \right. \right. \right. \\
 & \left. \left. \operatorname{ArcTan} \left[1 + \frac{(1 + i) \sqrt{a} \sqrt{\sin [c + d x]}}{(a^2 - b^2)^{1/4}} \right] - \operatorname{Log} \left[\frac{\sqrt{a^2 - b^2} - (1 + i) \sqrt{a}}{(a^2 - b^2)^{1/4} \sqrt{\sin [c + d x]} + i a \sin [c + d x]} \right] \right) \right. \\
 & \left. \left. + \operatorname{Log} \left[\frac{\sqrt{a^2 - b^2} + (1 + i) \sqrt{a}}{\sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\sin [c + d x]} + i a \sin [c + d x]} \right] \right) \right) \Bigg/ \left(\sqrt{a} (a^2 - b^2)^{1/4} \right) + \\
 & \left(56 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \sin [c + d x]^2, \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] \sin [c + d x]^{3/2} \right) \Bigg/ \\
 & \left(\sqrt{1 - \sin [c + d x]^2} \left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \sin [c + d x]^2, \right. \right. \right. \\
 & \left. \left. \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] + 2 \left(2 a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \sin [c + d x]^2, \right. \right. \right. \\
 & \left. \left. \frac{a^2 \sin [c + d x]^2}{a^2 - b^2} \right] + (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \sin [c + d x]^2, \right. \right. \right.
 \end{aligned}$$

$$\left(\left(\frac{a^2 \operatorname{Sin}[c + d x]^2}{a^2 - b^2} \right) \operatorname{Sin}[c + d x]^2 \left(b^2 + a^2 (-1 + \operatorname{Sin}[c + d x]^2) \right) \right) \left((b + a \operatorname{Cos}[c + d x])^2 \operatorname{Csc}[c + d x]^2 \operatorname{Sec}[c + d x]^2 (e \operatorname{Sin}[c + d x])^{5/2} \right. \\ \left. \left(\frac{4 b \operatorname{Sin}[c + d x]}{3 a^3} + \frac{b^2 \operatorname{Sin}[c + d x]}{a^3 (b + a \operatorname{Cos}[c + d x])} - \frac{\operatorname{Sin}[2 (c + d x)]}{5 a^2} \right) \right) \Big/ (d (a + b \operatorname{Sec}[c + d x])^2)$$

Problem 244: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \operatorname{Sin}[c + d x])^{3/2}}{(a + b \operatorname{Sec}[c + d x])^2} dx$$

Optimal (type 4, 882 leaves, 32 steps):

$$\begin{aligned}
 & \frac{b^3 e^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{e \sin[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{2 a^{7/2} (a^2-b^2)^{3/4} d} - \frac{2 b (a^2-b^2)^{1/4} e^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{e \sin[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{a^{7/2} d} + \\
 & \frac{b^3 e^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{e \sin[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{2 a^{7/2} (a^2-b^2)^{3/4} d} - \frac{2 b (a^2-b^2)^{1/4} e^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{e \sin[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{a^{7/2} d} + \\
 & \frac{2 e^2 \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\sin[c+dx]}}{3 a^2 d \sqrt{e \sin[c+dx]}} - \\
 & \frac{5 b^2 e^2 \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\sin[c+dx]}}{a^4 d \sqrt{e \sin[c+dx]}} - \\
 & \frac{b^4 e^2 \operatorname{EllipticPi}\left[\frac{2 a}{a-\sqrt{a^2-b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\sin[c+dx]}}{2 a^4 (a^2-b^2-a \sqrt{a^2-b^2}) d \sqrt{e \sin[c+dx]}} + \\
 & \left(\frac{2 b^2 (a^2-b^2) e^2 \operatorname{EllipticPi}\left[\frac{2 a}{a-\sqrt{a^2-b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\sin[c+dx]}}{a^4 (a^2-b^2-a \sqrt{a^2-b^2}) d \sqrt{e \sin[c+dx]}} \right) / \\
 & \frac{b^4 e^2 \operatorname{EllipticPi}\left[\frac{2 a}{a+\sqrt{a^2-b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\sin[c+dx]}}{2 a^4 (a^2-b^2+a \sqrt{a^2-b^2}) d \sqrt{e \sin[c+dx]}} + \\
 & \left(\frac{2 b^2 (a^2-b^2) e^2 \operatorname{EllipticPi}\left[\frac{2 a}{a+\sqrt{a^2-b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\sin[c+dx]}}{a^4 (a^2-b^2+a \sqrt{a^2-b^2}) d \sqrt{e \sin[c+dx]}} \right) / \\
 & \frac{2 e \cos[c+dx] \sqrt{e \sin[c+dx]}}{3 a^2 d} + \frac{b^2 e \sqrt{e \sin[c+dx]}}{a^3 d (b+a \cos[c+dx])}
 \end{aligned}$$

Result(type 6, 2212 leaves):

$$\begin{aligned}
 & \left((b+a \cos[c+dx])^2 \left(-\frac{2 \cos[c+dx]}{3 a^2} + \frac{b^2}{a^3 (b+a \cos[c+dx])} \right) \right) \\
 & \operatorname{Csc}[c+dx] \operatorname{Sec}[c+dx]^2 (e \sin[c+dx])^{3/2} \Big/ (d (a+b \operatorname{Sec}[c+dx])^2) - \\
 & \frac{1}{6 a^3 d (a+b \operatorname{Sec}[c+dx])^2 \sin[c+dx]^{3/2}} (b+a \cos[c+dx])^2 \operatorname{Sec}[c+dx]^2 (e \sin[c+dx])^{3/2} \\
 & \left(\frac{1}{(b+a \cos[c+dx]) (1-\sin[c+dx])^2} 2 (-2 a^2+3 b^2) \cos[c+dx]^2 (b+a \sqrt{1-\sin[c+dx]})^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(\left(b \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{a} \sqrt{\sin [c+d x]}}{(-a^2+b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{a} \sqrt{\sin [c+d x]}}{(-a^2+b^2)^{1/4}} \right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[\sqrt{-a^2+b^2} - \sqrt{2} \sqrt{a} (-a^2+b^2)^{1/4} \sqrt{\sin [c+d x]} + a \sin [c+d x] \right] + \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[\sqrt{-a^2+b^2} + \sqrt{2} \sqrt{a} (-a^2+b^2)^{1/4} \sqrt{\sin [c+d x]} + a \sin [c+d x] \right] \right) \right) / \\
 & \left(4 \sqrt{2} \sqrt{a} (-a^2+b^2)^{3/4} \right) - \left(5 a (a^2-b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \right. \right. \\
 & \quad \left. \left. \sin [c+d x]^2, \frac{a^2 \sin [c+d x]^2}{a^2-b^2} \right] \sqrt{\sin [c+d x]} \sqrt{1-\sin [c+d x]^2} \right) / \\
 & \left(\left(5 (a^2-b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \sin [c+d x]^2, \frac{a^2 \sin [c+d x]^2}{a^2-b^2} \right] + \right. \right. \\
 & \quad \left. \left(2 a^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \sin [c+d x]^2, \frac{a^2 \sin [c+d x]^2}{a^2-b^2} \right] + (-a^2+b^2) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \sin [c+d x]^2, \frac{a^2 \sin [c+d x]^2}{a^2-b^2} \right] \right) \sin [c+d x]^2 \right) \\
 & \quad \left. \left(b^2+a^2(-1+\sin [c+d x]^2) \right) \right) + \frac{1}{(b+a \cos [c+d x]) \sqrt{1-\sin [c+d x]^2}} \\
 & 8 a b \cos [c+d x] \left(b+a \sqrt{1-\sin [c+d x]^2} \right) \left(-\frac{1}{(a^2-b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{a} \right. \\
 & \quad \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{a} \sqrt{\sin [c+d x]}}{(a^2-b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{a} \sqrt{\sin [c+d x]}}{(a^2-b^2)^{1/4}} \right] \right) + \\
 & \quad \operatorname{Log} \left[\sqrt{a^2-b^2} - (1+i) \sqrt{a} (a^2-b^2)^{1/4} \sqrt{\sin [c+d x]} + i a \sin [c+d x] \right] - \\
 & \quad \left. \operatorname{Log} \left[\sqrt{a^2-b^2} + (1+i) \sqrt{a} (a^2-b^2)^{1/4} \sqrt{\sin [c+d x]} + i a \sin [c+d x] \right] \right) + \\
 & \left(5 b (a^2-b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \sin [c+d x]^2, \frac{a^2 \sin [c+d x]^2}{a^2-b^2} \right] \sqrt{\sin [c+d x]} \right) / \\
 & \left(\sqrt{1-\sin [c+d x]^2} \left(5 (a^2-b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \sin [c+d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{a^2 \sin [c+d x]^2}{a^2-b^2} \right] + 2 \left(2 a^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \sin [c+d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{a^2 \sin [c+d x]^2}{a^2-b^2} \right] + (a^2-b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \sin [c+d x]^2, \right. \right. \\
 & \quad \left. \left. \frac{a^2 \sin [c+d x]^2}{a^2-b^2} \right] \right) \sin [c+d x]^2 \right) \left(b^2+a^2(-1+\sin [c+d x]^2) \right) \right) \left. \right) - \\
 & \frac{1}{(b+a \cos [c+d x]) (1-2 \sin [c+d x]^2) \sqrt{1-\sin [c+d x]^2}} 6 a b \cos [c+d x] \\
 & \cos [2(c+d x)] \left(b+a \sqrt{1-\sin [c+d x]^2} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(\frac{\left(\frac{1}{2} - \frac{i}{2}\right) (a^2 - 2b^2) \operatorname{ArcTan}\left[1 - \frac{(1+i)\sqrt{a}\sqrt{\sin[c+dx]}}{(a^2-b^2)^{1/4}}\right]}{a^{3/2} (a^2 - b^2)^{3/4}} - \right. \\
 & \left. \frac{\left(\frac{1}{2} - \frac{i}{2}\right) (a^2 - 2b^2) \operatorname{ArcTan}\left[1 + \frac{(1+i)\sqrt{a}\sqrt{\sin[c+dx]}}{(a^2-b^2)^{1/4}}\right]}{a^{3/2} (a^2 - b^2)^{3/4}} + \left(\frac{1}{4} - \frac{i}{4}\right) (a^2 - 2b^2) \right. \\
 & \left. \operatorname{Log}\left[\sqrt{a^2 - b^2} - (1+i)\sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\sin[c+dx]} + ia \sin[c+dx]\right] \right) / \\
 & \left(a^{3/2} (a^2 - b^2)^{3/4} - \left(\frac{1}{4} - \frac{i}{4}\right) (a^2 - 2b^2) \operatorname{Log}\left[\sqrt{a^2 - b^2} + (1+i)\sqrt{a} (a^2 - b^2)^{1/4} \right. \right. \\
 & \left. \left. \sqrt{\sin[c+dx]} + ia \sin[c+dx]\right] \right) / \left(a^{3/2} (a^2 - b^2)^{3/4} + \frac{4\sqrt{\sin[c+dx]}}{a} + \right. \\
 & \left. \left(10b (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2 - b^2}\right] \sqrt{\sin[c+dx]} \right) / \right. \\
 & \left. \left(\sqrt{1 - \sin[c+dx]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \sin[c+dx]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{a^2 \sin[c+dx]^2}{a^2 - b^2} \right] + 2 \left(2 a^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \sin[c+dx]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{a^2 \sin[c+dx]^2}{a^2 - b^2} \right] + (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \sin[c+dx]^2, \right. \right. \right. \\
 & \left. \left. \frac{a^2 \sin[c+dx]^2}{a^2 - b^2} \right] \right) \sin[c+dx]^2 \left(b^2 + a^2 (-1 + \sin[c+dx]^2) \right) \right) + \\
 & \left(36b (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2 - b^2}\right] \sin[c+dx]^{5/2} \right) / \\
 & \left(5 \sqrt{1 - \sin[c+dx]^2} \left(9 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \sin[c+dx]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{a^2 \sin[c+dx]^2}{a^2 - b^2} \right] + 2 \left(2 a^2 \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \sin[c+dx]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{a^2 \sin[c+dx]^2}{a^2 - b^2} \right] + (a^2 - b^2) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \sin[c+dx]^2, \right. \right. \right. \\
 & \left. \left. \frac{a^2 \sin[c+dx]^2}{a^2 - b^2} \right] \right) \sin[c+dx]^2 \left(b^2 + a^2 (-1 + \sin[c+dx]^2) \right) \right) \Big) \Big)
 \end{aligned}$$

Problem 245: Result unnecessarily involves higher level functions.

$$\int \frac{\sqrt{e \sin[c+dx]}}{(a+b \sec[c+dx])^2} dx$$

Optimal (type 4, 809 leaves, 27 steps):

$$\frac{b^3 \sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{e \sin[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{2 a^{5/2} (a^2-b^2)^{5/4} d} + \frac{2 b \sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{e \sin[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{a^{5/2} (a^2-b^2)^{1/4} d} -$$

$$\frac{b^3 \sqrt{e} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{e \sin[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{2 a^{5/2} (a^2-b^2)^{5/4} d} - \frac{2 b \sqrt{e} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{e \sin[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{a^{5/2} (a^2-b^2)^{1/4} d} -$$

$$\frac{2 b^2 e \operatorname{EllipticPi}\left[\frac{2 a}{a-\sqrt{a^2-b^2}}, \frac{1}{2} \left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{\sin[c+dx]}}{a^3 \left(a-\sqrt{a^2-b^2}\right) d \sqrt{e \sin[c+dx]}} -$$

$$\frac{b^4 e \operatorname{EllipticPi}\left[\frac{2 a}{a-\sqrt{a^2-b^2}}, \frac{1}{2} \left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{\sin[c+dx]}}{2 a^3 \left(a^2-b^2\right) \left(a-\sqrt{a^2-b^2}\right) d \sqrt{e \sin[c+dx]}} -$$

$$\frac{2 b^2 e \operatorname{EllipticPi}\left[\frac{2 a}{a+\sqrt{a^2-b^2}}, \frac{1}{2} \left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{\sin[c+dx]}}{a^3 \left(a+\sqrt{a^2-b^2}\right) d \sqrt{e \sin[c+dx]}} -$$

$$\frac{b^4 e \operatorname{EllipticPi}\left[\frac{2 a}{a+\sqrt{a^2-b^2}}, \frac{1}{2} \left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{\sin[c+dx]}}{2 a^3 \left(a^2-b^2\right) \left(a+\sqrt{a^2-b^2}\right) d \sqrt{e \sin[c+dx]}} +$$

$$\frac{2 \operatorname{EllipticE}\left[\frac{1}{2} \left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{e \sin[c+dx]}}{a^2 d \sqrt{\sin[c+dx]}} -$$

$$\frac{b^2 \operatorname{EllipticE}\left[\frac{1}{2} \left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{e \sin[c+dx]}}{a^2 \left(a^2-b^2\right) d \sqrt{\sin[c+dx]}} + \frac{b^2 \left(e \sin[c+dx]\right)^{3/2}}{a \left(a^2-b^2\right) d e \left(b+a \cos[c+dx]\right)}$$

Result (type 6, 1248 leaves):

$$\frac{1}{2 a (-a+b) (a+b) d (a+b \operatorname{Sec}[c+dx])^2 \sqrt{\sin[c+dx]}} \frac{(b+a \cos[c+dx])^2 \operatorname{Sec}[c+dx]^2 \sqrt{e \sin[c+dx]}}{\left(\frac{1}{(b+a \cos[c+dx]) (1-\sin[c+dx])^2} 2 (-2 a^2+3 b^2) \cos[c+dx]^2 \left(b+a \sqrt{1-\sin[c+dx]^2}\right)\right.}$$

$$\left.\left(\left(b\left(-2 \operatorname{ArcTan}\left[1-\frac{\sqrt{2} \sqrt{a} \sqrt{\sin[c+dx]}}{(-a^2+b^2)^{1/4}}\right]+2 \operatorname{ArcTan}\left[1+\frac{\sqrt{2} \sqrt{a} \sqrt{\sin[c+dx]}}{(-a^2+b^2)^{1/4}}\right]\right)+\right.\right.$$

$$\left.\left.\operatorname{Log}\left[\sqrt{-a^2+b^2}-\sqrt{2} \sqrt{a}(-a^2+b^2)^{1/4} \sqrt{\sin[c+dx]}+a \sin[c+dx]\right]-\right.\right.$$

$$\left.\left.\operatorname{Log}\left[\sqrt{-a^2+b^2}+\sqrt{2} \sqrt{a}(-a^2+b^2)^{1/4} \sqrt{\sin[c+dx]}+a \sin[c+dx]\right]\right)\right) /$$

$$\left(4 \sqrt{2} a^{3/2}(-a^2+b^2)^{1/4}\right)-\left(7 a\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{4},-\frac{1}{2}, 1, \frac{7}{4},\right.\right.$$

$$\begin{aligned}
 & \left. \left(\frac{\sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2-b^2}}{\sin[c+dx]^{3/2} \sqrt{1-\sin[c+dx]^2}} \right) / \right. \\
 & \left(3 \left(7 (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2-b^2} \right] + \right. \right. \\
 & \quad \left. 2 \left(2 a^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2-b^2} \right] + \right. \right. \\
 & \quad \quad \left. \left. (-a^2+b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2-b^2} \right] \right) \right) \\
 & \quad \left. \left. \sin[c+dx]^2 \right) (b^2+a^2(-1+\sin[c+dx]^2)) \right) \Bigg) + \\
 & \frac{1}{6 (b+a \cos[c+dx]) \sqrt{1-\sin[c+dx]^2}} a b \cos[c+dx] (b+a \sqrt{1-\sin[c+dx]^2}) \\
 & \left(\left((3+3i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{a} \sqrt{\sin[c+dx]}}{(a^2-b^2)^{1/4}} \right] - \right. \right. \right. \\
 & \quad \left. 2 \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{a} \sqrt{\sin[c+dx]}}{(a^2-b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{a^2-b^2} - \right. \right. \\
 & \quad \left. \left. (1+i) \sqrt{a} (a^2-b^2)^{1/4} \sqrt{\sin[c+dx]} + i a \sin[c+dx] \right] + \operatorname{Log} \left[\sqrt{a^2-b^2} + \right. \right. \\
 & \quad \left. \left. (1+i) \sqrt{a} (a^2-b^2)^{1/4} \sqrt{\sin[c+dx]} + i a \sin[c+dx] \right] \right) \Bigg) / \left(\sqrt{a} (a^2-b^2)^{1/4} \right) + \\
 & \left(56 b (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \sin[c+dx]^2, \frac{a^2 \sin[c+dx]^2}{a^2-b^2} \right] \sin[c+dx]^{3/2} \right) / \\
 & \left(\sqrt{1-\sin[c+dx]^2} \left(7 (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \sin[c+dx]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{a^2 \sin[c+dx]^2}{a^2-b^2} \right] + 2 \left(2 a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \sin[c+dx]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{a^2 \sin[c+dx]^2}{a^2-b^2} \right] + (a^2-b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \sin[c+dx]^2, \right. \right. \\
 & \quad \left. \left. \frac{a^2 \sin[c+dx]^2}{a^2-b^2} \right] \right) \sin[c+dx]^2 \right) (b^2+a^2(-1+\sin[c+dx]^2)) \Bigg) \Bigg) + \\
 & \frac{b^2 (b+a \cos[c+dx]) \operatorname{Sec}[c+dx] \sqrt{e \sin[c+dx]} \operatorname{Tan}[c+dx]}{a (a^2-b^2) d (a+b \operatorname{Sec}[c+dx])^2}
 \end{aligned}$$

Problem 246: Result unnecessarily involves higher level functions.

$$\int \frac{1}{(a+b \operatorname{Sec}[c+dx])^2 \sqrt{e \sin[c+dx]}} dx$$

Optimal (type 4, 838 leaves, 27 steps):

$$\begin{aligned}
 & - \frac{3 b^3 \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c+d x]}}{\left(a^2-b^2\right)^{1/4} \sqrt{e}}\right]}{2 a^{3/2}\left(a^2-b^2\right)^{7/4} d \sqrt{e}} - \frac{2 b \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c+d x]}}{\left(a^2-b^2\right)^{1/4} \sqrt{e}}\right]}{a^{3/2}\left(a^2-b^2\right)^{3/4} d \sqrt{e}} - \\
 & \frac{3 b^3 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c+d x]}}{\left(a^2-b^2\right)^{1/4} \sqrt{e}}\right]}{2 a^{3/2}\left(a^2-b^2\right)^{7/4} d \sqrt{e}} - \frac{2 b \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c+d x]}}{\left(a^2-b^2\right)^{1/4} \sqrt{e}}\right]}{a^{3/2}\left(a^2-b^2\right)^{3/4} d \sqrt{e}} + \\
 & \frac{2 \operatorname{EllipticF}\left[\frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{\operatorname{Sin}[c+d x]}}{a^2 d \sqrt{e \operatorname{Sin}[c+d x]}} + \frac{b^2 \operatorname{EllipticF}\left[\frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{\operatorname{Sin}[c+d x]}}{a^2\left(a^2-b^2\right) d \sqrt{e \operatorname{Sin}[c+d x]}} + \\
 & \frac{2 b^2 \operatorname{EllipticPi}\left[\frac{-2 a}{a-\sqrt{a^2-b^2}}, \frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{\operatorname{Sin}[c+d x]}}{a^2\left(a^2-b^2-a \sqrt{a^2-b^2}\right) d \sqrt{e \operatorname{Sin}[c+d x]}} + \\
 & \frac{3 b^4 \operatorname{EllipticPi}\left[\frac{-2 a}{a-\sqrt{a^2-b^2}}, \frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{\operatorname{Sin}[c+d x]}}{2 a^2\left(a^2-b^2\right)\left(a^2-b^2-a \sqrt{a^2-b^2}\right) d \sqrt{e \operatorname{Sin}[c+d x]}} + \\
 & \frac{2 b^2 \operatorname{EllipticPi}\left[\frac{-2 a}{a+\sqrt{a^2-b^2}}, \frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{\operatorname{Sin}[c+d x]}}{a^2\left(a^2-b^2+a \sqrt{a^2-b^2}\right) d \sqrt{e \operatorname{Sin}[c+d x]}} + \\
 & \frac{3 b^4 \operatorname{EllipticPi}\left[\frac{-2 a}{a+\sqrt{a^2-b^2}}, \frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{\operatorname{Sin}[c+d x]}}{2 a^2\left(a^2-b^2\right)\left(a^2-b^2+a \sqrt{a^2-b^2}\right) d \sqrt{e \operatorname{Sin}[c+d x]}} + \frac{b^2 \sqrt{e \operatorname{Sin}[c+d x]}}{a\left(a^2-b^2\right) d e\left(b+a \operatorname{Cos}[c+d x]\right)}
 \end{aligned}$$

Result (type 6, 1246 leaves):

$$\begin{aligned}
 & \frac{1}{2 a(-a+b)(a+b) d(a+b \operatorname{Sec}[c+d x])^2 \sqrt{e \operatorname{Sin}[c+d x]}} \\
 & \frac{(b+a \operatorname{Cos}[c+d x])^2 \operatorname{Sec}[c+d x]^2 \sqrt{\operatorname{Sin}[c+d x]}}{\left(\frac{1}{(b+a \operatorname{Cos}[c+d x])\left(1-\operatorname{Sin}[c+d x]\right)^2} 2\left(-2 a^2+b^2\right) \operatorname{Cos}[c+d x]^2\left(b+a \sqrt{1-\operatorname{Sin}[c+d x]^2}\right)\right.} \\
 & \left.\left(\left(b\left(-2 \operatorname{ArcTan}\left[1-\frac{\sqrt{2} \sqrt{a} \sqrt{\operatorname{Sin}[c+d x]}}{\left(-a^2+b^2\right)^{1/4}}\right]+2 \operatorname{ArcTan}\left[1+\frac{\sqrt{2} \sqrt{a} \sqrt{\operatorname{Sin}[c+d x]}}{\left(-a^2+b^2\right)^{1/4}}\right]\right)-\right. \right. \\
 & \left. \left.\operatorname{Log}\left[\sqrt{-a^2+b^2}-\sqrt{2} \sqrt{a}\left(-a^2+b^2\right)^{1/4} \sqrt{\operatorname{Sin}[c+d x]}+a \operatorname{Sin}[c+d x]\right]+\right. \right. \\
 & \left. \left.\operatorname{Log}\left[\sqrt{-a^2+b^2}+\sqrt{2} \sqrt{a}\left(-a^2+b^2\right)^{1/4} \sqrt{\operatorname{Sin}[c+d x]}+a \operatorname{Sin}[c+d x]\right]\right)\right) / \\
 & \left(4 \sqrt{2} \sqrt{a}\left(-a^2+b^2\right)^{3/4}\right)-\left(5 a\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{4},-\frac{1}{2}, 1, \frac{5}{4},\right.\right. \\
 & \left.\left.\operatorname{Sin}[c+d x]^2, \frac{a^2 \operatorname{Sin}[c+d x]^2}{a^2-b^2}\right] \sqrt{\operatorname{Sin}[c+d x]} \sqrt{1-\operatorname{Sin}[c+d x]^2}\right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(\left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \sin[c + dx]^2, \frac{a^2 \sin[c + dx]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \quad 2 \left(2 a^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \sin[c + dx]^2, \frac{a^2 \sin[c + dx]^2}{a^2 - b^2} \right] + (-a^2 + b^2) \right. \\
 & \quad \quad \left. \left. \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \sin[c + dx]^2, \frac{a^2 \sin[c + dx]^2}{a^2 - b^2} \right] \right) \sin[c + dx]^2 \right) \\
 & \quad \left. \left. \left. (b^2 + a^2 (-1 + \sin[c + dx]^2)) \right) \right) \right) + \frac{1}{(b + a \cos[c + dx]) \sqrt{1 - \sin[c + dx]^2}} \\
 & 4 a b \cos[c + dx] \left(b + a \sqrt{1 - \sin[c + dx]^2} \right) \left(-\frac{1}{(a^2 - b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{a} \right. \\
 & \quad \left(2 \operatorname{ArcTan} \left[1 - \frac{(1 + i) \sqrt{a} \sqrt{\sin[c + dx]}}{(a^2 - b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[1 + \frac{(1 + i) \sqrt{a} \sqrt{\sin[c + dx]}}{(a^2 - b^2)^{1/4}} \right] \right) + \\
 & \quad \left(\log \left[\sqrt{a^2 - b^2} - (1 + i) \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\sin[c + dx]} + i a \sin[c + dx] \right] - \right. \\
 & \quad \left. \log \left[\sqrt{a^2 - b^2} + (1 + i) \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\sin[c + dx]} + i a \sin[c + dx] \right] \right) + \\
 & \quad \left(5 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \sin[c + dx]^2, \frac{a^2 \sin[c + dx]^2}{a^2 - b^2} \right] \sqrt{\sin[c + dx]} \right) / \\
 & \quad \left(\sqrt{1 - \sin[c + dx]^2} \right) \\
 & \quad \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \sin[c + dx]^2, \frac{a^2 \sin[c + dx]^2}{a^2 - b^2} \right] + \right. \\
 & \quad 2 \left(2 a^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \sin[c + dx]^2, \frac{a^2 \sin[c + dx]^2}{a^2 - b^2} \right] + (a^2 - b^2) \right. \\
 & \quad \quad \left. \left. \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \sin[c + dx]^2, \frac{a^2 \sin[c + dx]^2}{a^2 - b^2} \right] \right) \sin[c + dx]^2 \right) \\
 & \quad \left. \left. \left. (b^2 + a^2 (-1 + \sin[c + dx]^2)) \right) \right) \right) \right) + \frac{b^2 (b + a \cos[c + dx]) \sec[c + dx] \tan[c + dx]}{a (a^2 - b^2) d (a + b \sec[c + dx])^2 \sqrt{e \sin[c + dx]}}
 \end{aligned}$$

Problem 247: Result unnecessarily involves higher level functions.

$$\int \frac{1}{(a + b \sec[c + dx])^2 (e \sin[c + dx])^{3/2}} dx$$

Optimal (type 4, 1054 leaves, 33 steps):

$$\begin{aligned}
 & \frac{5 b^3 \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c+d x]}}{\left(a^2-b^2\right)^{1 / 4} \sqrt{e}}\right]}{2 \sqrt{a}\left(a^2-b^2\right)^{9 / 4} d e^{3 / 2}}+\frac{2 b \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c+d x]}}{\left(a^2-b^2\right)^{1 / 4} \sqrt{e}}\right]}{\sqrt{a}\left(a^2-b^2\right)^{5 / 4} d e^{3 / 2}}- \\
 & \frac{5 b^3 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c+d x]}}{\left(a^2-b^2\right)^{1 / 4} \sqrt{e}}\right]}{2 \sqrt{a}\left(a^2-b^2\right)^{9 / 4} d e^{3 / 2}}-\frac{2 b \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{e \operatorname{Sin}[c+d x]}}{\left(a^2-b^2\right)^{1 / 4} \sqrt{e}}\right]}{\sqrt{a}\left(a^2-b^2\right)^{5 / 4} d e^{3 / 2}}- \\
 & \frac{2 \operatorname{Cos}[c+d x]}{a^2 d e \sqrt{e \operatorname{Sin}[c+d x]}}+\frac{b^2}{a\left(a^2-b^2\right) d e\left(b+a \operatorname{Cos}[c+d x]\right) \sqrt{e \operatorname{Sin}[c+d x]}}+ \\
 & \frac{4 b\left(a-b \operatorname{Cos}[c+d x]\right)}{a^2\left(a^2-b^2\right) d e \sqrt{e \operatorname{Sin}[c+d x]}}+\frac{b^2\left(5 a b-\left(3 a^2+2 b^2\right) \operatorname{Cos}[c+d x]\right)}{a^2\left(a^2-b^2\right)^2 d e \sqrt{e \operatorname{Sin}[c+d x]}}- \\
 & \frac{5 b^4 \operatorname{EllipticPi}\left[\frac{-2 a}{a-\sqrt{a^2-b^2}}, \frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{\operatorname{Sin}[c+d x]}}{2 a\left(a^2-b^2\right)^2\left(a-\sqrt{a^2-b^2}\right) d e \sqrt{e \operatorname{Sin}[c+d x]}}- \\
 & \frac{2 b^2 \operatorname{EllipticPi}\left[\frac{-2 a}{a-\sqrt{a^2-b^2}}, \frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{\operatorname{Sin}[c+d x]}}{a\left(a^2-b^2\right)\left(a-\sqrt{a^2-b^2}\right) d e \sqrt{e \operatorname{Sin}[c+d x]}}- \\
 & \frac{5 b^4 \operatorname{EllipticPi}\left[\frac{-2 a}{a+\sqrt{a^2-b^2}}, \frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{\operatorname{Sin}[c+d x]}}{2 a\left(a^2-b^2\right)^2\left(a+\sqrt{a^2-b^2}\right) d e \sqrt{e \operatorname{Sin}[c+d x]}}- \\
 & \frac{2 b^2 \operatorname{EllipticPi}\left[\frac{-2 a}{a+\sqrt{a^2-b^2}}, \frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{\operatorname{Sin}[c+d x]}}{a\left(a^2-b^2\right)\left(a+\sqrt{a^2-b^2}\right) d e \sqrt{e \operatorname{Sin}[c+d x]}}- \\
 & \frac{2 \operatorname{EllipticE}\left[\frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{e \operatorname{Sin}[c+d x]}}{a^2 d e^2 \sqrt{\operatorname{Sin}[c+d x]}}- \\
 & \frac{4 b^2 \operatorname{EllipticE}\left[\frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{e \operatorname{Sin}[c+d x]}}{a^2\left(a^2-b^2\right) d e^2 \sqrt{\operatorname{Sin}[c+d x]}}- \\
 & \frac{b^2\left(3 a^2+2 b^2\right) \operatorname{EllipticE}\left[\frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{e \operatorname{Sin}[c+d x]}}{a^2\left(a^2-b^2\right)^2 d e^2 \sqrt{\operatorname{Sin}[c+d x]}}
 \end{aligned}$$

Result (type 6, 1316 leaves):

$$\begin{aligned}
 & -\frac{1}{2\left(a-b\right)^2\left(a+b\right)^2 d\left(a+b \operatorname{Sec}[c+d x]\right)^2\left(e \operatorname{Sin}[c+d x]\right)^{3 / 2}} \\
 & \left(b+a \operatorname{Cos}[c+d x]\right)^2 \operatorname{Sec}[c+d x]^2 \operatorname{Sin}[c+d x]^{3 / 2} \\
 & \left(\frac{1}{\left(b+a \operatorname{Cos}[c+d x]\right)\left(1-\operatorname{Sin}[c+d x]\right)^2}\right) 2\left(2 a^3+3 a b^2\right) \operatorname{Cos}[c+d x]^2\left(b+a \sqrt{1-\operatorname{Sin}[c+d x]}\right)^2
 \end{aligned}$$

$$\begin{aligned}
 & \left(\left(b \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{a} \sqrt{\sin [c+d x]}}{(-a^2+b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{a} \sqrt{\sin [c+d x]}}{(-a^2+b^2)^{1/4}} \right] + \operatorname{Log} \left[\right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{-a^2+b^2} - \sqrt{2} \sqrt{a} (-a^2+b^2)^{1/4} \sqrt{\sin [c+d x]} + a \sin [c+d x] \right] - \operatorname{Log} \left[\right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{-a^2+b^2} + \sqrt{2} \sqrt{a} (-a^2+b^2)^{1/4} \sqrt{\sin [c+d x]} + a \sin [c+d x] \right] \right) \right) / \\
 & \quad \left(4 \sqrt{2} a^{3/2} (-a^2+b^2)^{1/4} \right) - \left(7 a (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \right. \right. \\
 & \quad \left. \left. \sin [c+d x]^2, \frac{a^2 \sin [c+d x]^2}{a^2-b^2} \right] \sin [c+d x]^{3/2} \sqrt{1-\sin [c+d x]^2} \right) / \\
 & \quad \left(3 \left(7 (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \sin [c+d x]^2, \frac{a^2 \sin [c+d x]^2}{a^2-b^2} \right] + 2 \right. \right. \\
 & \quad \left. \left(2 a^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \sin [c+d x]^2, \frac{a^2 \sin [c+d x]^2}{a^2-b^2} \right] + \right. \right. \\
 & \quad \left. \left. (-a^2+b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \sin [c+d x]^2, \frac{a^2 \sin [c+d x]^2}{a^2-b^2} \right] \right) \right) \\
 & \quad \left. \sin [c+d x]^2 \right) (b^2+a^2(-1+\sin [c+d x]^2)) \Big) + \\
 & \frac{1}{12 (b+a \cos [c+d x]) \sqrt{1-\sin [c+d x]^2}} (6 a^2 b+4 b^3) \cos [c+d x] \\
 & \quad (b+a \sqrt{1-\sin [c+d x]^2}) \\
 & \quad \left(\left((3+3 i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{a} \sqrt{\sin [c+d x]}}{(a^2-b^2)^{1/4}} \right] - 2 \right. \right. \right. \\
 & \quad \left. \left. \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{a} \sqrt{\sin [c+d x]}}{(a^2-b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{a^2-b^2} - (1+i) \sqrt{a} \right. \right. \right. \\
 & \quad \left. \left. (a^2-b^2)^{1/4} \sqrt{\sin [c+d x]} + i a \sin [c+d x] \right] + \operatorname{Log} \left[\sqrt{a^2-b^2} + (1+i) \right. \right. \\
 & \quad \left. \left. \sqrt{a} (a^2-b^2)^{1/4} \sqrt{\sin [c+d x]} + i a \sin [c+d x] \right] \right) \right) / \left(\sqrt{a} (a^2-b^2)^{1/4} + \right. \\
 & \quad \left. \left(56 b (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \sin [c+d x]^2, \frac{a^2 \sin [c+d x]^2}{a^2-b^2} \right] \sin [c+d x]^{3/2} \right) / \right. \\
 & \quad \left(\sqrt{1-\sin [c+d x]^2} \left(7 (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \sin [c+d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{a^2 \sin [c+d x]^2}{a^2-b^2} \right] + 2 \left(2 a^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \sin [c+d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{a^2 \sin [c+d x]^2}{a^2-b^2} \right] + (a^2-b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \sin [c+d x]^2, \right. \right. \\
 & \quad \left. \left. \frac{a^2 \sin [c+d x]^2}{a^2-b^2} \right] \right) \sin [c+d x]^2 \right) (b^2+a^2(-1+\sin [c+d x]^2)) \Big) \Big) +
 \end{aligned}$$

$$\left((b + a \cos [c + d x])^2 \left(-\frac{2 (-2 a b + a^2 \cos [c + d x] + b^2 \cos [c + d x]) \operatorname{Csc}[c + d x]}{(-a^2 + b^2)^2} + \frac{a b^2 \sin [c + d x]}{(-a^2 + b^2)^2 (b + a \cos [c + d x])} \right) \right) \operatorname{Tan}[c + d x]^2 \Big/ \left(d (a + b \operatorname{Sec}[c + d x])^2 (e \sin [c + d x])^{3/2} \right)$$

Problem 248: Result unnecessarily involves higher level functions.

$$\int \frac{1}{(a + b \operatorname{Sec}[c + d x])^2 (e \sin [c + d x])^{5/2}} dx$$

Optimal (type 4, 1089 leaves, 33 steps):

$$\begin{aligned}
 & - \frac{7 \sqrt{a} b^3 \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{e \sin[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{2 (a^2-b^2)^{11/4} d e^{5/2}} - \frac{2 \sqrt{a} b \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{e \sin[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{(a^2-b^2)^{7/4} d e^{5/2}} - \\
 & \frac{7 \sqrt{a} b^3 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{e \sin[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{2 (a^2-b^2)^{11/4} d e^{5/2}} - \frac{2 \sqrt{a} b \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{e \sin[c+dx]}}{(a^2-b^2)^{1/4} \sqrt{e}}\right]}{(a^2-b^2)^{7/4} d e^{5/2}} - \\
 & \frac{2 \operatorname{Cos}[c+dx]}{3 a^2 d e (e \sin[c+dx])^{3/2}} + \frac{b^2}{a (a^2-b^2) d e (b+a \operatorname{Cos}[c+dx]) (e \sin[c+dx])^{3/2}} + \\
 & \frac{4 b (a-b \operatorname{Cos}[c+dx])}{3 a^2 (a^2-b^2) d e (e \sin[c+dx])^{3/2}} + \frac{b^2 (7 a b - (5 a^2 + 2 b^2) \operatorname{Cos}[c+dx])}{3 a^2 (a^2-b^2)^2 d e (e \sin[c+dx])^{3/2}} + \\
 & \frac{2 \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\sin[c+dx]}}{3 a^2 d e^2 \sqrt{e \sin[c+dx]}} + \frac{4 b^2 \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\sin[c+dx]}}{3 a^2 (a^2-b^2) d e^2 \sqrt{e \sin[c+dx]}} + \\
 & \frac{b^2 (5 a^2 + 2 b^2) \operatorname{EllipticF}\left[\frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\sin[c+dx]}}{3 a^2 (a^2-b^2)^2 d e^2 \sqrt{e \sin[c+dx]}} + \\
 & \frac{7 b^4 \operatorname{EllipticPi}\left[\frac{-2 a}{a-\sqrt{a^2-b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\sin[c+dx]}}{2 (a^2-b^2)^2 (a^2-b^2-a \sqrt{a^2-b^2}) d e^2 \sqrt{e \sin[c+dx]}} + \\
 & \frac{2 b^2 \operatorname{EllipticPi}\left[\frac{-2 a}{a-\sqrt{a^2-b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\sin[c+dx]}}{(a^2-b^2) (a^2-b^2-a \sqrt{a^2-b^2}) d e^2 \sqrt{e \sin[c+dx]}} + \\
 & \frac{7 b^4 \operatorname{EllipticPi}\left[\frac{-2 a}{a+\sqrt{a^2-b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\sin[c+dx]}}{2 (a^2-b^2)^2 (a^2-b^2+a \sqrt{a^2-b^2}) d e^2 \sqrt{e \sin[c+dx]}} + \\
 & \frac{2 b^2 \operatorname{EllipticPi}\left[\frac{-2 a}{a+\sqrt{a^2-b^2}}, \frac{1}{2} \left(c - \frac{\pi}{2} + dx\right), 2\right] \sqrt{\sin[c+dx]}}{(a^2-b^2) (a^2-b^2+a \sqrt{a^2-b^2}) d e^2 \sqrt{e \sin[c+dx]}}
 \end{aligned}$$

Result (type 6, 1320 leaves):

$$\begin{aligned}
 & - \frac{1}{6 (a-b)^2 (a+b)^2 d (a+b \operatorname{Sec}[c+dx])^2 (e \sin[c+dx])^{5/2}} \\
 & (b+a \operatorname{Cos}[c+dx])^2 \operatorname{Sec}[c+dx]^2 \sin[c+dx]^{5/2} \left(\frac{1}{(b+a \operatorname{Cos}[c+dx]) (1-\sin[c+dx])^2} \right. \\
 & \left. 2 (-2 a^3 - 5 a b^2) \operatorname{Cos}[c+dx]^2 \left(b+a \sqrt{1-\sin[c+dx]^2} \right) \right. \\
 & \left. \left(\left(b \left(-2 \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{a} \sqrt{\sin[c+dx]}}{(-a^2+b^2)^{1/4}}\right] + 2 \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{a} \sqrt{\sin[c+dx]}}{(-a^2+b^2)^{1/4}}\right] \right) - \operatorname{Log}\left[\right. \right. \right. \\
 & \left. \left. \left. \sqrt{-a^2+b^2} - \sqrt{2} \sqrt{a} (-a^2+b^2)^{1/4} \sqrt{\sin[c+dx]} + a \sin[c+dx] \right] + \operatorname{Log}\left[\right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \sqrt{-a^2 + b^2} + \sqrt{2} \sqrt{a} (-a^2 + b^2)^{1/4} \sqrt{\sin[c + dx]} + a \sin[c + dx] \right) \right) \right) / \\
 & \left(4 \sqrt{2} \sqrt{a} (-a^2 + b^2)^{3/4} \right) - \left(5 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \right. \right. \\
 & \left. \left. \sin[c + dx]^2, \frac{a^2 \sin[c + dx]^2}{a^2 - b^2} \right] \sqrt{\sin[c + dx]} \sqrt{1 - \sin[c + dx]^2} \right) / \\
 & \left(\left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \sin[c + dx]^2, \frac{a^2 \sin[c + dx]^2}{a^2 - b^2} \right] + 2 \right. \right. \\
 & \left. \left(2 a^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \sin[c + dx]^2, \frac{a^2 \sin[c + dx]^2}{a^2 - b^2} \right] + \right. \right. \\
 & \left. \left. (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \sin[c + dx]^2, \frac{a^2 \sin[c + dx]^2}{a^2 - b^2} \right] \right) \right) \right) \\
 & \left. \left. \left. \sin[c + dx]^2 \right) (b^2 + a^2 (-1 + \sin[c + dx]^2)) \right) \right) \right) + \\
 & \frac{1}{(b + a \cos[c + dx]) \sqrt{1 - \sin[c + dx]^2}} 2 (10 a^2 b + 4 b^3) \cos[c + dx] \\
 & \left(b + a \sqrt{1 - \sin[c + dx]^2} \right) \\
 & \left(-\frac{1}{(a^2 - b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{a} \left(2 \operatorname{ArcTan} \left[1 - \frac{(1 + i) \sqrt{a} \sqrt{\sin[c + dx]}}{(a^2 - b^2)^{1/4}} \right] - \right. \right. \\
 & \left. \left. 2 \operatorname{ArcTan} \left[1 + \frac{(1 + i) \sqrt{a} \sqrt{\sin[c + dx]}}{(a^2 - b^2)^{1/4}} \right] + \right. \right. \\
 & \left. \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} - (1 + i) \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\sin[c + dx]} + i a \sin[c + dx] \right] - \right. \right. \\
 & \left. \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} + (1 + i) \sqrt{a} (a^2 - b^2)^{1/4} \sqrt{\sin[c + dx]} + i a \sin[c + dx] \right] \right) \right) + \\
 & \left(5 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \sin[c + dx]^2, \frac{a^2 \sin[c + dx]^2}{a^2 - b^2} \right] \sqrt{\sin[c + dx]} \right) / \\
 & \left(\sqrt{1 - \sin[c + dx]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \sin[c + dx]^2, \right. \right. \right. \\
 & \left. \left. \frac{a^2 \sin[c + dx]^2}{a^2 - b^2} \right] + 2 \left(2 a^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \sin[c + dx]^2, \right. \right. \right. \\
 & \left. \left. \frac{a^2 \sin[c + dx]^2}{a^2 - b^2} \right] + (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \sin[c + dx]^2, \right. \right. \\
 & \left. \left. \frac{a^2 \sin[c + dx]^2}{a^2 - b^2} \right] \right) \sin[c + dx]^2 \right) (b^2 + a^2 (-1 + \sin[c + dx]^2)) \right) \right) \right) + \\
 & \left((b + a \cos[c + dx])^2 \left(\frac{a b^2}{(-a^2 + b^2)^2 (b + a \cos[c + dx])} - \right. \right.
 \end{aligned}$$

$$\frac{2 \left(-2 a b + a^2 \cos [c + d x] + b^2 \cos [c + d x] \right) \operatorname{Csc} [c + d x]^2}{3 \left(-a^2 + b^2 \right)^2} \left(\operatorname{Sin} [c + d x] \operatorname{Tan} [c + d x]^2 \right) / \left(d \left(a + b \operatorname{Sec} [c + d x] \right)^2 \right. \\ \left. \left(e \operatorname{Sin} [c + d x] \right)^{5/2} \right)$$

Problem 249: Unable to integrate problem.

$$\int \sqrt{a + b \operatorname{Sec} [e + f x]} dx$$

Optimal (type 4, 125 leaves, 1 step):

$$-\frac{1}{\sqrt{a+b} f} 2 \operatorname{Cot} [e + f x] \operatorname{EllipticPi} \left[\frac{a}{a+b}, \operatorname{ArcSin} \left[\frac{\sqrt{a+b}}{\sqrt{a+b \operatorname{Sec} [e + f x]}} \right], \frac{a-b}{a+b} \right] \\ \sqrt{-\frac{b(1-\operatorname{Sec} [e + f x])}{a+b \operatorname{Sec} [e + f x]}} \sqrt{\frac{b(1+\operatorname{Sec} [e + f x])}{a+b \operatorname{Sec} [e + f x]}} (a + b \operatorname{Sec} [e + f x])$$

Result (type 8, 16 leaves):

$$\int \sqrt{a + b \operatorname{Sec} [e + f x]} dx$$

Problem 251: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int (a + b \operatorname{Sec} [e + f x])^{3/2} dx$$

Optimal (type 4, 309 leaves, 5 steps):

$$\begin{aligned}
 & -\frac{1}{f} (a-b) \sqrt{a+b} \operatorname{Cot}[e+fx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[e+fx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\operatorname{Sec}[e+fx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[e+fx])}{a-b}} + \frac{1}{f} \\
 & 2(2a-b) \sqrt{a+b} \operatorname{Cot}[e+fx] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[e+fx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\operatorname{Sec}[e+fx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[e+fx])}{a-b}} - \frac{1}{f} \\
 & 2a \sqrt{a+b} \operatorname{Cot}[e+fx] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[e+fx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\operatorname{Sec}[e+fx])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[e+fx])}{a-b}}
 \end{aligned}$$

Result (type 4, 882 leaves):

$$\begin{aligned}
 & \frac{2b \operatorname{Cos}[e+fx] (a+b \operatorname{Sec}[e+fx])^{3/2} \operatorname{Sin}[e+fx]}{f(b+a \operatorname{Cos}[e+fx])} + \\
 & \left(2(a+b \operatorname{Sec}[e+fx])^{3/2} \left(ab \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] + \right. \right. \\
 & b^2 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right] - 2ab \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^3 + \\
 & ab \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^5 - b^2 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^5 + \\
 & \left. \left. 2ia^2 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right], \frac{a+b}{a-b}\right] \right. \right. \\
 & \left. \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}} + \right. \\
 & \left. \left. 2ia^2 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right], \frac{a+b}{a-b}\right] \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2 \right. \right. \\
 & \left. \left. \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2}{a+b}} - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & i (a-b) b \text{EllipticE}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(e+fx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1-\tan\left[\frac{1}{2}(e+fx)\right]^2} \\
 & \left(1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right) \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(e+fx)\right]^2+b \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}} - \\
 & i (a-b)^2 \text{EllipticF}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(e+fx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1-\tan\left[\frac{1}{2}(e+fx)\right]^2} \\
 & \left(1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right) \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(e+fx)\right]^2+b \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}} \right) \Bigg) / \\
 & \left(\sqrt{\frac{-a+b}{a+b}} f (b+a \cos[e+fx])^{3/2} \sec[e+fx]^{3/2} \sqrt{\frac{1}{1-\tan\left[\frac{1}{2}(e+fx)\right]^2}} \right. \\
 & \left. \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right) \left(1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)^{3/2} \right. \\
 & \left. \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(e+fx)\right]^2+b \tan\left[\frac{1}{2}(e+fx)\right]^2}{1+\tan\left[\frac{1}{2}(e+fx)\right]^2}} \right)
 \end{aligned}$$

Problem 253: Unable to integrate problem.

$$\int \frac{1}{\sqrt{a+b \sec[e+fx]}} dx$$

Optimal (type 4, 106 leaves, 1 step):

$$\begin{aligned}
 & -\frac{1}{af} 2\sqrt{a+b} \cot[e+fx] \text{EllipticPi}\left[\frac{a+b}{a}, \text{ArcSin}\left[\frac{\sqrt{a+b \sec[e+fx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\sec[e+fx])}{a+b}} \sqrt{-\frac{b(1+\sec[e+fx])}{a-b}}
 \end{aligned}$$

Result (type 8, 16 leaves):

$$\int \frac{1}{\sqrt{a+b \sec[e+fx]}} dx$$

Problem 255: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{1}{(a + b \operatorname{Sec}[e + f x])^{3/2}} dx$$

Optimal (type 4, 347 leaves, 6 steps):

$$\frac{1}{a \sqrt{a+b} f} 2 \operatorname{Cot}[e + f x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[e + f x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ + \sqrt{\frac{b(1-\operatorname{Sec}[e + f x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[e + f x])}{a-b}} - \frac{1}{a \sqrt{a+b} f} 2 \operatorname{Cot}[e + f x] \\ \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[e + f x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[e + f x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[e + f x])}{a-b}} - \\ \frac{1}{a^2 f} 2 \sqrt{a+b} \operatorname{Cot}[e + f x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[e + f x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ + \sqrt{\frac{b(1-\operatorname{Sec}[e + f x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[e + f x])}{a-b}} + \frac{2 b^2 \operatorname{Tan}[e + f x]}{a(a^2 - b^2) f \sqrt{a+b \operatorname{Sec}[e + f x]}}$$

Result (type 4, 1249 leaves):

$$\frac{(b + a \operatorname{Cos}[e + f x])^2 \operatorname{Sec}[e + f x]^2 \left(\frac{2 b \operatorname{Sin}[e + f x]}{a(-a^2 + b^2)} + \frac{2 b^2 \operatorname{Sin}[e + f x]}{a(a^2 - b^2)(b + a \operatorname{Cos}[e + f x])} \right)}{f (a + b \operatorname{Sec}[e + f x])^{3/2}} + \\ \left(2 (b + a \operatorname{Cos}[e + f x])^{3/2} \operatorname{Sec}[e + f x]^{3/2} \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}} \right. \\ \left. \left(a b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] + b^2 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] - 2 a b \sqrt{\frac{-a+b}{a+b}} \right. \right. \\ \left. \left. \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^3 + a b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^5 - b^2 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^5 - \right. \right. \\ \left. \left. 2 i a^2 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]\right], \frac{a+b}{a-b}\right] \right. \right. \\ \left. \left. \sqrt{1 - \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2} \sqrt{\frac{a + b - a \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2 + b \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]^2}{a+b}} \right) \right. \\ \left. \right)$$

$$\begin{aligned}
 & 2 i b^2 \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(e+fx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1-\tan\left[\frac{1}{2}(e+fx)\right]^2} \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(e+fx)\right]^2+b \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}} - \\
 & 2 i a^2 \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(e+fx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \\
 & \sqrt{1-\tan\left[\frac{1}{2}(e+fx)\right]^2} \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(e+fx)\right]^2+b \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}} + \\
 & 2 i b^2 \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(e+fx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \\
 & \sqrt{1-\tan\left[\frac{1}{2}(e+fx)\right]^2} \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(e+fx)\right]^2+b \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}} - \\
 & i(a-b)b \text{EllipticE}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(e+fx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1-\tan\left[\frac{1}{2}(e+fx)\right]^2} \\
 & \left(1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right) \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(e+fx)\right]^2+b \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}} + \\
 & i(a^2+ab-2b^2) \text{EllipticF}\left[i \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(e+fx)\right]\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{1-\tan\left[\frac{1}{2}(e+fx)\right]^2} \left(1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right) \\
 & \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(e+fx)\right]^2+b \tan\left[\frac{1}{2}(e+fx)\right]^2}{a+b}} \Bigg) \Bigg/ \\
 & \left(a \sqrt{\frac{-a+b}{a+b}} (a^2-b^2) f (a+b \sec[e+fx])^{3/2} \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]^2\right)\right. \\
 & \left.\sqrt{\frac{1+\tan\left[\frac{1}{2}(e+fx)\right]^2}{1-\tan\left[\frac{1}{2}(e+fx)\right]^2}}\right)
 \end{aligned}$$

$$\left(a \left(-1 + \tan \left[\frac{1}{2} (e + f x) \right] \right)^2 - b \left(1 + \tan \left[\frac{1}{2} (e + f x) \right] \right)^2 \right)$$

Problem 256: Unable to integrate problem.

$$\int \frac{\csc [e + f x]^2}{(a + b \sec [e + f x])^{3/2}} dx$$

Optimal (type 4, 318 leaves, 6 steps):

$$\left(4 a \cot [e + f x] \operatorname{EllipticE} \left[\operatorname{ArcSin} \left[\frac{\sqrt{a + b \sec [e + f x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \right. \\ \left. \sqrt{\frac{b (1 - \sec [e + f x])}{a + b}} \sqrt{-\frac{b (1 + \sec [e + f x])}{a - b}} \right) / \left((a - b) (a + b)^{3/2} f \right) - \\ \left((3 a - b) \cot [e + f x] \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\sqrt{a + b \sec [e + f x]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \right. \\ \left. \sqrt{\frac{b (1 - \sec [e + f x])}{a + b}} \sqrt{-\frac{b (1 + \sec [e + f x])}{a - b}} \right) / \left((a - b) (a + b)^{3/2} f \right) - \\ \frac{\cot [e + f x]}{f (a + b \sec [e + f x])^{3/2}} + \frac{b^2 \tan [e + f x]}{(a^2 - b^2) f (a + b \sec [e + f x])^{3/2}} + \\ \frac{4 a b^2 \tan [e + f x]}{(a^2 - b^2)^2 f \sqrt{a + b \sec [e + f x]}}$$

Result (type 8, 25 leaves):

$$\int \frac{\csc [e + f x]^2}{(a + b \sec [e + f x])^{3/2}} dx$$

Problem 260: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \sin [c + d x])^m}{a + b \sec [c + d x]} dx$$

Optimal (type 6, 232 leaves, 4 steps):

$$\begin{aligned}
 & -\frac{1}{a^2 d (1-m)} b e \operatorname{AppellF1}\left[1-m, \frac{1-m}{2}, \frac{1-m}{2}, 2-m, -\frac{a-b}{b+a \cos [c+d x]}, \frac{a+b}{b+a \cos [c+d x]}\right] \\
 & \left(-\frac{a(1-\cos [c+d x])}{b+a \cos [c+d x]}\right)^{\frac{1-m}{2}} \left(\frac{a(1+\cos [c+d x])}{b+a \cos [c+d x]}\right)^{\frac{1-m}{2}} (e \sin [c+d x])^{-1+m} + \\
 & \left(\cos [c+d x] \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, \sin [c+d x]^2\right] (e \sin [c+d x])^{1+m}\right) / \\
 & \left(a d e (1+m) \sqrt{\cos [c+d x]^2}\right)
 \end{aligned}$$

Result (type 6, 3387 leaves):

$$\begin{aligned}
 & -\left(\left(2 \sin [c+d x]^m (e \sin [c+d x])^m \tan \left[\frac{1}{2}(c+d x)\right]\right.\right. \\
 & \left.\left(-\operatorname{Hypergeometric2F1}\left[\frac{1+m}{2}, 1+m, \frac{3+m}{2}, -\tan \left[\frac{1}{2}(c+d x)\right]^2\right] \left(\sec \left[\frac{1}{2}(c+d x)\right]^2\right)^m -\right.\right. \\
 & \left.\left(b(a+b)(3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\tan \left[\frac{1}{2}(c+d x)\right]^2\right],\right.\right. \\
 & \left.\left.\frac{(a-b) \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] \cos \left[\frac{1}{2}(c+d x)\right]^2\right) / \left((b+a \cos [c+d x])\left(-\frac{(a+b)(3+m)}{a+b}\right.\right.\right. \\
 & \left.\left.\operatorname{AppellF1}\left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\tan \left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right]\right) +\right. \\
 & \left.2\left(-\frac{(a+b)(3+m)}{a+b}\right) \operatorname{AppellF1}\left[\frac{3+m}{2}, m, 2, \frac{5+m}{2}, -\tan \left[\frac{1}{2}(c+d x)\right]^2,\right.\right. \\
 & \left.\left.\frac{(a-b) \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] + (a+b) m \operatorname{AppellF1}\left[\frac{3+m}{2}, 1+m, 1, \frac{5+m}{2},\right.\right. \\
 & \left.\left.-\tan \left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] \tan \left[\frac{1}{2}(c+d x)\right]^2\right)\right) / \\
 & \left(a d (1+m) (a+b \sec [c+d x])\left(-\frac{1}{a(1+m)} \sec \left[\frac{1}{2}(c+d x)\right]^2 \sin [c+d x]^m\right.\right. \\
 & \left.\left(-\operatorname{Hypergeometric2F1}\left[\frac{1+m}{2}, 1+m, \frac{3+m}{2}, -\tan \left[\frac{1}{2}(c+d x)\right]^2\right] \left(\sec \left[\frac{1}{2}(c+d x)\right]^2\right)^m -\right.\right. \\
 & \left.\left(b(a+b)(3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\tan \left[\frac{1}{2}(c+d x)\right]^2\right],\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \Big/ \\
 & \left((b+a \operatorname{Cos}[c+dx]) \left(-(a+b)(3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \\
 & \quad \left. \left. 2 \left((-a+b) \operatorname{AppellF1}\left[\frac{3+m}{2}, m, 2, \frac{5+m}{2}, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) m \operatorname{AppellF1}\left[\frac{3+m}{2}, 1+m, 1, \frac{5+m}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) - \\
 & \frac{1}{a(1+m)} 2m \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]^{-1+m} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \\
 & \left(-\operatorname{Hypergeometric2F1}\left[\frac{1+m}{2}, 1+m, \frac{3+m}{2}, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \left(\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right)^m - \right. \\
 & \left. \left(b(a+b)(3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big/ \right. \\
 & \left. \left((b+a \operatorname{Cos}[c+dx]) \left(-(a+b)(3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \\
 & \quad \left. \left. 2 \left((-a+b) \operatorname{AppellF1}\left[\frac{3+m}{2}, m, 2, \frac{5+m}{2}, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) m \operatorname{AppellF1}\left[\frac{3+m}{2}, 1+m, 1, \frac{5+m}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{a(1+m)} 2 \operatorname{Sin}[c+dx]^m \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left(-m \operatorname{Hypergeometric2F1}\left[\frac{1+m}{2}, 1+m, \right. \right. \\
 & \quad \left. \left. \frac{3+m}{2}, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \left(\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right)^m \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left(b(a+b)(3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \Big/ \\
 & \quad \left((b+a \operatorname{Cos}[c+dx]) \left(- (a+b)(3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \\
 & \quad \left. 2 \left((-a+b) \operatorname{AppellF1}\left[\frac{3+m}{2}, m, 2, \frac{5+m}{2}, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) m \operatorname{AppellF1}\left[\frac{3+m}{2}, 1+m, 1, \frac{5+m}{2}, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big) - \\
 & \quad \left(a b (a+b)(3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sin}[c+dx] \right) \Big/ \\
 & \quad \left((b+a \operatorname{Cos}[c+dx])^2 \left(- (a+b)(3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \\
 & \quad \left. 2 \left((-a+b) \operatorname{AppellF1}\left[\frac{3+m}{2}, m, 2, \frac{5+m}{2}, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) m \operatorname{AppellF1}\left[\frac{3+m}{2}, 1+m, 1, \frac{5+m}{2}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right)\tan\left[\frac{1}{2}(c+dx)\right]^2\right) - \\
 & \left(b(a+b)(3+m)\cos\left[\frac{1}{2}(c+dx)\right]^2\left(\left((a-b)(1+m)\operatorname{AppellF1}\left[1+\frac{1+m}{2},\right.\right.\right. \right. \\
 & \left.\left.\left.\left.m, 2, 1+\frac{3+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right.\right.\right. \right. \\
 & \left.\left.\left.\left.\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\tan\left[\frac{1}{2}(c+dx)\right]\right)\right)/\left((a+b)(3+m)\right)-\frac{1}{3+m}\right.\right.\right. \\
 & \left.\left.\left.\left.m(1+m)\operatorname{AppellF1}\left[1+\frac{1+m}{2}, 1+m, 1, 1+\frac{3+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2,\right.\right.\right.\right. \\
 & \left.\left.\left.\left.\frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\tan\left[\frac{1}{2}(c+dx)\right]\right)\right)\right)/ \\
 & \left((b+a\cos[c+dx])\left(-\left(a+b\right)(3+m)\operatorname{AppellF1}\left[\frac{1+m}{2}, m, 1, \frac{3+m}{2},\right.\right.\right. \right. \\
 & \left.\left.\left.\left.-\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right)+\right.\right.\right. \\
 & \left.\left.\left.\left.2\left(-a+b\right)\operatorname{AppellF1}\left[\frac{3+m}{2}, m, 2, \frac{5+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2,\right.\right.\right.\right. \right. \\
 & \left.\left.\left.\left.\frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]+\left(a+b\right)m\operatorname{AppellF1}\left[\frac{3+m}{2}, 1+m, 1, \frac{5+m}{2},\right.\right.\right.\right. \right. \\
 & \left.\left.\left.\left.\left.-\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right)\right)\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) - \\
 & \frac{1}{2}(1+m)\operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]\left(\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right)^m \\
 & \left(-\operatorname{Hypergeometric2F1}\left[\frac{1+m}{2}, 1+m, \frac{3+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]+ \right. \\
 & \left.\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{-1-m}\right)+\left(b(a+b)(3+m)\right.\right. \\
 & \left.\left.\operatorname{AppellF1}\left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right)\right. \\
 & \left.\cos\left[\frac{1}{2}(c+dx)\right]^2\right)\left(2\left(-a+b\right)\operatorname{AppellF1}\left[\frac{3+m}{2}, m, 2, \frac{5+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2,\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} + (a+b) m \operatorname{AppellF1}\left[\frac{3+m}{2}, 1+m, 1, \frac{5+m}{2}, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \tan\left[\frac{1}{2}(c+dx)\right] - (a+b) (3+m) \left(\left((a-b) (1+m) \operatorname{AppellF1}\left[1+\frac{1+m}{2}, \right. \right. \right. \\
 & \left. \left. m, 2, 1+\frac{3+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right. \\
 & \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \left((a+b) (3+m) \right) - \frac{1}{3+m} \\
 & m (1+m) \operatorname{AppellF1}\left[1+\frac{1+m}{2}, 1+m, 1, 1+\frac{3+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \\
 & 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left((-a+b) \left(\left(2 (a-b) (3+m) \operatorname{AppellF1}\left[1+\frac{3+m}{2}, \right. \right. \right. \right. \\
 & \left. \left. m, 3, 1+\frac{5+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right. \\
 & \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \left((a+b) (5+m) \right) - \frac{1}{5+m} \\
 & m (3+m) \operatorname{AppellF1}\left[1+\frac{3+m}{2}, 1+m, 2, 1+\frac{5+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \\
 & (a+b) m \left(\left((a-b) (3+m) \operatorname{AppellF1}\left[1+\frac{3+m}{2}, 1+m, 2, 1+\frac{5+m}{2}, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \tan\left[\frac{1}{2}(c+dx)\right] \right) / \left((a+b) (5+m) \right) - \frac{1}{5+m} (1+m) (3+m) \\
 & \operatorname{AppellF1}\left[1+\frac{3+m}{2}, 2+m, 1, 1+\frac{5+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(\text{Hypergeometric2F1} \left[\frac{1+m}{2}, 1+m, \frac{3+m}{2}, -\text{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \left(1 + \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right)^m - \right. \\
 & \left. \left(2 a b^2 (a+b) (3+m) \right. \right. \\
 & \left. \left. \text{AppellF1} \left[\frac{1+m}{2}, m, 2, \frac{3+m}{2}, -\text{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) / \right. \\
 & \left((a-b) \left(- (a+b) (3+m) \text{AppellF1} \left[\frac{1+m}{2}, m, 2, \frac{3+m}{2}, -\text{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + 2 \left(-2 (a-b) \text{AppellF1} \left[\frac{3+m}{2}, m, 3, \frac{5+m}{2}, \right. \right. \right. \\
 & \left. \left. -\text{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) m \text{AppellF1} \left[\frac{3+m}{2}, 1+ \right. \right. \\
 & \left. \left. m, 2, \frac{5+m}{2}, -\text{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \\
 & \left. \left(a \left(-1 + \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) - b \left(1 + \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \right)^2 - \left(2 a b (a+b) (3+m) \right. \right. \\
 & \left. \left. \text{AppellF1} \left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\text{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) / \right. \\
 & \left((a-b) \left(- (a+b) (3+m) \text{AppellF1} \left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\text{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + 2 \left((-a+b) \text{AppellF1} \left[\frac{3+m}{2}, m, 2, \frac{5+m}{2}, \right. \right. \right. \\
 & \left. \left. -\text{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) m \text{AppellF1} \left[\frac{3+m}{2}, 1+ \right. \right. \\
 & \left. \left. m, 1, \frac{5+m}{2}, -\text{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \\
 & \left. \left(a \left(-1 + \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) - b \left(1 + \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \right)^2 + \left(b^2 (a+b) (3+m) \right. \right. \\
 & \left. \left. \text{AppellF1} \left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\text{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) / \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left((a-b) \left(- (a+b) (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + 2 \left((-a+b) \operatorname{AppellF1} \left[\frac{3+m}{2}, m, 2, \frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) m \operatorname{AppellF1} \left[\frac{3+m}{2}, 1+ \right. \right. \\
 & \quad \left. \left. m, 1, \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \\
 & \left. \left(a \left(-1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) - b \left(1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \right) \right) / \\
 & \left(a^2 d (1+m) (a+b \operatorname{Sec} [c+dx])^2 \left(\frac{1}{a^2 (1+m)} 2^m \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \left(\frac{\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]}{1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2} \right)^m \right. \right. \\
 & \left. \left(\operatorname{Hypergeometric2F1} \left[\frac{1+m}{2}, 1+m, \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right] \left(1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right)^m - \right. \right. \\
 & \left. \left(2 a b^2 (a+b) (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, m, 2, \frac{3+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right) / \\
 & \left((a-b) \left(- (a+b) (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, m, 2, \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + 2 \left(-2 (a-b) \operatorname{AppellF1} \left[\frac{3+m}{2}, m, 3, \frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) m \operatorname{AppellF1} \left[\right. \right. \\
 & \quad \left. \left. \frac{3+m}{2}, 1+m, 2, \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right) \\
 & \left. \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \left(a \left(-1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) - b \left(1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \right) \right) - \\
 & \left(2 a b (a+b) (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \Bigg/ \left((a-b) \left(- (a+b) (3+m) \operatorname{AppellF1}\left[\right. \right. \right. \\
 & \left. \left. \left. \frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \right. \\
 & \left. \left. 2 \left((-a+b) \operatorname{AppellF1}\left[\frac{3+m}{2}, m, 2, \frac{5+m}{2}, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) m \operatorname{AppellF1}\left[\frac{3+m}{2}, 1+m, 1, \frac{5+m}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left(a \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) + \left(b^2 (a+b) (3+m) \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \Bigg/ \\
 & \left((a-b) \left(- (a+b) (3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + 2 \left((-a+b) \operatorname{AppellF1}\left[\frac{3+m}{2}, m, 2, \frac{5+m}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) m \operatorname{AppellF1}\left[\right. \right. \right. \\
 & \left. \left. \left. \frac{3+m}{2}, 1+m, 1, \frac{5+m}{2}, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right) \right) \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \left(a \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) \Bigg) + \\
 & \frac{1}{a^2 (1+m)} 2^{1+m} m \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left(\frac{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{-1+m} \\
 & \left(- \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{\left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2} + \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2 \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)} \right) \\
 & \left(\operatorname{Hypergeometric2F1}\left[\frac{1+m}{2}, 1+m, \frac{3+m}{2}, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right] \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^m - \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(2 a b^2 (a+b) (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, m, 2, \frac{3+m}{2}, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right) / \\
 & \left((a-b) \left(- (a+b) (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, m, 2, \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2}{a+b} \right] + 2 \left(-2 (a-b) \operatorname{AppellF1} \left[\frac{3+m}{2}, m, 3, \frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2}{a+b} \right] + (a+b) m \operatorname{AppellF1} \left[\right. \right. \\
 & \quad \left. \left. \frac{3+m}{2}, 1+m, 2, \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right) \right) \\
 & \quad \left. \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2 \right) \left(a \left(-1 + \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2 \right) - b \left(1 + \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2 \right) \right)^2 - \\
 & \left(2 a b (a+b) (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right) / \left((a-b) \left(- (a+b) (3+m) \operatorname{AppellF1} \left[\right. \right. \right. \\
 & \quad \left. \left. \frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2}{a+b} \right] + \right. \\
 & \quad \left. 2 \left((-a+b) \operatorname{AppellF1} \left[\frac{3+m}{2}, m, 2, \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2}{a+b} \right] + (a+b) m \operatorname{AppellF1} \left[\frac{3+m}{2}, 1+m, 1, \frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2 \right) \\
 & \quad \left(a \left(-1 + \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2 \right) - b \left(1 + \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2 \right) \right) \right) + \left(b^2 (a+b) (3+m) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left((a-b) \left(- (a+b) (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\tan \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + 2 \left((-a+b) \operatorname{AppellF1} \left[\frac{3+m}{2}, m, 2, \frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) m \operatorname{AppellF1} \left[\right. \right. \\
 & \quad \left. \left. \frac{3+m}{2}, 1+m, 1, \frac{5+m}{2}, -\tan \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \\
 & \quad \left. \left. \tan \left[\frac{1}{2} (c+dx) \right]^2 \right) \left(a \left(-1 + \tan \left[\frac{1}{2} (c+dx) \right]^2 \right) - b \left(1 + \tan \left[\frac{1}{2} (c+dx) \right]^2 \right) \right) \right) + \\
 & \frac{1}{a^2 (1+m)} 2^{1+m} \tan \left[\frac{1}{2} (c+dx) \right] \left(\frac{\tan \left[\frac{1}{2} (c+dx) \right]}{1 + \tan \left[\frac{1}{2} (c+dx) \right]^2} \right)^m \\
 & \left(m \operatorname{Hypergeometric2F1} \left[\frac{1+m}{2}, 1+m, \frac{3+m}{2}, -\tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \right. \\
 & \quad \tan \left[\frac{1}{2} (c+dx) \right] \left(1 + \tan \left[\frac{1}{2} (c+dx) \right]^2 \right)^{-1+m} + \left(4 a b^2 (a+b) (3+m) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{1+m}{2}, m, 2, \frac{3+m}{2}, -\tan \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \left(a \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] - b \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] \right) \right) / \\
 & \left((a-b) \left(- (a+b) (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, m, 2, \frac{3+m}{2}, -\tan \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + 2 \left(-2 (a-b) \operatorname{AppellF1} \left[\frac{3+m}{2}, m, 3, \frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) m \operatorname{AppellF1} \left[\right. \right. \\
 & \quad \left. \left. \frac{3+m}{2}, 1+m, 2, \frac{5+m}{2}, -\tan \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \\
 & \quad \left. \left. \tan \left[\frac{1}{2} (c+dx) \right]^2 \right) \left(a \left(-1 + \tan \left[\frac{1}{2} (c+dx) \right]^2 \right) - b \left(1 + \tan \left[\frac{1}{2} (c+dx) \right]^2 \right) \right)^3 \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left(2 a b (a+b) (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \left(a \operatorname{Sec} \left[\frac{1}{2} (c+d x) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right] - b \operatorname{Sec} \left[\frac{1}{2} (c+d x) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right] \right) \right) / \\
 & \left((a-b) \left(- (a+b) (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2}{a+b} \right] + 2 \left((-a+b) \operatorname{AppellF1} \left[\frac{3+m}{2}, m, 2, \frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2}{a+b} \right] + (a+b) m \operatorname{AppellF1} \left[\right. \right. \\
 & \quad \left. \left. \frac{3+m}{2}, 1+m, 1, \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right) \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2 \right) \left(a \left(-1 + \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2 \right) - b \left(1 + \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2 \right) \right)^2 \right) - \\
 & \left(b^2 (a+b) (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \left(a \operatorname{Sec} \left[\frac{1}{2} (c+d x) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right] - b \operatorname{Sec} \left[\frac{1}{2} (c+d x) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right] \right) \right) / \\
 & \left((a-b) \left(- (a+b) (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2}{a+b} \right] + 2 \left((-a+b) \operatorname{AppellF1} \left[\frac{3+m}{2}, m, 2, \frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2}{a+b} \right] + (a+b) m \operatorname{AppellF1} \left[\right. \right. \\
 & \quad \left. \left. \frac{3+m}{2}, 1+m, 1, \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+d x) \right]^2}{a+b} \right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(a \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right)^2 \right) - \\
 & \left(2ab^2(a+b)(3+m) \left(\left(2(a-b)(1+m) \operatorname{AppellF1}\left[1 + \frac{1+m}{2}, m, 3, 1 + \frac{3+m}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right) \right) / \left((a+b)(3+m) - \frac{1}{3+m} \right. \\
 & \quad \left. m(1+m) \operatorname{AppellF1}\left[1 + \frac{1+m}{2}, 1+m, 2, 1 + \frac{3+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Bigg/ \\
 & \left((a-b) \left(- (a+b)(3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, m, 2, \frac{3+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + 2 \left(-2(a-b) \operatorname{AppellF1}\left[\frac{3+m}{2}, m, 3, \frac{5+m}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b)m \operatorname{AppellF1}\left[\right. \right. \right. \\
 & \quad \left. \left. \left. \frac{3+m}{2}, 1+m, 2, \frac{5+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right) \right) \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(a \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right)^2 \right) - \\
 & \left(2ab(a+b)(3+m) \left(\left((a-b)(1+m) \operatorname{AppellF1}\left[1 + \frac{1+m}{2}, m, 2, 1 + \frac{3+m}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right) \right) / \left((a+b)(3+m) - \frac{1}{3+m} \right. \\
 & \quad \left. m(1+m) \operatorname{AppellF1}\left[1 + \frac{1+m}{2}, 1+m, 1, 1 + \frac{3+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Bigg/
 \end{aligned}$$

$$\begin{aligned}
 & \left((a-b) \left(- (a+b) (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + 2 \left((-a+b) \operatorname{AppellF1} \left[\frac{3+m}{2}, m, 2, \frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) m \operatorname{AppellF1} \left[\right. \right. \\
 & \quad \left. \left. \frac{3+m}{2}, 1+m, 1, \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right) \\
 & \quad \left. \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \left(a \left(-1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) - b \left(1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \right) \right) + \\
 & \left(b^2 (a+b) (3+m) \left(\left((a-b) (1+m) \operatorname{AppellF1} \left[1 + \frac{1+m}{2}, m, 2, 1 + \frac{3+m}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) \right) / \left((a+b) (3+m) - \frac{1}{3+m} \right. \\
 & \quad \left. m (1+m) \operatorname{AppellF1} \left[1 + \frac{1+m}{2}, 1+m, 1, 1 + \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) \right) / \\
 & \left((a-b) \left(- (a+b) (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + 2 \left((-a+b) \operatorname{AppellF1} \left[\frac{3+m}{2}, m, 2, \frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) m \operatorname{AppellF1} \left[\right. \right. \\
 & \quad \left. \left. \frac{3+m}{2}, 1+m, 1, \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right) \\
 & \quad \left. \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \left(a \left(-1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) - b \left(1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \right) \right) + \\
 & \frac{1}{2} (1+m) \operatorname{Csc} \left[\frac{1}{2} (c+dx) \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right] \left(1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right)^m
 \end{aligned}$$

$$\begin{aligned}
 & \left(-\text{Hypergeometric2F1}\left[\frac{1+m}{2}, 1+m, \frac{3+m}{2}, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad \left. \left(1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^{-1-m} \right) + \\
 & \left(2ab(a+b)(3+m) \text{AppellF1}\left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right], \right. \\
 & \quad \frac{(a-b) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \left[2 \left((-a+b) \text{AppellF1}\left[\frac{3+m}{2}, m, 2, \frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b)m \text{AppellF1}\left[\frac{3+m}{2}, 1+m, 1, \frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right] \\
 & \quad \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] - (a+b)(3+m) \left(\left((a-b)(1+m) \text{AppellF1}\left[\right. \right. \right. \\
 & \quad \left. \left. \left. 1 + \frac{1+m}{2}, m, 2, 1 + \frac{3+m}{2}, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right)^2 \right. \\
 & \quad \left. \left. \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right] / \left((a+b)(3+m) \right) - \frac{1}{3+m} \\
 & \quad m(1+m) \text{AppellF1}\left[1 + \frac{1+m}{2}, 1+m, 1, 1 + \frac{3+m}{2}, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. \frac{(a-b) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] \left. \right) + \\
 & \quad 2 \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left((-a+b) \left(\left(2(a-b)(3+m) \text{AppellF1}\left[1 + \frac{3+m}{2}, m, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 3, 1 + \frac{5+m}{2}, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right)^2 \right. \right. \\
 & \quad \left. \left. \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right] / \left((a+b)(5+m) \right) - \frac{1}{5+m} \\
 & \quad m(3+m) \text{AppellF1}\left[1 + \frac{3+m}{2}, 1+m, 2, 1 + \frac{5+m}{2}, -\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. \frac{(a-b) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] \left. \right) +
 \end{aligned}$$

$$\begin{aligned}
 & (a+b) m \left(\left((a-b) (3+m) \operatorname{AppellF1} \left[1 + \frac{3+m}{2}, 1+m, 2, 1 + \frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) / \left((a+b) (5+m) - \frac{1}{5+m} (1+m) (3+m) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[1 + \frac{3+m}{2}, 2+m, 1, 1 + \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) \right) \right) / \\
 & \left((a-b) \left(- (a+b) (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + 2 \left((-a+b) \operatorname{AppellF1} \left[\frac{3+m}{2}, m, 2, \frac{5+m}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) m \operatorname{AppellF1} \left[\right. \right. \right. \\
 & \quad \left. \left. \left. \frac{3+m}{2}, 1+m, 1, \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right) \right) \\
 & \quad \left. \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right)^2 \left(a \left(-1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) - b \left(1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \right) \right) - \\
 & \left(b^2 (a+b) (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \left(2 \left((-a+b) \operatorname{AppellF1} \left[\frac{3+m}{2}, m, 2, \frac{5+m}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) m \operatorname{AppellF1} \left[\right. \right. \right. \\
 & \quad \left. \left. \left. \frac{3+m}{2}, 1+m, 1, \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right) \right) \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] - (a+b) (3+m) \left(\left((a-b) (1+m) \operatorname{AppellF1} \left[\right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. 1 + \frac{1+m}{2}, m, 2, 1 + \frac{3+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \\
 & \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \left((a+b)(3+m) - \frac{1}{3+m} \right. \\
 & \left. m(1+m) \operatorname{AppellF1}\left[1 + \frac{1+m}{2}, 1+m, 1, 1 + \frac{3+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \\
 & 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left((-a+b) \left(\left(2(a-b)(3+m) \operatorname{AppellF1}\left[1 + \frac{3+m}{2}, m, \right. \right. \right. \right. \\
 & \left. \left. \left. 3, 1 + \frac{5+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right. \right. \\
 & \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \left((a+b)(5+m) - \frac{1}{5+m} \right. \right. \\
 & \left. \left. m(3+m) \operatorname{AppellF1}\left[1 + \frac{3+m}{2}, 1+m, 2, 1 + \frac{5+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
 & (a+b)m \left(\left((a-b)(3+m) \operatorname{AppellF1}\left[1 + \frac{3+m}{2}, 1+m, 2, 1 + \frac{5+m}{2}, \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] \right) / \left((a+b)(5+m) - \frac{1}{5+m}(1+m)(3+m) \right) \right. \\
 & \left. \operatorname{AppellF1}\left[1 + \frac{3+m}{2}, 2+m, 1, 1 + \frac{5+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \\
 & \left((a-b) \left(- (a+b)(3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, m, 1, \frac{3+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + 2 \left((-a+b) \operatorname{AppellF1}\left[\frac{3+m}{2}, m, 2, \frac{5+m}{2}, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}] + (a+b)m\operatorname{AppellF1}\left[\right. \\
 & \left. \frac{3+m}{2}, 1+m, 1, \frac{5+m}{2}, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \left(a \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) + \\
 & \left(2ab^2(a+b)(3+m)\operatorname{AppellF1}\left[\frac{1+m}{2}, m, 2, \frac{3+m}{2}, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left(2 \left(-2(a-b)\operatorname{AppellF1}\left[\frac{3+m}{2}, m, 3, \frac{5+m}{2}, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b)m\operatorname{AppellF1}\left[\frac{3+m}{2}, 1+m, 2, \frac{5+m}{2}, \right. \right. \right. \\
 & \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\right. \right. \\
 & \left. \left. \frac{1}{2}(c+dx)\right] - (a+b)(3+m) \left(\left(2(a-b)(1+m)\operatorname{AppellF1}\left[1 + \frac{1+m}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. m, 3, 1 + \frac{3+m}{2}, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) / \left((a+b)(3+m) - \frac{1}{3+m} \right. \\
 & \left. m(1+m)\operatorname{AppellF1}\left[1 + \frac{1+m}{2}, 1+m, 2, 1 + \frac{3+m}{2}, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
 & 2\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left(-2(a-b) \left(\left(3(a-b)(3+m)\operatorname{AppellF1}\left[1 + \frac{3+m}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. m, 4, 1 + \frac{5+m}{2}, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) / \left((a+b)(5+m) - \frac{1}{5+m} \right)
 \end{aligned}$$

$$\begin{aligned}
 & m(3+m) \operatorname{AppellF1}\left[1 + \frac{3+m}{2}, 1+m, 3, 1 + \frac{5+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \\
 & (a+b) m \left(\left(2(a-b)(3+m) \operatorname{AppellF1}\left[1 + \frac{3+m}{2}, 1+m, 3, 1 + \frac{5+m}{2}, \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) / \left((a+b)(5+m) - \frac{1}{5+m}(1+m)(3+m) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[1 + \frac{3+m}{2}, 2+m, 2, 1 + \frac{5+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \\
 & \left((a-b) \left(- (a+b)(3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, m, 2, \frac{3+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \left. 2 \left(-2(a-b) \operatorname{AppellF1}\left[\frac{3+m}{2}, m, 3, \frac{5+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) m \operatorname{AppellF1}\left[\frac{3+m}{2}, 1+m, 2, \frac{5+m}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
 & \left(a \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) \right) \right)
 \end{aligned}$$

Problem 262: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \sin[c+dx])^m}{(a+b \sec[c+dx])^3} dx$$

Optimal (type 6, 580 leaves, 7 steps):

$$\begin{aligned}
 & -\frac{1}{a^4 d (1-m)} 3 b e \operatorname{AppellF1}\left[1-m, \frac{1-m}{2}, \frac{1-m}{2}, 2-m, -\frac{a-b}{b+a \cos [c+d x]}, \frac{a+b}{b+a \cos [c+d x]}\right] \\
 & \left(-\frac{a(1-\cos [c+d x])}{b+a \cos [c+d x]}\right)^{\frac{1-m}{2}} \left(\frac{a(1+\cos [c+d x])}{b+a \cos [c+d x]}\right)^{\frac{1-m}{2}} (e \sin [c+d x])^{-1+m} - \\
 & \left(b^3 e \operatorname{AppellF1}\left[3-m, \frac{1-m}{2}, \frac{1-m}{2}, 4-m, -\frac{a-b}{b+a \cos [c+d x]}, \frac{a+b}{b+a \cos [c+d x]}\right]\right. \\
 & \left.\left(-\frac{a(1-\cos [c+d x])}{b+a \cos [c+d x]}\right)^{\frac{1-m}{2}} \left(\frac{a(1+\cos [c+d x])}{b+a \cos [c+d x]}\right)^{\frac{1-m}{2}} (e \sin [c+d x])^{-1+m}\right) / \\
 & \left(a^4 d (3-m)(b+a \cos [c+d x])^2\right) + \\
 & \left(3 b^2 e \operatorname{AppellF1}\left[2-m, \frac{1-m}{2}, \frac{1-m}{2}, 3-m, -\frac{a-b}{b+a \cos [c+d x]}, \frac{a+b}{b+a \cos [c+d x]}\right]\right. \\
 & \left.\left(-\frac{a(1-\cos [c+d x])}{b+a \cos [c+d x]}\right)^{\frac{1-m}{2}} \left(\frac{a(1+\cos [c+d x])}{b+a \cos [c+d x]}\right)^{\frac{1-m}{2}} (e \sin [c+d x])^{-1+m}\right) / \\
 & \left(a^4 d (2-m)(b+a \cos [c+d x])\right) + \\
 & \left(\cos [c+d x] \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, \sin [c+d x]^2\right] (e \sin [c+d x])^{1+m}\right) / \\
 & \left(a^3 d e (1+m) \sqrt{\cos [c+d x]^2}\right)
 \end{aligned}$$

Result (type 6, 12336 leaves):

$$\begin{aligned}
 & \left((e \sin [c+d x])^m \right. \\
 & \left. \left(\left((a+b)(3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, 1+m, 3, \frac{3+m}{2}, -\tan \left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] \right)^2 \right. \right. \\
 & \left. \left. \left(\frac{\tan \left[\frac{1}{2}(c+d x)\right]}{1+\tan \left[\frac{1}{2}(c+d x)\right]^2} \right)^{1+m} \right) \right) / \\
 & \left((1+m) \left(a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2 + b \tan \left[\frac{1}{2}(c+d x)\right]^2 \right)^3 \left(- (a+b)(3+m) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{1+m}{2}, 1+m, 3, \frac{3+m}{2}, -\tan \left[\frac{1}{2}(c+d x)\right]^2, \frac{(a-b) \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}\right] \right) + \right. \\
 & \left. 2 \left(-3(a-b) \operatorname{AppellF1}\left[\frac{3+m}{2}, 1+m, 4, \frac{5+m}{2}, -\tan \left[\frac{1}{2}(c+d x)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b} \right] + (a+b)(1+m) \operatorname{AppellF1}\left[\frac{3+m}{2}, 2+m, 3, \frac{5+m}{2}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) - \\
 & \left(3(a+b)(5+m) \operatorname{AppellF1}\left[\frac{3+m}{2}, 1+m, 3, \frac{5+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(\frac{\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^{1+m}\right] \right) / \\
 & \left((3+m) \left(a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2 + b\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^3 \left(-(a+b)(5+m) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{3+m}{2}, 1+m, 3, \frac{5+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right)^2 + \right. \\
 & \quad 2 \left(-3(a-b) \operatorname{AppellF1}\left[\frac{5+m}{2}, 1+m, 4, \frac{7+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b)(1+m) \operatorname{AppellF1}\left[\frac{5+m}{2}, 2+m, 3, \frac{7+m}{2}, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \left(3(a+b)(7+m) \operatorname{AppellF1}\left[\frac{5+m}{2}, 1+m, 3, \frac{7+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^4 \left(\frac{\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^{1+m}\right] \right) / \\
 & \left((5+m) \left(a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2 + b\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^3 \left(-(a+b)(7+m) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{5+m}{2}, 1+m, 3, \frac{7+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right)^2 + \right. \\
 & \quad 2 \left(-3(a-b) \operatorname{AppellF1}\left[\frac{7+m}{2}, 1+m, 4, \frac{9+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b)(1+m) \operatorname{AppellF1}\left[\frac{7+m}{2}, 2+m, 3, \frac{9+m}{2}, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) -
 \end{aligned}$$

$$\begin{aligned}
& \left((a+b) (9+m) \operatorname{AppellF1} \left[\frac{7+m}{2}, 1+m, 3, \frac{9+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^6 \left(\frac{\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]}{1+\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2} \right)^{1+m} \right) / \\
& \left((7+m) \left(a+b-a \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right)^3 \left(- (a+b) (9+m) \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1} \left[\frac{7+m}{2}, 1+m, 3, \frac{9+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
& \quad \left. \left. 2 \left(-3 (a-b) \operatorname{AppellF1} \left[\frac{9+m}{2}, 1+m, 4, \frac{11+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \right. \\
& \quad \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) (1+m) \operatorname{AppellF1} \left[\frac{9+m}{2}, 2+m, 3, \frac{11+m}{2}, \right. \right. \right. \\
& \quad \quad \left. \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
& \left(d (a+b \operatorname{Sec} [c+dx])^3 \left(\left(\left(3 (a+b) (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, 1+m, 3, \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \right. \right. \right. \\
& \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \left(-a \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] + \right. \right. \right. \\
& \quad \left. \left. \left. b \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) \left(\frac{\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]}{1+\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2} \right)^{1+m} \right) \right) / \\
& \left((1+m) \left(a+b-a \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right)^4 \left(- (a+b) (3+m) \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1} \left[\frac{1+m}{2}, 1+m, 3, \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
& \quad \left. \left. 2 \left(-3 (a-b) \operatorname{AppellF1} \left[\frac{3+m}{2}, 1+m, 4, \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \right. \\
& \quad \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) (1+m) \operatorname{AppellF1} \left[\frac{3+m}{2}, 2+m, 3, \frac{5+m}{2}, \right. \right. \right. \\
& \quad \quad \left. \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \right) \right) +
\end{aligned}$$

$$\begin{aligned}
 & \left((a+b) (3+m) \left(\frac{1}{(a+b) (3+m)} {}_3F_2 \left(a-b, 1+m, \text{AppellF1} \left[1 + \frac{1+m}{2}, 1+m, 4, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 1 + \frac{3+m}{2}, -\text{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right. \\
 & \quad \left. \text{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \text{Tan} \left[\frac{1}{2} (c+dx) \right] - \frac{1}{3+m} (1+m)^2 \right. \\
 & \quad \left. \text{AppellF1} \left[1 + \frac{1+m}{2}, 2+m, 3, 1 + \frac{3+m}{2}, -\text{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \left. \left. \text{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \text{Tan} \left[\frac{1}{2} (c+dx) \right] \right) \left(\frac{\text{Tan} \left[\frac{1}{2} (c+dx) \right]}{1 + \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2} \right)^{1+m} \right) / \\
 & \left((1+m) \left(a+b - a \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2 + b \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right)^3 \left(- (a+b) (3+m) \right. \right. \\
 & \quad \left. \left. \text{AppellF1} \left[\frac{1+m}{2}, 1+m, 3, \frac{3+m}{2}, -\text{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) + \right. \\
 & \quad \left. 2 \left(-3 (a-b) \text{AppellF1} \left[\frac{3+m}{2}, 1+m, 4, \frac{5+m}{2}, -\text{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) (1+m) \text{AppellF1} \left[\frac{3+m}{2}, 2+m, 3, \frac{5+m}{2}, \right. \right. \\
 & \quad \quad \left. \left. -\text{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) + \\
 & \left(9 (a+b) (5+m) \text{AppellF1} \left[\frac{3+m}{2}, 1+m, 3, \frac{5+m}{2}, -\text{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right. \\
 & \quad \left. \left(-a \text{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \text{Tan} \left[\frac{1}{2} (c+dx) \right] + b \text{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \text{Tan} \left[\frac{1}{2} (c+dx) \right] \right) \right. \\
 & \quad \left. \left(\frac{\text{Tan} \left[\frac{1}{2} (c+dx) \right]}{1 + \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2} \right)^{1+m} \right) / \\
 & \left((3+m) \left(a+b - a \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2 + b \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right)^4 \left(- (a+b) (5+m) \right. \right. \\
 & \quad \left. \left. \text{AppellF1} \left[\frac{3+m}{2}, 1+m, 3, \frac{5+m}{2}, -\text{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \text{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left(-3 (a-b) \operatorname{AppellF1} \left[\frac{5+m}{2}, 1+m, 4, \frac{7+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) (1+m) \operatorname{AppellF1} \left[\frac{5+m}{2}, 2+m, 3, \frac{7+m}{2}, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) - \\
 & \left(3 (a+b) (5+m) \operatorname{AppellF1} \left[\frac{3+m}{2}, 1+m, 3, \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \right. \\
 & \quad \left. \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \left(\frac{\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]}{1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2} \right)^{1+m} \right) / \\
 & \left((3+m) \left(a+b - a \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right)^3 \left(- (a+b) (5+m) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[\frac{3+m}{2}, 1+m, 3, \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) + \right. \\
 & 2 \left(-3 (a-b) \operatorname{AppellF1} \left[\frac{5+m}{2}, 1+m, 4, \frac{7+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) (1+m) \operatorname{AppellF1} \left[\frac{5+m}{2}, 2+m, 3, \frac{7+m}{2}, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) - \\
 & \left(3 (a+b) (5+m) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \left(\frac{1}{(a+b) (5+m)} - 3 (a-b) (3+m) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[1 + \frac{3+m}{2}, 1+m, 4, 1 + \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right. \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] - \frac{1}{5+m} (1+m) (3+m) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[1 + \frac{3+m}{2}, 2+m, 3, 1 + \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) \left(\frac{\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]}{1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2} \right)^{1+m} /
 \end{aligned}$$

$$\begin{aligned}
 & \left((3+m) \left(a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^3 \left(-(a+b)(5+m) \right. \right. \\
 & \quad \left. \text{AppellF1}\left[\frac{3+m}{2}, 1+m, 3, \frac{5+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \quad \left. 2 \left(-3(a-b) \text{AppellF1}\left[\frac{5+m}{2}, 1+m, 4, \frac{7+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b)(1+m) \text{AppellF1}\left[\frac{5+m}{2}, 2+m, 3, \frac{7+m}{2}, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left. \right) - \\
 & \left(9(a+b)(7+m) \text{AppellF1}\left[\frac{5+m}{2}, 1+m, 3, \frac{7+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^4 \right. \\
 & \quad \left(-a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + b \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \\
 & \quad \left. \left(\frac{\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1+m} \right) / \\
 & \left((5+m) \left(a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^4 \left(-(a+b)(7+m) \right. \right. \\
 & \quad \left. \text{AppellF1}\left[\frac{5+m}{2}, 1+m, 3, \frac{7+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \quad \left. 2 \left(-3(a-b) \text{AppellF1}\left[\frac{7+m}{2}, 1+m, 4, \frac{9+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b)(1+m) \text{AppellF1}\left[\frac{7+m}{2}, 2+m, 3, \frac{9+m}{2}, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left. \right) + \\
 & \left(6(a+b)(7+m) \text{AppellF1}\left[\frac{5+m}{2}, 1+m, 3, \frac{7+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^3 \left(\frac{\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^{1+m}\right] / \\
 & \left((5+m) \left(a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^3 \left(-(a+b)(7+m) \right. \right. \\
 & \quad \left. \left. \text{AppellF1}\left[\frac{5+m}{2}, 1+m, 3, \frac{7+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) + \right. \\
 & \quad 2 \left(-3(a-b) \text{AppellF1}\left[\frac{7+m}{2}, 1+m, 4, \frac{9+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b)(1+m) \text{AppellF1}\left[\frac{7+m}{2}, 2+m, 3, \frac{9+m}{2}, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \left(3(a+b)(7+m) \tan\left[\frac{1}{2}(c+dx)\right]^4 \left(\frac{1}{(a+b)(7+m)} - 3(a-b)(5+m) \right. \right. \\
 & \quad \left. \left. \text{AppellF1}\left[1+\frac{5+m}{2}, 1+m, 4, 1+\frac{7+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \frac{1}{7+m}(1+m)(5+m) \right. \\
 & \quad \left. \text{AppellF1}\left[1+\frac{5+m}{2}, 2+m, 3, 1+\frac{7+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \left(\frac{\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^{1+m}\right] / \\
 & \left((5+m) \left(a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^3 \left(-(a+b)(7+m) \right. \right. \\
 & \quad \left. \left. \text{AppellF1}\left[\frac{5+m}{2}, 1+m, 3, \frac{7+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) + \right. \\
 & \quad 2 \left(-3(a-b) \text{AppellF1}\left[\frac{7+m}{2}, 1+m, 4, \frac{9+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b)(1+m) \text{AppellF1}\left[\frac{7+m}{2}, 2+m, 3, \frac{9+m}{2}, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left(3 (a+b) (9+m) \operatorname{AppellF1} \left[\frac{7+m}{2}, 1+m, 3, \frac{9+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \right. \\
 & \quad \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^6 \\
 & \left(-a \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] + b \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) \\
 & \left(\frac{\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]}{1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2} \right)^{1+m} \Big/ \\
 & \left((7+m) \left(a+b - a \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right)^4 \left(- (a+b) (9+m) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[\frac{7+m}{2}, 1+m, 3, \frac{9+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \quad \left. 2 \left(-3 (a-b) \operatorname{AppellF1} \left[\frac{9+m}{2}, 1+m, 4, \frac{11+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) (1+m) \operatorname{AppellF1} \left[\frac{9+m}{2}, 2+m, 3, \frac{11+m}{2}, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \Big) - \\
 & \left(3 (a+b) (9+m) \operatorname{AppellF1} \left[\frac{7+m}{2}, 1+m, 3, \frac{9+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \right. \\
 & \quad \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \\
 & \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^5 \left(\frac{\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]}{1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2} \right)^{1+m} \Big/ \\
 & \left((7+m) \left(a+b - a \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right)^3 \left(- (a+b) (9+m) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[\frac{7+m}{2}, 1+m, 3, \frac{9+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \quad \left. 2 \left(-3 (a-b) \operatorname{AppellF1} \left[\frac{9+m}{2}, 1+m, 4, \frac{11+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) (1+m) \operatorname{AppellF1} \left[\frac{9+m}{2}, 2+m, 3, \frac{11+m}{2}, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right) \Big) -
 \end{aligned}$$

$$\begin{aligned}
 & \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & \left((a+b)(9+m)\tan\left[\frac{1}{2}(c+dx)\right]^6 \left(\frac{1}{(a+b)(9+m)} {}_3F_2(a-b)(7+m) \operatorname{AppellF1}\left[\right. \right. \right. \\
 & \quad \left. \left. \left. 1+\frac{7+m}{2}, 1+m, 4, 1+\frac{9+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \frac{1}{9+m}(1+m)(7+m) \right. \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[1+\frac{7+m}{2}, 2+m, 3, 1+\frac{9+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \left(\frac{\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1+m} \right) \right) / \\
 & \left((7+m) \left(a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2 + b\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^3 \left(-(a+b)(9+m) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{7+m}{2}, 1+m, 3, \frac{9+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \quad \left. 2 \left(-3(a-b) \operatorname{AppellF1}\left[\frac{9+m}{2}, 1+m, 4, \frac{11+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b)(1+m) \operatorname{AppellF1}\left[\frac{9+m}{2}, 2+m, 3, \frac{11+m}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \left((a+b)(3+m) \operatorname{AppellF1}\left[\frac{1+m}{2}, 1+m, 3, \frac{3+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left(\frac{\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^m \right. \right. \\
 & \quad \left. \left(-\frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2}{\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2} + \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right) \right) / \\
 & \left(\left(a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2 + b\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^3 \left(-(a+b)(3+m) \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{1+m}{2}, 1+m, 3, \frac{3+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \\
 & 2\left(-3(a-b)\text{AppellF1}\left[\frac{3+m}{2}, 1+m, 4, \frac{5+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b)(1+m)\text{AppellF1}\left[\frac{3+m}{2}, 2+m, 3, \frac{5+m}{2}, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\tan\left[\frac{1}{2}(c+dx)\right]^2\right) - \\
 & \left(3(a+b)(1+m)(5+m)\text{AppellF1}\left[\frac{3+m}{2}, 1+m, 3, \frac{5+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\tan\left[\frac{1}{2}(c+dx)\right]^2\left(\frac{\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^m \right. \\
 & \left. \left(-\frac{\sec\left[\frac{1}{2}(c+dx)\right]^2\tan\left[\frac{1}{2}(c+dx)\right]^2}{\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2} + \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2}{2\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right)\right) / \\
 & \left((3+m)\left(a+b-a\tan\left[\frac{1}{2}(c+dx)\right]^2+b\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^3\left(-\frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right) + \right. \\
 & \left.\text{AppellF1}\left[\frac{3+m}{2}, 1+m, 3, \frac{5+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2\left(-3(a-b)\text{AppellF1}\left[\frac{5+m}{2}, 1+m, 4, \frac{7+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b)(1+m)\text{AppellF1}\left[\frac{5+m}{2}, 2+m, 3, \frac{7+m}{2}, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\tan\left[\frac{1}{2}(c+dx)\right]^2\right) + \\
 & \left(3(a+b)(1+m)(7+m)\text{AppellF1}\left[\frac{5+m}{2}, 1+m, 3, \frac{7+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\tan\left[\frac{1}{2}(c+dx)\right]^2\left(\frac{\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^m \right. \\
 & \left. \left(-\frac{\sec\left[\frac{1}{2}(c+dx)\right]^2\tan\left[\frac{1}{2}(c+dx)\right]^2}{\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2} + \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2}{2\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right)\right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left((5+m) \left(a+b - a \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right)^3 \left(- (a+b) (7+m) \right. \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{5+m}{2}, 1+m, 3, \frac{7+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \quad \left. 2 \left(-3 (a-b) \operatorname{AppellF1} \left[\frac{7+m}{2}, 1+m, 4, \frac{9+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) (1+m) \operatorname{AppellF1} \left[\frac{7+m}{2}, 2+m, 3, \frac{9+m}{2}, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \left. \right) \right) - \\
 & \left((a+b) (1+m) (9+m) \operatorname{AppellF1} \left[\frac{7+m}{2}, 1+m, 3, \frac{9+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^6 \left(\frac{\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]}{1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2} \right)^m \\
 & \quad \left(- \frac{\operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{\left(1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right)^2} + \frac{\operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2}{2 \left(1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right)} \right) \right) / \\
 & \left((7+m) \left(a+b - a \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right)^3 \left(- (a+b) (9+m) \right. \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{7+m}{2}, 1+m, 3, \frac{9+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \quad \left. 2 \left(-3 (a-b) \operatorname{AppellF1} \left[\frac{9+m}{2}, 1+m, 4, \frac{11+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) (1+m) \operatorname{AppellF1} \left[\frac{9+m}{2}, 2+m, 3, \frac{11+m}{2}, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \left. \right) \right) - \\
 & \left((a+b) (3+m) \operatorname{AppellF1} \left[\frac{1+m}{2}, 1+m, 3, \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \left(\frac{\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]}{1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2} \right)^{1+m} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(2 \left(-3 (a-b) \operatorname{AppellF1} \left[\frac{3+m}{2}, 1+m, 4, \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \right. \right. \\
 & \quad \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) + (a+b) (1+m) \operatorname{AppellF1} \left[\frac{3+m}{2}, 2+m, 3, \right. \\
 & \quad \left. \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \\
 & \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] - (a+b) (3+m) \left(\left(3 (a-b) (1+m) \operatorname{AppellF1} \left[1 + \frac{1+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. 1+m, 4, 1 + \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \right. \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) / \left((a+b) (3+m) - \frac{1}{3+m} \right) \\
 & (1+m)^2 \operatorname{AppellF1} \left[1 + \frac{1+m}{2}, 2+m, 3, 1 + \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \\
 & \quad \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) + \\
 & 2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \left(-3 (a-b) \left(\left(4 (a-b) (3+m) \operatorname{AppellF1} \left[1 + \frac{3+m}{2}, 1+m, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 5, 1 + \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \right. \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) / \left((a+b) (5+m) - \frac{1}{5+m} \right) \\
 & (1+m) (3+m) \operatorname{AppellF1} \left[1 + \frac{3+m}{2}, 2+m, 4, 1 + \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \\
 & \quad \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) + \\
 & (a+b) (1+m) \left(\left(3 (a-b) (3+m) \operatorname{AppellF1} \left[1 + \frac{3+m}{2}, 2+m, 4, 1 + \frac{5+m}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \right. \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) / \left((a+b) (5+m) - \frac{1}{5+m} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left((2+m) (3+m) \operatorname{AppellF1} \left[1 + \frac{3+m}{2}, 3+m, 3, 1 + \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left((1+m) \left(a+b - a \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \right)^3 \left(- (a+b) (3+m) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[\frac{1+m}{2}, 1+m, 3, \frac{3+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) + \right. \\
 & \quad 2 \left(-3 (a-b) \operatorname{AppellF1} \left[\frac{3+m}{2}, 1+m, 4, \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) (1+m) \operatorname{AppellF1} \left[\frac{3+m}{2}, 2+m, 3, \frac{5+m}{2}, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \Bigg)^2 \Bigg) + \\
 & \left(3 (a+b) (5+m) \operatorname{AppellF1} \left[\frac{3+m}{2}, 1+m, 3, \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \left(\frac{\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]}{1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2} \right)^{1+m} \right) \right. \\
 & \quad \left(2 \left(-3 (a-b) \operatorname{AppellF1} \left[\frac{5+m}{2}, 1+m, 4, \frac{7+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) (1+m) \operatorname{AppellF1} \left[\frac{5+m}{2}, 2+m, 3, \right. \right. \\
 & \quad \left. \left. \frac{7+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \right. \\
 & \quad \left. \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] - (a+b) (5+m) \left(\left(3 (a-b) (3+m) \operatorname{AppellF1} \left[1 + \frac{3+m}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 1+m, 4, 1 + \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \right. \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) \right) / \left((a+b) (5+m) - \frac{1}{5+m} \right) \\
 & \quad (1+m) (3+m) \operatorname{AppellF1} \left[1 + \frac{3+m}{2}, 2+m, 3, 1 + \frac{5+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \Bigg) + \\
 & 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(-3(a-b) \left(\left(\left(4(a-b)(5+m) \operatorname{AppellF1}\left[1+\frac{5+m}{2}, 1+m, \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \left. 5, 1+\frac{7+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right] \right) / \left((a+b)(7+m) - \frac{1}{7+m} \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \left. (1+m)(5+m) \operatorname{AppellF1}\left[1+\frac{5+m}{2}, 2+m, 4, 1+\frac{7+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right] \right) \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \left. (a+b)(1+m) \left(\left(\left(3(a-b)(5+m) \operatorname{AppellF1}\left[1+\frac{5+m}{2}, 2+m, 4, 1+\frac{7+m}{2}, \right. \right. \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right] \right) / \left((a+b)(7+m) - \frac{1}{7+m} \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \left. (2+m)(5+m) \operatorname{AppellF1}\left[1+\frac{5+m}{2}, 3+m, 3, 1+\frac{7+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right] \right) \right) \right) \right) \Bigg) / \\
 & \left((3+m) \left(a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^3 \left(- (a+b)(5+m) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{3+m}{2}, 1+m, 3, \frac{5+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right. \right. \\
 & \quad \left. \left. \left. \left. \left. 2 \left(-3(a-b) \operatorname{AppellF1}\left[\frac{5+m}{2}, 1+m, 4, \frac{7+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b)(1+m) \operatorname{AppellF1}\left[\frac{5+m}{2}, 2+m, 3, \frac{7+m}{2}, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left(3 (a+b) (7+m) \operatorname{AppellF1} \left[\frac{5+m}{2}, 1+m, 3, \frac{7+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \right. \\
 & \quad \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^4 \left(\frac{\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]}{1 + \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2} \right)^{1+m} \\
 & \left(2 \left(-3 (a-b) \operatorname{AppellF1} \left[\frac{7+m}{2}, 1+m, 4, \frac{9+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \right. \right. \\
 & \quad \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) (1+m) \operatorname{AppellF1} \left[\frac{7+m}{2}, 2+m, 3, \right. \\
 & \quad \left. \frac{9+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \right) \\
 & \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] - (a+b) (7+m) \left(\left(3 (a-b) (5+m) \operatorname{AppellF1} \left[1 + \frac{5+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. 1+m, 4, 1 + \frac{7+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \\
 & \left. \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) / \left((a+b) (7+m) - \frac{1}{7+m} \right) \\
 & (1+m) (5+m) \operatorname{AppellF1} \left[1 + \frac{5+m}{2}, 2+m, 3, 1 + \frac{7+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \\
 & \quad \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) + \\
 & 2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \left(-3 (a-b) \left(\left(4 (a-b) (7+m) \operatorname{AppellF1} \left[1 + \frac{7+m}{2}, 1+m, \right. \right. \right. \right. \\
 & \quad \left. \left. 5, 1 + \frac{9+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) / \left((a+b) (9+m) - \frac{1}{9+m} \right) \\
 & (1+m) (7+m) \operatorname{AppellF1} \left[1 + \frac{7+m}{2}, 2+m, 4, 1 + \frac{9+m}{2}, -\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \\
 & \quad \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) + \\
 & (a+b) (1+m) \left(\left(3 (a-b) (7+m) \operatorname{AppellF1} \left[1 + \frac{7+m}{2}, 2+m, 4, 1 + \frac{9+m}{2}, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \\
 & \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) / \left((a+b)(9+m) - \frac{1}{9+m} \right. \\
 & \left. (2+m)(7+m) \operatorname{AppellF1}\left[1+\frac{7+m}{2}, 3+m, 3, 1+\frac{9+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) \right) \right) / \\
 & \left((5+m) \left(a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^3 \left(- (a+b)(7+m) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{5+m}{2}, 1+m, 3, \frac{7+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \\
 & \left. 2 \left(-3(a-b) \operatorname{AppellF1}\left[\frac{7+m}{2}, 1+m, 4, \frac{9+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b)(1+m) \operatorname{AppellF1}\left[\frac{7+m}{2}, 2+m, 3, \frac{9+m}{2}, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) + \\
 & \left((a+b)(9+m) \operatorname{AppellF1}\left[\frac{7+m}{2}, 1+m, 3, \frac{9+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^6 \left(\frac{\tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{1+m} \\
 & \left(2 \left(-3(a-b) \operatorname{AppellF1}\left[\frac{9+m}{2}, 1+m, 4, \frac{11+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b)(1+m) \operatorname{AppellF1}\left[\frac{9+m}{2}, 2+m, 3, \right. \right. \\
 & \left. \left. \frac{11+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{2}(c+dx)\right] - (a+b)(9+m) \left(\left(3(a-b)(7+m) \operatorname{AppellF1}\left[1+\frac{7+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. 1+m, 4, 1+\frac{9+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right)^2 \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \left((a+b)(9+m) - \frac{1}{9+m} \right. \\
 & \quad \left. (1+m)(7+m) \operatorname{AppellF1}\left[1+\frac{7+m}{2}, 2+m, 3, 1+\frac{9+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \\
 & 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(-3(a-b) \left(\left(4(a-b)(9+m) \operatorname{AppellF1}\left[1+\frac{9+m}{2}, 1+m, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 5, 1+\frac{11+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right)^2 \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \left((a+b)(11+m) - \frac{1}{11+m} \right. \right. \\
 & \quad \left. \left. (1+m)(9+m) \operatorname{AppellF1}\left[1+\frac{9+m}{2}, 2+m, 4, 1+\frac{11+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
 & (a+b)(1+m) \left(\left(3(a-b)(9+m) \operatorname{AppellF1}\left[1+\frac{9+m}{2}, 2+m, 4, 1+\frac{11+m}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right)^2 \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \left((a+b)(11+m) - \frac{1}{11+m} \right. \\
 & \quad \left. (2+m)(9+m) \operatorname{AppellF1}\left[1+\frac{9+m}{2}, 3+m, 3, 1+\frac{11+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \\
 & \left((7+m) \left(a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^3 \left(- (a+b)(9+m) \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{7+m}{2}, 1+m, 3, \frac{9+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \\
 & 2 \left(-3(a-b) \text{AppellF1}\left[\frac{9+m}{2}, 1+m, 4, \frac{11+m}{2}, -\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b)(1+m) \text{AppellF1}\left[\frac{9+m}{2}, 2+m, 3, \frac{11+m}{2}, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right)
 \end{aligned}$$

Problem 268: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int (a+b \sec[c+dx])^n \sin[c+dx]^5 dx$$

Optimal (type 5, 150 leaves, 6 steps):

$$\begin{aligned}
 & \frac{1}{a^2 d (1+n)} b \text{Hypergeometric2F1}\left[2, 1+n, 2+n, 1+\frac{b \sec[c+dx]}{a}\right] (a+b \sec[c+dx])^{1+n} - \\
 & \frac{1}{a^4 d (1+n)} 2 b^3 \text{Hypergeometric2F1}\left[4, 1+n, 2+n, 1+\frac{b \sec[c+dx]}{a}\right] (a+b \sec[c+dx])^{1+n} + \\
 & \frac{1}{a^6 d (1+n)} b^5 \text{Hypergeometric2F1}\left[6, 1+n, 2+n, 1+\frac{b \sec[c+dx]}{a}\right] (a+b \sec[c+dx])^{1+n}
 \end{aligned}$$

Result (type 6, 8397 leaves):

$$\begin{aligned}
 & \left(16(a-b)(a+b \sec[c+dx])^n \sin[c+dx]^5 \right. \\
 & \quad \left(\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^n \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^{-4+n} \left(b+\frac{a-a \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^n \\
 & \quad \left(-\left(\left(20 \text{AppellF1}\left[3, n, -n, 4, \frac{2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \right. \right. \right. \\
 & \quad \left. \left. \left. \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) \right) / \\
 & \quad \left(-n \left(a \text{AppellF1}\left[4, n, 1-n, 5, \frac{2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] + \right. \right. \\
 & \quad \left. \left. (-a+b) \text{AppellF1}\left[4, 1+n, -n, 5, \frac{2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] + 2(a-b) \operatorname{AppellF1}\left[3, n, -n, 4, \right. \\
 & \left. \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right] + \\
 & \left(75 \operatorname{AppellF1}\left[4, n, -n, 5, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \right. \\
 & \left. \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) / \\
 & \left(-2n \left(a \operatorname{AppellF1}\left[5, n, 1-n, 6, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] + \right. \right. \\
 & \left. \left. (-a+b) \operatorname{AppellF1}\left[5, 1+n, -n, 6, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \right. \\
 & \left. \left. \left. \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] + 5(a-b) \operatorname{AppellF1}\left[4, n, -n, 5, \right. \right. \right. \\
 & \left. \left. \left. \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right) - \\
 & \left(18 \operatorname{AppellF1}\left[5, n, -n, 6, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \right) / \\
 & \left(-n \left(a \operatorname{AppellF1}\left[6, n, 1-n, 7, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] + \right. \right. \\
 & \left. \left. (-a+b) \operatorname{AppellF1}\left[6, 1+n, -n, 7, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \right. \\
 & \left. \left. \left. \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] + 3(a-b) \operatorname{AppellF1}\left[5, n, -n, 6, \right. \right. \right. \\
 & \left. \left. \left. \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right) / \\
 & \left(15d \left(\frac{16}{15} (a-b)n \left(\frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^n \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{-4+n} \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(-\frac{a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} - \right. \\
 & \left. \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left(a-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)}{\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^2} \right) \\
 & \left(b + \frac{a-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^{-1+n} \\
 & \left(-\left(\left(20 \operatorname{AppellF1}\left[3, n, -n, 4, \frac{2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \right. \right. \right. \\
 & \left. \left. \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) / \left(-n \left(a \operatorname{AppellF1}\left[4, n, 1-n, 5, \frac{2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{2a}{(a-b)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] + (-a+b) \operatorname{AppellF1}\left[4, 1+n, \right. \right. \right. \\
 & \left. \left. \left. -n, 5, \frac{2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \right) \right) + \\
 & \left. 2(a-b) \operatorname{AppellF1}\left[3, n, -n, 4, \frac{2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \\
 & \left. \left. \frac{2a}{(a-b)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right) + \\
 & \left(75 \operatorname{AppellF1}\left[4, n, -n, 5, \frac{2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \right. \\
 & \left. \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right) / \left(-2n \left(a \operatorname{AppellF1}\left[5, n, 1-n, 6, \frac{2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{2a}{(a-b)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] + (-a+b) \operatorname{AppellF1}\left[5, 1+n, \right. \right. \right. \\
 & \left. \left. \left. -n, 6, \frac{2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \right) \right) + \\
 & \left. 5(a-b) \operatorname{AppellF1}\left[4, n, -n, 5, \frac{2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \\
 & \left. \left. \frac{2a}{(a-b)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left(18 \operatorname{AppellF1} \left[5, n, -n, 6, \frac{2}{1 + \tan \left[\frac{1}{2} (c + dx) \right]^2}, \frac{2a}{(a-b) \left(1 + \tan \left[\frac{1}{2} (c + dx) \right]^2 \right)} \right] \right) / \\
 & \left(-n \left(a \operatorname{AppellF1} \left[6, n, 1-n, 7, \frac{2}{1 + \tan \left[\frac{1}{2} (c + dx) \right]^2}, \frac{2a}{(a-b) \left(1 + \tan \left[\frac{1}{2} (c + dx) \right]^2 \right)} \right] + \right. \right. \\
 & \quad (-a+b) \operatorname{AppellF1} \left[6, 1+n, -n, 7, \frac{2}{1 + \tan \left[\frac{1}{2} (c + dx) \right]^2}, \right. \\
 & \quad \left. \left. \frac{2a}{(a-b) \left(1 + \tan \left[\frac{1}{2} (c + dx) \right]^2 \right)} \right] \right) + 3(a-b) \operatorname{AppellF1} \left[5, n, -n, 6, \right. \\
 & \quad \left. \frac{2}{1 + \tan \left[\frac{1}{2} (c + dx) \right]^2}, \frac{2a}{(a-b) \left(1 + \tan \left[\frac{1}{2} (c + dx) \right]^2 \right)} \right] \left(1 + \tan \left[\frac{1}{2} (c + dx) \right]^2 \right) \right) \Bigg) + \\
 & \frac{16}{15} (a-b) (-4+n) \operatorname{Sec} \left[\frac{1}{2} (c + dx) \right]^2 \tan \left[\frac{1}{2} (c + dx) \right] \left(\frac{1}{1 - \tan \left[\frac{1}{2} (c + dx) \right]^2} \right)^n \\
 & \left(1 + \tan \left[\frac{1}{2} (c + dx) \right]^2 \right)^{-5+n} \\
 & \left(b + \frac{a - a \tan \left[\frac{1}{2} (c + dx) \right]^2}{1 + \tan \left[\frac{1}{2} (c + dx) \right]^2} \right)^n \\
 & \left(- \left(\left(20 \operatorname{AppellF1} \left[3, n, -n, 4, \frac{2}{1 + \tan \left[\frac{1}{2} (c + dx) \right]^2}, \frac{2a}{(a-b) \left(1 + \tan \left[\frac{1}{2} (c + dx) \right]^2 \right)} \right] \right) \right. \right. \\
 & \quad \left. \left. \left(1 + \tan \left[\frac{1}{2} (c + dx) \right]^2 \right)^2 \right) / \left(-n \left(a \operatorname{AppellF1} \left[4, n, 1-n, 5, \frac{2}{1 + \tan \left[\frac{1}{2} (c + dx) \right]^2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{2a}{(a-b) \left(1 + \tan \left[\frac{1}{2} (c + dx) \right]^2 \right)} \right] + (-a+b) \operatorname{AppellF1} \left[4, 1+n, \right. \right. \right. \\
 & \quad \left. \left. \left. -n, 5, \frac{2}{1 + \tan \left[\frac{1}{2} (c + dx) \right]^2}, \frac{2a}{(a-b) \left(1 + \tan \left[\frac{1}{2} (c + dx) \right]^2 \right)} \right] \right) \right) + \\
 & \quad 2(a-b) \operatorname{AppellF1} \left[3, n, -n, 4, \frac{2}{1 + \tan \left[\frac{1}{2} (c + dx) \right]^2}, \right. \\
 & \quad \left. \left. \frac{2a}{(a-b) \left(1 + \tan \left[\frac{1}{2} (c + dx) \right]^2 \right)} \right] \left(1 + \tan \left[\frac{1}{2} (c + dx) \right]^2 \right) \right) \Bigg) + \\
 & \left(75 \operatorname{AppellF1} \left[4, n, -n, 5, \frac{2}{1 + \tan \left[\frac{1}{2} (c + dx) \right]^2}, \frac{2a}{(a-b) \left(1 + \tan \left[\frac{1}{2} (c + dx) \right]^2 \right)} \right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \Bigg/ \left(-2n \left[a \operatorname{AppellF1}\left[5, n, 1-n, 6, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \right. \\
 & \quad \left. \left. \frac{2a}{(a-b)\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] + (-a+b) \operatorname{AppellF1}\left[5, 1+n, \right. \right. \\
 & \quad \left. \left. -n, 6, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b)\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] \right) + \\
 & 5(a-b) \operatorname{AppellF1}\left[4, n, -n, 5, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \\
 & \quad \left. \frac{2a}{(a-b)\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \Bigg) - \\
 & \left(18 \operatorname{AppellF1}\left[5, n, -n, 6, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b)\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] \right) \Bigg/ \\
 & \left(-n \left[a \operatorname{AppellF1}\left[6, n, 1-n, 7, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b)\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] + \right. \right. \\
 & \quad \left. \left. (-a+b) \operatorname{AppellF1}\left[6, 1+n, -n, 7, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \right. \\
 & \quad \left. \left. \frac{2a}{(a-b)\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] \right) + 3(a-b) \operatorname{AppellF1}\left[5, n, -n, 6, \right. \\
 & \quad \left. \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b)\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \Bigg) + \\
 & \frac{16}{15}(a-b)n \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(\frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^{1+n} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{-4+n} \\
 & \left(b + \frac{a - a \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^n \\
 & \left(- \left(\left(20 \operatorname{AppellF1}\left[3, n, -n, 4, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b)\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] \right) \right. \right. \\
 & \quad \left. \left. \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) \right) \Bigg/ \left(-n \left[a \operatorname{AppellF1}\left[4, n, 1-n, 5, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] + (-a+b) \operatorname{AppellF1}\left[4, 1+n, \right. \\
 & \left. -n, 5, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \right) + \\
 & 2(a-b) \operatorname{AppellF1}\left[3, n, -n, 4, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \\
 & \left. \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \Bigg) + \\
 & \left(75 \operatorname{AppellF1}\left[4, n, -n, 5, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \right. \\
 & \left. \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \Bigg) / \left(-2n \left(a \operatorname{AppellF1}\left[5, n, 1-n, 6, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \right. \\
 & \left. \left. \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] + (-a+b) \operatorname{AppellF1}\left[5, 1+n, \right. \right. \\
 & \left. \left. -n, 6, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \right) \right) + \\
 & 5(a-b) \operatorname{AppellF1}\left[4, n, -n, 5, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \\
 & \left. \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) - \\
 & \left(18 \operatorname{AppellF1}\left[5, n, -n, 6, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \right) / \\
 & \left(-n \left(a \operatorname{AppellF1}\left[6, n, 1-n, 7, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \right. \right. \\
 & \left. \left. (-a+b) \operatorname{AppellF1}\left[6, 1+n, -n, 7, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \right. \\
 & \left. \left. \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \right) \right) + 3(a-b) \operatorname{AppellF1}\left[5, n, -n, 6, \right. \\
 & \left. \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \Bigg) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{16}{15} (a-b) \left(\frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^n \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^{-4+n} \\
 & \left(b + \frac{a - a \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^n \\
 & \left(- \left(\left(40 \operatorname{AppellF1}\left[3, n, -n, 4, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b)\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right] \right) / \left(-n \left(a \operatorname{AppellF1}\left[\right. \right. \right. \right. \\
 & \quad \left. \left. \left. 4, n, 1-n, 5, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b)\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \right) + \right. \\
 & \quad \left. \left(-a+b \right) \operatorname{AppellF1}\left[4, 1+n, -n, 5, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \\
 & \quad \left. \left. \frac{2a}{(a-b)\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \right) + 2(a-b) \operatorname{AppellF1}\left[3, n, -n, 4, \right. \\
 & \quad \left. \left. \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b)\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) - \\
 & \left(20 \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \left(\left(3 a n \operatorname{AppellF1}\left[4, n, 1-n, 5, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{2a}{(a-b)\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \right. \right. \\
 & \quad \left. \left(2(a-b)\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) - \left(3 n \operatorname{AppellF1}\left[4, 1+n, -n, 5, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b)\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \right) \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \left(2 \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) \right) / \\
 & \left(-n \left(a \operatorname{AppellF1}\left[4, n, 1-n, 5, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b)\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \right) + \right. \\
 & \quad \left. \left(-a+b \right) \operatorname{AppellF1}\left[4, 1+n, -n, 5, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{2 a}{(a-b) \left(1+\tan \left[\frac{1}{2}(c+d x)\right]^2\right)} \right] + 2(a-b) \operatorname{AppellF1}\left[3, n, -n, 4, \right. \\
 & \left. \frac{2}{1+\tan \left[\frac{1}{2}(c+d x)\right]^2}, \frac{2 a}{(a-b) \left(1+\tan \left[\frac{1}{2}(c+d x)\right]^2\right)} \left(1+\tan \left[\frac{1}{2}(c+d x)\right]^2\right)\right] + \\
 & \left(75 \operatorname{AppellF1}\left[4, n, -n, 5, \frac{2}{1+\tan \left[\frac{1}{2}(c+d x)\right]^2}, \frac{2 a}{(a-b) \left(1+\tan \left[\frac{1}{2}(c+d x)\right]^2\right)} \right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \tan \left[\frac{1}{2}(c+d x)\right]\right) / \left(-2 n\right. \\
 & \left. \left(a \operatorname{AppellF1}\left[5, n, 1-n, 6, \frac{2}{1+\tan \left[\frac{1}{2}(c+d x)\right]^2}, \frac{2 a}{(a-b) \left(1+\tan \left[\frac{1}{2}(c+d x)\right]^2\right)}\right] + \right. \right. \\
 & \left. \left. (-a+b) \operatorname{AppellF1}\left[5, 1+n, -n, 6, \frac{2}{1+\tan \left[\frac{1}{2}(c+d x)\right]^2}, \right. \right. \right. \\
 & \left. \left. \left. \frac{2 a}{(a-b) \left(1+\tan \left[\frac{1}{2}(c+d x)\right]^2\right)}\right] + 5(a-b) \operatorname{AppellF1}\left[4, n, -n, 5, \right. \right. \right. \\
 & \left. \left. \frac{2}{1+\tan \left[\frac{1}{2}(c+d x)\right]^2}, \frac{2 a}{(a-b) \left(1+\tan \left[\frac{1}{2}(c+d x)\right]^2\right)} \left(1+\tan \left[\frac{1}{2}(c+d x)\right]^2\right)\right] + \right. \\
 & \left. \left(75 \left(1+\tan \left[\frac{1}{2}(c+d x)\right]^2\right)\left(\left(\frac{2 a}{(a-b) \left(1+\tan \left[\frac{1}{2}(c+d x)\right]^2\right)} \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \tan \left[\frac{1}{2}(c+d x)\right]\right) / \right. \right. \right. \\
 & \left. \left. \left. \left(5(a-b) \left(1+\tan \left[\frac{1}{2}(c+d x)\right]^2\right)^2\right) - \left(8 n \operatorname{AppellF1}\left[5, 1+n, -n, 6, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{2}{1+\tan \left[\frac{1}{2}(c+d x)\right]^2}, \frac{2 a}{(a-b) \left(1+\tan \left[\frac{1}{2}(c+d x)\right]^2\right)} \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \right. \right. \right. \\
 & \left. \left. \left. \tan \left[\frac{1}{2}(c+d x)\right]\right) / \left(5 \left(1+\tan \left[\frac{1}{2}(c+d x)\right]^2\right)^2\right)\right)\right) / \left(-2 n\right. \\
 & \left. \left(a \operatorname{AppellF1}\left[5, n, 1-n, 6, \frac{2}{1+\tan \left[\frac{1}{2}(c+d x)\right]^2}, \frac{2 a}{(a-b) \left(1+\tan \left[\frac{1}{2}(c+d x)\right]^2\right)}\right] + \right. \right. \\
 & \left. \left. (-a+b) \operatorname{AppellF1}\left[5, 1+n, -n, 6, \frac{2}{1+\tan \left[\frac{1}{2}(c+d x)\right]^2}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] + 5(a-b) \operatorname{AppellF1}\left[4, n, -n, 5, \right. \\
 & \left. \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right] - \\
 & \left(18 \left(\left(5a n \operatorname{AppellF1}\left[6, n, 1-n, 7, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) / \right. \\
 & \left. \left(3(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) - \left(5n \operatorname{AppellF1}\left[6, 1+n, -n, 7, \right. \right. \right. \\
 & \left. \left. \left. \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \right) \right) / \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) / \left(3 \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) \right) / \right. \\
 & \left. \left(-n \left(a \operatorname{AppellF1}\left[6, n, 1-n, 7, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] + \right. \right. \right. \\
 & \left. \left. \left. (-a+b) \operatorname{AppellF1}\left[6, 1+n, -n, 7, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \right) \right) + 3(a-b) \operatorname{AppellF1}\left[5, n, -n, 6, \right. \\
 & \left. \left. \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right] \right) + \\
 & \left(20 \operatorname{AppellF1}\left[3, n, -n, 4, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \right) \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \left(2(a-b) \operatorname{AppellF1}\left[3, n, -n, 4, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \\
 & \left. \left. \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 2(a-b) \right) \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left(\left(3a n \operatorname{AppellF1}\left[4, n, 1-n, 5, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{2 a}{(a-b) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)} \right] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] \Bigg/ \\
 & \left(2(a-b) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)^2\right) - \left(3 n \operatorname{AppellF1}\left[4, 1+n, -n, \right. \right. \\
 & \left. \left. 5, \frac{2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}, \frac{2 a}{(a-b) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)} \right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] \Bigg/ \left(2 \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)^2\right)\right) - \\
 & n \left(a \left(- \left(\left(\left(8 a(1-n) \operatorname{AppellF1}\left[5, n, 2-n, 6, \frac{2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}, \right. \right. \right. \right. \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{2 a}{(a-b) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)} \right] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] \right. \right. \right. \\
 & \left. \left. \left. \Bigg/ \left(5(a-b) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)^2\right)\right) - \left(8 n \operatorname{AppellF1}\left[5, \right. \right. \right. \right. \\
 & \left. \left. \left. 1+n, 1-n, 6, \frac{2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}, \frac{2 a}{(a-b) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)} \right] \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] \Bigg/ \left(5 \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)^2\right)\right) + \right. \right. \\
 & \left. \left. (-a+b) \left(\left(\left(\left(8 a n \operatorname{AppellF1}\left[5, 1+n, 1-n, 6, \frac{2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}, \right. \right. \right. \right. \right. \right. \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{2 a}{(a-b) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)} \right] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] \right. \right. \right. \\
 & \left. \left. \left. \Bigg/ \left(5(a-b) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)^2\right)\right) - \left(8(1+n) \operatorname{AppellF1}\left[5, 2+n, \right. \right. \right. \right. \\
 & \left. \left. \left. -n, 6, \frac{2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}, \frac{2 a}{(a-b) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)} \right] \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] \Bigg/ \left(5 \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)^2\right)\right) \right) \right) \Bigg/ \\
 & \left(-n \left(a \operatorname{AppellF1}\left[4, n, 1-n, 5, \frac{2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}, \frac{2 a}{(a-b) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)} \right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & (-a+b) \operatorname{AppellF1}\left[4, 1+n, -n, 5, \frac{2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \\
 & \left. \frac{2a}{(a-b)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] + 2(a-b) \operatorname{AppellF1}\left[3, n, -n, 4, \right. \\
 & \left. \frac{2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 - \\
 & \left(75 \operatorname{AppellF1}\left[4, n, -n, 5, \frac{2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] \right. \\
 & \left. \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \left(5(a-b) \operatorname{AppellF1}\left[4, n, -n, 5, \frac{2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \right. \\
 & \left. \left. \frac{2a}{(a-b)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 5(a-b) \right. \right. \\
 & \left. \left. \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \left(\left(8an \operatorname{AppellF1}\left[5, n, 1-n, 6, \frac{2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \right. \right. \right. \\
 & \left. \left. \frac{2a}{(a-b)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) \right) / \\
 & \left. \left(5(a-b)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right) - \left(8n \operatorname{AppellF1}\left[5, 1+n, -n, \right. \right. \right. \\
 & \left. \left. 6, \frac{2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) \right) / \left(5\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right) \right) - \\
 & 2n \left(a \left(- \left(\left(5a(1-n) \operatorname{AppellF1}\left[6, n, 2-n, 7, \frac{2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \right. \right. \right. \right. \right. \\
 & \left. \left. \frac{2a}{(a-b)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+ \right. \right. \right. \\
 & \left. \left. \left. dx)\right] \right) / \left(3(a-b)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right) \right) - \left(5n \operatorname{AppellF1}\left[6, \right. \right. \right. \\
 & \left. \left. 1+n, 1-n, 7, \frac{2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \left] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right] / \\
 & \left(3(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right) - \left(5n \operatorname{AppellF1}\left[6, 1+n, -n, \right. \right. \\
 & \left. \left. 7, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] \right. \\
 & \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right] / \left(3 \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right)\right) - \\
 & n \left(a \left(- \left(\left(\left(12a(1-n) \operatorname{AppellF1}\left[7, n, 2-n, 8, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \right. \right. \right. \right. \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+ \right. \right. \right. \\
 & \left. \left. \left. dx)\right]\right] / \left(7(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right) \right) - \left(12n \operatorname{AppellF1}\left[7, \right. \right. \right. \\
 & \left. \left. \left. 1+n, 1-n, 8, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] \right. \right. \\
 & \left. \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right] / \left(7 \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right) \right) \right) + \\
 & (-a+b) \left(\left(\left(\left(12an \operatorname{AppellF1}\left[7, 1+n, 1-n, 8, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \right. \right. \right. \right. \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right] / \right. \right. \\
 & \left. \left. \left. \left(7(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right) \right) - \left(12(1+n) \operatorname{AppellF1}\left[7, \right. \right. \right. \\
 & \left. \left. \left. 2+n, -n, 8, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] \right. \right. \\
 & \left. \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right] / \left(7 \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right) \right) \right) \right) \right) / \\
 & \left(-n \left(a \operatorname{AppellF1}\left[6, n, 1-n, 7, \frac{2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}, \frac{2a}{(a-b) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] \right) + \right.
 \end{aligned}$$

$$\begin{aligned} & (-a+b) \operatorname{AppellF1}\left[6, 1+n, -n, 7, \frac{2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \\ & \left. \frac{2a}{(a-b)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] + \\ & 3(a-b) \operatorname{AppellF1}\left[5, n, -n, 6, \frac{2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}, \right. \\ & \left. \frac{2a}{(a-b)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)}\right] \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) \right) \right) \end{aligned}$$

Problem 269: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int (a+b \operatorname{Sec}[c+dx])^n \operatorname{Sin}[c+dx]^3 dx$$

Optimal (type 5, 121 leaves, 3 steps):

$$\begin{aligned} & \frac{1}{6a^4d(1+n)} b(6a^2-b^2(2-3n+n^2)) \operatorname{Hypergeometric2F1}\left[2, 1+n, 2+n, 1+\frac{b \operatorname{Sec}[c+dx]}{a}\right] \\ & (a+b \operatorname{Sec}[c+dx])^{1+n} + \frac{\operatorname{Cos}[c+dx]^3 (a+b \operatorname{Sec}[c+dx])^{1+n} (2a-b(2-n) \operatorname{Sec}[c+dx])}{6a^2d} \end{aligned}$$

Result (type 6, 4523 leaves):

$$\begin{aligned} & \left(4(a-b)(b+a \operatorname{Cos}[c+dx])^n \left(\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right)^{-2+n}\right. \\ & \left(-\left(\left(9 \operatorname{AppellF1}\left[2, n, -n, 3, 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right) / \right. \right. \right. \\ & \left. \left(-2an \operatorname{AppellF1}\left[3, n, 1-n, 4, 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] + (a-b)\left(2n \right. \right. \right. \\ & \left. \left. \operatorname{AppellF1}\left[3, 1+n, -n, 4, 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] + 3 \operatorname{AppellF1}\left[\right. \right. \right. \\ & \left. \left. \left. 2, n, -n, 3, 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\right) \right) + \\ & \left(4 \operatorname{AppellF1}\left[3, n, -n, 4, 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right]\right) / \end{aligned}$$

$$\begin{aligned}
 & \left(-a n \operatorname{AppellF1}\left[4, n, 1-n, 5, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] + (a-b) \right. \\
 & \quad \left. \left(n \operatorname{AppellF1}\left[4, 1+n, -n, 5, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] + 2 \operatorname{AppellF1}\left[\right. \right. \right. \\
 & \quad \quad \left. \left. \left. 3, n, -n, 4, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \right) \\
 & \left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx] \right)^n (a+b \operatorname{Sec}[c+dx])^n \\
 & \operatorname{Sin}[c+dx]^3 \Big/ \left(3 \right. \\
 & d \\
 & \left. \left(-\frac{4}{3} a (a-b) n (b+a \cos[c+dx])^{-1+n} \left(\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right)^{-2+n} \right. \right. \\
 & \quad \left. \left(-\left(\left(9 \operatorname{AppellF1}\left[2, n, -n, 3, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big/ \left(-2 a n \operatorname{AppellF1}\left[3, n, 1-n, 4, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b} \right] + (a-b) \left(2 n \operatorname{AppellF1}\left[3, 1+n, -n, 4, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b} \right] + 3 \operatorname{AppellF1}\left[2, n, -n, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. 3, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) + \\
 & \quad \left(4 \operatorname{AppellF1}\left[3, n, -n, 4, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \right) \Big/ \\
 & \quad \left(-a n \operatorname{AppellF1}\left[4, n, 1-n, 5, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] + \right. \\
 & \quad \left. (a-b) \left(n \operatorname{AppellF1}\left[4, 1+n, -n, 5, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] + \right. \right. \\
 & \quad \quad \left. \left. 2 \operatorname{AppellF1}\left[3, n, -n, 4, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \frac{2 a \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2}{a-b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2\right)\right) \\
 & \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Sec}[c+d x]\right)^n \operatorname{Sin}[c+d x] + \frac{4}{3}(a-b)(-2+n) \\
 & (b+a \operatorname{Cos}[c+d x])^n \\
 & \left(\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2\right)^{-2+n} \\
 & \left(-\left(\left(9 \operatorname{AppellF1}\left[2, n, -n, 3, 2 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2, \frac{2 a \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2}{a-b}\right]\right.\right.\right. \\
 & \left.\left.\left.\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2\right) / \left(-2 a n \operatorname{AppellF1}\left[3, n, 1-n, 4, 2 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2, \right.\right.\right. \right. \\
 & \left.\left.\left.\frac{2 a \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2}{a-b}\right] + (a-b)\left(2 n \operatorname{AppellF1}\left[3, 1+n, -n, 4, \right.\right.\right. \right. \\
 & \left.\left.\left.2 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2, \frac{2 a \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2}{a-b}\right] + 3 \operatorname{AppellF1}\left[2, n, -n, \right.\right.\right. \right. \\
 & \left.\left.\left.3, 2 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2, \frac{2 a \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2}{a-b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2\right)\right)\right) + \\
 & \left(4 \operatorname{AppellF1}\left[3, n, -n, 4, 2 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2, \frac{2 a \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2}{a-b}\right]\right) / \\
 & \left(-a n \operatorname{AppellF1}\left[4, n, 1-n, 5, 2 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2, \frac{2 a \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2}{a-b}\right] + \right. \\
 & \left.(a-b)\left(n \operatorname{AppellF1}\left[4, 1+n, -n, 5, 2 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2, \frac{2 a \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2}{a-b}\right] + \right. \right. \\
 & \left.\left.2 \operatorname{AppellF1}\left[3, n, -n, 4, 2 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2, \right.\right.\right. \\
 & \left.\left.\left.\frac{2 a \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2}{a-b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2\right)\right)\right) \\
 & \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Sec}[c+d x]\right)^n \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + \frac{4}{3}(a-b) \\
 & (b+a \operatorname{Cos}[c+d x])^n \\
 & \left(\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2\right)^{-2+n} \\
 & \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Sec}[c+d x]\right)^n
 \end{aligned}$$

$$\begin{aligned}
 & \left(- \left(\left(9 \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \left(\frac{1}{3(a-b)} 4 a n \operatorname{AppellF1} [3, n, 1-n, 4, 2 \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{2 a \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2}{a-b} \right] \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right] \operatorname{Sin} \left[\frac{1}{2} (c+dx) \right] - \frac{4}{3} n \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{AppellF1} [3, 1+n, -n, 4, 2 \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2, \frac{2 a \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2}{a-b} \right] \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right] \operatorname{Sin} \left[\frac{1}{2} (c+dx) \right] \right) \right) \right) / \left(-2 a n \operatorname{AppellF1} [3, n, 1-n, 4, 2 \right. \\
 & \quad \left. \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2, \frac{2 a \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2}{a-b} \right] + (a-b) \left(2 n \operatorname{AppellF1} [3, 1+n, \right. \\
 & \quad \left. -n, 4, 2 \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2, \frac{2 a \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2}{a-b} \right] + 3 \operatorname{AppellF1} [2, n, \right. \\
 & \quad \left. -n, 3, 2 \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2, \frac{2 a \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2}{a-b} \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \right) \right) \right) + \\
 & \left(4 \left(\frac{1}{2(a-b)} 3 a n \operatorname{AppellF1} [4, n, 1-n, 5, 2 \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2, \frac{2 a \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2}{a-b} \right] \right. \right. \\
 & \quad \left. \left. \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right] \operatorname{Sin} \left[\frac{1}{2} (c+dx) \right] - \frac{3}{2} n \operatorname{AppellF1} [4, 1+n, -n, 5, 2 \right. \right. \\
 & \quad \left. \left. \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2, \frac{2 a \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2}{a-b} \right] \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right] \operatorname{Sin} \left[\frac{1}{2} (c+dx) \right] \right) \right) / \\
 & \left(-a n \operatorname{AppellF1} [4, n, 1-n, 5, 2 \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2, \frac{2 a \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2}{a-b} \right] + \right. \\
 & \quad \left. (a-b) \left(n \operatorname{AppellF1} [4, 1+n, -n, 5, 2 \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2, \frac{2 a \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2}{a-b} \right] + \right. \\
 & \quad \left. 2 \operatorname{AppellF1} [3, n, -n, 4, 2 \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2, \right. \\
 & \quad \left. \left. \frac{2 a \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2}{a-b} \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \right) \right) - \\
 & \left(9 \operatorname{AppellF1} [2, n, -n, 3, 2 \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2, \frac{2 a \operatorname{Cos} \left[\frac{1}{2} (c+dx) \right]^2}{a-b} \right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sin\left[\frac{1}{2}(c+dx)\right]\right)^2 + 3 \operatorname{AppellF1}\left[2, n, -n, 3, 2 \cos\left[\frac{1}{2}(c+dx)\right]\right]^2, \\
 & \left. \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \Bigg) \Bigg) / \\
 & \left(-2an \operatorname{AppellF1}\left[3, n, 1-n, 4, 2 \cos\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] + \right. \\
 & (a-b) \left(2n \operatorname{AppellF1}\left[3, 1+n, -n, 4, 2 \cos\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] + \right. \\
 & 3 \operatorname{AppellF1}\left[2, n, -n, 3, 2 \cos\left[\frac{1}{2}(c+dx)\right]\right]^2, \\
 & \left. \left. \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right)^2 - \\
 & \left(4 \operatorname{AppellF1}\left[3, n, -n, 4, 2 \cos\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \right. \\
 & \left(-an \left(-\frac{1}{5(a-b)} 8a(1-n) \operatorname{AppellF1}\left[5, n, 2-n, 6, 2 \cos\left[\frac{1}{2}(c+dx)\right]\right]^2, \right. \right. \\
 & \left. \left. \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \cos\left[\frac{1}{2}(c+dx)\right] \sin\left[\frac{1}{2}(c+dx)\right] - \frac{8}{5}n \operatorname{AppellF1}\left[5, \right. \right. \\
 & \left. \left. 1+n, 1-n, 6, 2 \cos\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \cos\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \left. \sin\left[\frac{1}{2}(c+dx)\right] \right) + (a-b) \left(2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(\frac{1}{2(a-b)} 3an \operatorname{AppellF1}\left[4, \right. \right. \right. \\
 & \left. \left. n, 1-n, 5, 2 \cos\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \cos\left[\frac{1}{2}(c+dx)\right] \right. \\
 & \left. \sin\left[\frac{1}{2}(c+dx)\right] - \frac{3}{2}n \operatorname{AppellF1}\left[4, 1+n, -n, 5, 2 \cos\left[\frac{1}{2}(c+dx)\right]\right]^2, \right. \\
 & \left. \left. \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \cos\left[\frac{1}{2}(c+dx)\right] \sin\left[\frac{1}{2}(c+dx)\right] \right) + n \left(\frac{1}{5(a-b)} \right. \\
 & \left. 8an \operatorname{AppellF1}\left[5, 1+n, 1-n, 6, 2 \cos\left[\frac{1}{2}(c+dx)\right]\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \right. \\
 & \left. \cos\left[\frac{1}{2}(c+dx)\right] \sin\left[\frac{1}{2}(c+dx)\right] - \frac{8}{5}(1+n) \operatorname{AppellF1}\left[5, 2+n, -n, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 6, 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2}{a-b} \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \\
 & \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \Bigg) + 2 \operatorname{AppellF1}\left[3, n, -n, 4, 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{2a \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2}{a-b} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right] \Bigg) \Bigg) / \\
 & \left(-a n \operatorname{AppellF1}\left[4, n, 1-n, 5, 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2}{a-b} \right] + \right. \\
 & (a-b) \left(n \operatorname{AppellF1}\left[4, 1+n, -n, 5, 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2}{a-b} \right] + \right. \\
 & \left. 2 \operatorname{AppellF1}\left[3, n, -n, 4, 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{2a \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2}{a-b} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \Bigg) \Bigg) + \\
 & \frac{4}{3} (a-b) n (b+a \operatorname{Cos}[c+dx])^n \left(\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right)^{-2+n} \\
 & \left(- \left(\left(9 \operatorname{AppellF1}\left[2, n, -n, 3, 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{2a \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2}{a-b} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \Bigg) / \right. \\
 & \left(-2 a n \operatorname{AppellF1}\left[3, n, 1-n, 4, 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2}{a-b} \right] + \right. \\
 & (a-b) \left(2 n \operatorname{AppellF1}\left[3, 1+n, -n, 4, 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2}{a-b} \right] + \right. \\
 & \left. 3 \operatorname{AppellF1}\left[2, n, -n, 3, 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{2a \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2}{a-b} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \Bigg) \Bigg) + \\
 & \left(4 \operatorname{AppellF1}\left[3, n, -n, 4, 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2}{a-b} \right] \right) /
 \end{aligned}$$

$$\begin{aligned} & \left(-a n \operatorname{AppellF1}\left[4, n, 1-n, 5, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] + \right. \\ & \quad (a-b) \left(n \operatorname{AppellF1}\left[4, 1+n, -n, 5, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] + \right. \\ & \quad \quad 2 \operatorname{AppellF1}\left[3, n, -n, 4, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \right. \\ & \quad \quad \quad \left. \left. \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\ & \left. \left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx] \right)^{-1+n} \left(-\cos\left[\frac{1}{2}(c+dx)\right] \operatorname{Sec}[c+dx] \right. \right. \\ & \quad \left. \left. \sin\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\ & \quad \left. \left. \cos\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx] \operatorname{Tan}[c+dx] \right) \right) \right) \end{aligned}$$

Problem 270: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int (a+b \operatorname{Sec}[c+dx])^n \sin[c+dx] dx$$

Optimal (type 5, 48 leaves, 2 steps):

$$\frac{1}{a^2 d (1+n)} b \operatorname{Hypergeometric2F1}\left[2, 1+n, 2+n, 1 + \frac{b \operatorname{Sec}[c+dx]}{a}\right] (a+b \operatorname{Sec}[c+dx])^{1+n}$$

Result (type 6, 1849 leaves):

$$\begin{aligned} & - \left(\left(2(a-b) \operatorname{AppellF1}\left[1, n, -n, 2, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \right. \right. \\ & \quad \left. \left. (b+a \cos[c+dx])^n \operatorname{Sec}[c+dx]^n (a+b \operatorname{Sec}[c+dx])^n \sin[c+dx] \right) \right) / \\ & \left(d \left(-a n \operatorname{AppellF1}\left[2, n, 1-n, 3, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] + \right. \right. \\ & \quad (a-b) \left(n \operatorname{AppellF1}\left[2, 1+n, -n, 3, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] + \right. \\ & \quad \quad \left. \left. \operatorname{AppellF1}\left[1, n, -n, 2, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \left(- \left(\left(2 (a-b) (b+a \cos [c+dx])^n \sec [c+dx]^n \left(\frac{1}{a-b} a n \operatorname{AppellF1} [2, n, 1-n, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 3, 2 \cos \left[\frac{1}{2} (c+dx) \right]^2, \frac{2 a \cos \left[\frac{1}{2} (c+dx) \right]^2}{a-b} \right] \cos \left[\frac{1}{2} (c+dx) \right] \sin \left[\right. \right. \right. \\
 & \quad \left. \left. \left. \frac{1}{2} (c+dx) \right] - n \operatorname{AppellF1} [2, 1+n, -n, 3, 2 \cos \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{2 a \cos \left[\frac{1}{2} (c+dx) \right]^2}{a-b} \right] \cos \left[\frac{1}{2} (c+dx) \right] \sin \left[\frac{1}{2} (c+dx) \right] \right) \right) \Bigg/ \\
 & \left(-a n \operatorname{AppellF1} [2, n, 1-n, 3, 2 \cos \left[\frac{1}{2} (c+dx) \right]^2, \frac{2 a \cos \left[\frac{1}{2} (c+dx) \right]^2}{a-b}] + (a-b) \right. \\
 & \quad \left(n \operatorname{AppellF1} [2, 1+n, -n, 3, 2 \cos \left[\frac{1}{2} (c+dx) \right]^2, \frac{2 a \cos \left[\frac{1}{2} (c+dx) \right]^2}{a-b}] + \operatorname{AppellF1} [\right. \\
 & \quad \left. \left. 1, n, -n, 2, 2 \cos \left[\frac{1}{2} (c+dx) \right]^2, \frac{2 a \cos \left[\frac{1}{2} (c+dx) \right]^2}{a-b} \right] \sec \left[\frac{1}{2} (c+dx) \right]^2 \right) \Bigg) \Bigg) + \\
 & \left(2 a (a-b) n \operatorname{AppellF1} [1, n, -n, 2, 2 \cos \left[\frac{1}{2} (c+dx) \right]^2, \frac{2 a \cos \left[\frac{1}{2} (c+dx) \right]^2}{a-b}] \right. \\
 & \quad \left. (b+a \cos [c+dx])^{-1+n} \sec [c+dx]^n \sin [c+dx] \right) \Bigg/ \\
 & \left(-a n \operatorname{AppellF1} [2, n, 1-n, 3, 2 \cos \left[\frac{1}{2} (c+dx) \right]^2, \frac{2 a \cos \left[\frac{1}{2} (c+dx) \right]^2}{a-b}] + (a-b) \right. \\
 & \quad \left(n \operatorname{AppellF1} [2, 1+n, -n, 3, 2 \cos \left[\frac{1}{2} (c+dx) \right]^2, \frac{2 a \cos \left[\frac{1}{2} (c+dx) \right]^2}{a-b}] + \operatorname{AppellF1} [1, \right. \\
 & \quad \left. \left. n, -n, 2, 2 \cos \left[\frac{1}{2} (c+dx) \right]^2, \frac{2 a \cos \left[\frac{1}{2} (c+dx) \right]^2}{a-b} \right] \sec \left[\frac{1}{2} (c+dx) \right]^2 \right) \Bigg) \Bigg) - \\
 & \left(2 (a-b) n \operatorname{AppellF1} [1, n, -n, 2, 2 \cos \left[\frac{1}{2} (c+dx) \right]^2, \frac{2 a \cos \left[\frac{1}{2} (c+dx) \right]^2}{a-b}] \right. \\
 & \quad \left. (b+a \cos [c+dx])^n \sec [c+dx]^{1+n} \sin [c+dx] \right) \Bigg/ \\
 & \left(-a n \operatorname{AppellF1} [2, n, 1-n, 3, 2 \cos \left[\frac{1}{2} (c+dx) \right]^2, \frac{2 a \cos \left[\frac{1}{2} (c+dx) \right]^2}{a-b}] + (a-b) \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(n \operatorname{AppellF1}\left[2, 1+n, -n, 3, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] + \operatorname{AppellF1}\left[1, \right. \right. \\
 & \quad \left. \left. n, -n, 2, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) + \\
 & \left(2(a-b) \operatorname{AppellF1}\left[1, n, -n, 2, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \right) \\
 & (b+a \cos[c+dx])^n \operatorname{Sec}[c+dx]^n \left(-a n \left(-\frac{1}{3(a-b)} 4a(1-n) \operatorname{AppellF1}\left[3, n, 2-n, 4, \right. \right. \right. \\
 & \quad \left. \left. 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \cos\left[\frac{1}{2}(c+dx)\right] \sin\left[\frac{1}{2}(c+dx)\right] - \right. \right. \\
 & \quad \left. \left. \frac{4}{3} n \operatorname{AppellF1}\left[3, 1+n, 1-n, 4, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \right. \right. \\
 & \quad \left. \left. \cos\left[\frac{1}{2}(c+dx)\right] \sin\left[\frac{1}{2}(c+dx)\right] \right) + (a-b) \left(\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \quad \left. \left. \left(\frac{1}{a-b} a n \operatorname{AppellF1}\left[2, n, 1-n, 3, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \right. \right. \right. \\
 & \quad \left. \left. \cos\left[\frac{1}{2}(c+dx)\right] \sin\left[\frac{1}{2}(c+dx)\right] - n \operatorname{AppellF1}\left[2, 1+n, -n, 3, 2 \cos\left[\frac{1}{2}(c+ \right. \right. \right. \right. \\
 & \quad \left. \left. \left. dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \cos\left[\frac{1}{2}(c+dx)\right] \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
 & n \left(\frac{1}{3(a-b)} 4a n \operatorname{AppellF1}\left[3, 1+n, 1-n, 4, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \cos\left[\frac{1}{2}(c+dx)\right] \sin\left[\frac{1}{2}(c+dx)\right] - \frac{4}{3}(1+n) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[3, 2+n, -n, 4, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \cos\left[\frac{1}{2}(c+dx)\right] \right. \right. \\
 & \quad \left. \left. \sin\left[\frac{1}{2}(c+dx)\right] \right) + \operatorname{AppellF1}\left[1, n, -n, 2, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{2a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) /
 \end{aligned}$$

$$\left(-a n \operatorname{AppellF1}\left[2, n, 1-n, 3, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2 a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] + \right. \\ \left. (a-b) \left(n \operatorname{AppellF1}\left[2, 1+n, -n, 3, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \frac{2 a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] + \right. \right. \\ \left. \left. \operatorname{AppellF1}\left[1, n, -n, 2, 2 \cos\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\ \left. \left. \left. \frac{2 a \cos\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right)$$

Problem 271: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \operatorname{Csc}[c+dx] (a+b \operatorname{Sec}[c+dx])^n dx$$

Optimal (type 5, 115 leaves, 6 steps):

$$\frac{\operatorname{Hypergeometric2F1}\left[1, 1+n, 2+n, \frac{a+b \operatorname{Sec}[c+dx]}{a-b}\right] (a+b \operatorname{Sec}[c+dx])^{1+n}}{2(a-b)d(1+n)} - \frac{\left(\operatorname{Hypergeometric2F1}\left[1, 1+n, 2+n, \frac{a+b \operatorname{Sec}[c+dx]}{a+b}\right] (a+b \operatorname{Sec}[c+dx])^{1+n}\right)}{(2(a+b)d(1+n))}$$

Result (type 6, 3438 leaves):

$$\left(b(-2+n) \operatorname{AppellF1}\left[1-n, -n, 1, 2-n, \frac{(-a+b) \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2b}, \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\ \left. (b+a \cos[c+dx])^n \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Csc}[c+dx] \operatorname{Sec}[c+dx]^{-1+n} (a+b \operatorname{Sec}[c+dx])^n \right) / \\ \left(d(-1+n) \left(2b(-2+n) \operatorname{AppellF1}\left[1-n, -n, 1, 2-n, \frac{(-a+b) \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2b}, \right. \right. \right. \\ \left. \left. \left. \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right] \cos\left[\frac{1}{2}(c+dx)\right]^2 + \right. \right. \right. \\ \left. \left. \left. - (a-b)n \operatorname{AppellF1}\left[2-n, 1-n, 1, 3-n, \frac{(-a+b) \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2b}, \right. \right. \right. \right. \\ \left. \left. \left. \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right] - 2b \operatorname{AppellF1}\left[2-n, -n, 2, 3-n, \right. \right. \right. \right)$$

$$\begin{aligned}
 & \left. \frac{(-a+b) \cos [c+dx] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2}{2b}, \cos [c+dx] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \right) \cos [c+dx] \Bigg) \\
 & \left(- \left(\left(b (-2+n) \operatorname{AppellF1} [1-n, -n, 1, 2-n, \frac{(-a+b) \cos [c+dx] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2}{2b}], \right. \right. \right. \\
 & \quad \cos [c+dx] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 (b+a \cos [c+dx])^n \cot \left[\frac{1}{2} (c+dx) \right] \operatorname{Csc} \left[\frac{1}{2} (c+dx) \right]^2 \\
 & \quad \left. \operatorname{Sec} [c+dx]^{-1+n} \right) / \left((-1+n) \left(2b (-2+n) \operatorname{AppellF1} [1-n, -n, 1, 2-n, \right. \right. \\
 & \quad \left. \left. \frac{(-a+b) \cos [c+dx] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2}{2b}, \cos [c+dx] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \right] \right. \\
 & \quad \left. \cos \left[\frac{1}{2} (c+dx) \right]^2 + \left(- (a-b) n \operatorname{AppellF1} [2-n, 1-n, 1, 3-n, \right. \right. \\
 & \quad \left. \left. \frac{(-a+b) \cos [c+dx] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2}{2b}, \cos [c+dx] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \right) - 2 \right. \\
 & \quad \left. b \operatorname{AppellF1} [2-n, -n, 2, 3-n, \frac{(-a+b) \cos [c+dx] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2}{2b}], \right. \\
 & \quad \left. \left. \left. \cos [c+dx] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \right) \cos [c+dx] \right) \right) \Bigg) - \\
 & \left(a b (-2+n) n \operatorname{AppellF1} [1-n, -n, 1, 2-n, \frac{(-a+b) \cos [c+dx] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2}{2b}], \right. \\
 & \quad \left. \cos [c+dx] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 (b+a \cos [c+dx])^{-1+n} \right. \\
 & \quad \left. \cot \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Sec} [c+dx]^{-1+n} \sin [c+dx] \right) / \\
 & \left((-1+n) \left(2b (-2+n) \operatorname{AppellF1} [1-n, -n, 1, 2-n, \frac{(-a+b) \cos [c+dx] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2}{2b}], \right. \right. \\
 & \quad \left. \left. \cos [c+dx] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \cos \left[\frac{1}{2} (c+dx) \right]^2 + \left(- (a-b) n \operatorname{AppellF1} [2-n, 1-n, \right. \right. \right. \\
 & \quad \left. \left. \left. 1, 3-n, \frac{(-a+b) \cos [c+dx] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2}{2b}, \cos [c+dx] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \right) - \right. \right. \\
 & \quad \left. \left. 2b \operatorname{AppellF1} [2-n, -n, 2, 3-n, \frac{(-a+b) \cos [c+dx] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2}{2b}], \right. \right. \\
 & \quad \left. \left. \left. \cos [c+dx] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \right) \cos [c+dx] \right) \right) \Bigg) -
 \end{aligned}$$

$$\begin{aligned}
 & \left((-1+n) \left(2b(-2+n) \operatorname{AppellF1}\left[1-n, -n, 1, 2-n, \frac{(-a+b) \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2b}\right], \right. \right. \\
 & \quad \left. \left. \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) \cos\left[\frac{1}{2}(c+dx)\right]^2 + \left(-(a-b)n \operatorname{AppellF1}\left[2-n, 1-n, \right. \right. \right. \\
 & \quad \left. \left. \left. 1, 3-n, \frac{(-a+b) \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2b}, \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right] - \right. \right. \\
 & \quad \left. \left. 2b \operatorname{AppellF1}\left[2-n, -n, 2, 3-n, \frac{(-a+b) \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2b}, \right. \right. \right. \\
 & \quad \left. \left. \left. \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \cos[c+dx] \right) \right) - \\
 & \left(b(-2+n) \operatorname{AppellF1}\left[1-n, -n, 1, 2-n, \frac{(-a+b) \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2b}, \right. \right. \\
 & \quad \left. \left. \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) (b+a \cos[c+dx])^n \cot\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx]^{-1+n} \right. \\
 & \quad \left. \left(-2b(-2+n) \operatorname{AppellF1}\left[1-n, -n, 1, 2-n, \frac{(-a+b) \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2b}, \right. \right. \right. \\
 & \quad \left. \left. \left. \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) \cos\left[\frac{1}{2}(c+dx)\right] \sin\left[\frac{1}{2}(c+dx)\right] - \right. \right. \\
 & \quad \left. \left(-(a-b)n \operatorname{AppellF1}\left[2-n, 1-n, 1, 3-n, \frac{(-a+b) \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2b}, \right. \right. \right. \\
 & \quad \left. \left. \left. \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) - 2b \operatorname{AppellF1}\left[2-n, -n, 2, 3-n, \right. \right. \right. \\
 & \quad \left. \left. \left. n, \frac{(-a+b) \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2b}, \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \right) \\
 & \quad \sin[c+dx] + 2b(-2+n) \cos\left[\frac{1}{2}(c+dx)\right]^2 \left(\frac{1}{2-n} (1-n) \operatorname{AppellF1}\left[2-n, -n, \right. \right. \\
 & \quad \left. \left. 2, 3-n, \frac{(-a+b) \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2b}, \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \\
 & \quad \left(-\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \sin[c+dx] + \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] \right) - \frac{1}{2-n} (1-n)n \operatorname{AppellF1}\left[2-n, 1-n, 1, 3-n, \right. \\
 & \quad \left. \frac{(-a+b) \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2b}, \cos[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(-\frac{(-a+b) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sin}[c+dx]}{2b} + \frac{1}{2b}(-a+b) \operatorname{Cos}[c+dx] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + \operatorname{Cos}[c+dx] \left(-2b \left(\frac{1}{3-n} \right. \right. \\
 & \left. \left. 2(2-n) \operatorname{AppellF1}\left[3-n, -n, 3, 4-n, \frac{(-a+b) \operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2b}, \right. \right. \right. \\
 & \left. \left. \operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right] \left(-\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sin}[c+dx] + \right. \right. \\
 & \left. \left. \operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) - \frac{1}{3-n}(2-n)n \right. \\
 & \left. \operatorname{AppellF1}\left[3-n, 1-n, 2, 4-n, \frac{(-a+b) \operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2b}, \right. \right. \\
 & \left. \left. \operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right] \left(-\frac{(-a+b) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sin}[c+dx]}{2b} + \frac{1}{2b} \right. \right. \\
 & \left. \left. (-a+b) \operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) - (a-b)n \left(\frac{1}{3-n} \right. \\
 & \left. (2-n) \operatorname{AppellF1}\left[3-n, 1-n, 2, 4-n, \frac{(-a+b) \operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2b}, \right. \right. \\
 & \left. \left. \operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right] \left(-\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sin}[c+dx] + \right. \right. \\
 & \left. \left. \operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + \frac{1}{3-n}(1-n)(2-n) \right. \\
 & \left. \operatorname{AppellF1}\left[3-n, 2-n, 1, 4-n, \frac{(-a+b) \operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2b}, \right. \right. \\
 & \left. \left. \operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right] \left(-\frac{(-a+b) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sin}[c+dx]}{2b} + \right. \right. \\
 & \left. \left. \frac{1}{2b}(-a+b) \operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \\
 & \left((-1+n) \left(2b(-2+n) \operatorname{AppellF1}\left[1-n, -n, 1, 2-n, \frac{(-a+b) \operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2b}, \right. \right. \right. \\
 & \left. \left. \operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right] \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 + \right. \right. \\
 & \left. \left(-(a-b)n \operatorname{AppellF1}\left[2-n, 1-n, 1, 3-n, \frac{(-a+b) \operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2b}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(a - a \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}{\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2} \right) \\
 & \left(b + \frac{a - a \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{-1+n} \\
 & \left(- \left(\left((a-b) \operatorname{AppellF1}\left[1, n, -n, 2, \cot\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a+b) \cot\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \right) / \right. \right. \\
 & \quad \left(-n \left((a+b) \operatorname{AppellF1}\left[2, n, 1-n, 3, \cot\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a+b) \cot\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \right) + \right. \\
 & \quad \quad \left. (-a+b) \operatorname{AppellF1}\left[2, 1+n, -n, 3, \cot\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a+b) \cot\left[\frac{1}{2}(c+dx)\right]^2}{a-b} \right] \right) + 2(a-b) \operatorname{AppellF1}\left[1, n, -n, 2, \right. \\
 & \quad \quad \left. \cot\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a+b) \cot\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \left((a+b) \operatorname{AppellF1}\left[1, n, -n, 2, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) / \\
 & \left(2(a+b) \operatorname{AppellF1}\left[1, n, -n, 2, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \quad n \left((-a+b) \operatorname{AppellF1}\left[2, n, 1-n, 3, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \\
 & \quad \quad (a+b) \operatorname{AppellF1}\left[2, 1+n, -n, 3, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \quad \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 - \\
 & \left(2b(-2+n) \operatorname{AppellF1}\left[1-n, -n, 1, 2-n, \frac{(a-b) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}, \right. \right. \\
 & \quad \left. \left. 1 - \tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \cot\left[\frac{1}{2}(c+dx)\right]^2 \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left((-1+n) \left(2b(-2+n) \operatorname{AppellF1}\left[1-n, -n, 1, 2-n, \frac{(a-b)\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}\right], \right. \right. \\
 & \quad \left. \left. 1-\tan\left[\frac{1}{2}(c+dx)\right]^2\right) + \left((a-b)n \operatorname{AppellF1}\left[2-n, 1-n, 1, 3-n, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b)\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}, 1-\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. 2b \operatorname{AppellF1}\left[2-n, -n, 2, 3-n, \frac{(a-b)\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}\right], \right. \right. \\
 & \quad \left. \left. 1-\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \Bigg) + \\
 & \frac{1}{4} n \left(\frac{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{-1+n} \left(\frac{\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} + \right. \\
 & \quad \left. \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)}{\left(1-\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2} \right) \left(b + \frac{a-a \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^n \\
 & \left(- \left(\left((a-b) \operatorname{AppellF1}\left[1, n, -n, 2, \cot\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a+b) \cot\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \right) / \right. \right. \\
 & \quad \left. \left(-n \left((a+b) \operatorname{AppellF1}\left[2, n, 1-n, 3, \cot\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a+b) \cot\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \right) + \right. \right. \\
 & \quad \quad \left. \left. (-a+b) \operatorname{AppellF1}\left[2, 1+n, -n, 3, \cot\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{(a+b) \cot\left[\frac{1}{2}(c+dx)\right]^2}{a-b} \right) \right) + 2(a-b) \operatorname{AppellF1}\left[1, n, -n, 2, \right. \\
 & \quad \left. \cot\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a+b) \cot\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg) + \\
 & \left((a+b) \operatorname{AppellF1}\left[1, n, -n, 2, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) / \\
 & \left(2(a+b) \operatorname{AppellF1}\left[1, n, -n, 2, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) +
 \end{aligned}$$

$$\begin{aligned}
 & n \left((-a+b) \operatorname{AppellF1}\left[2, n, 1-n, 3, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \quad (a+b) \operatorname{AppellF1}\left[2, 1+n, -n, 3, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 - \\
 & \left(2b(-2+n) \operatorname{AppellF1}\left[1-n, -n, 1, 2-n, \frac{(a-b) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}, \right. \right. \\
 & \quad \left. \left. 1 - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \cot\left[\frac{1}{2}(c+dx)\right]^2 \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) / \\
 & \left((-1+n) \left(2b(-2+n) \operatorname{AppellF1}\left[1-n, -n, 1, 2-n, \frac{(a-b) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}, \right. \right. \right. \\
 & \quad \left. \left. 1 - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \left((a-b) n \operatorname{AppellF1}\left[2-n, 1-n, 1, 3-n, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}, 1 - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. 2b \operatorname{AppellF1}\left[2-n, -n, 2, 3-n, \frac{(a-b) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}, \right. \right. \right. \\
 & \quad \left. \left. \left. 1 - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right) + \\
 & \frac{1}{4} \left(\frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^n \left(\frac{a - a \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^n \\
 & \left(- \left((a-b) \left(\frac{1}{2(a-b)} (a+b) n \operatorname{AppellF1}\left[2, n, 1-n, 3, \cot\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \frac{(a+b) \cot\left[\frac{1}{2}(c+dx)\right]^2}{a-b} \right] \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 - \frac{1}{2} n \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[2, 1+n, -n, 3, \cot\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a+b) \cot\left[\frac{1}{2}(c+dx)\right]^2}{a-b} \right] \right. \right. \\
 & \quad \left. \left. \left. \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left(-n \left((a+b) \operatorname{AppellF1}\left[2, n, 1-n, 3, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left(\cot \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a+b) \cot \left[\frac{1}{2} (c+dx) \right]^2}{a-b} \right] + (-a+b) \operatorname{AppellF1} \left[2, 1+n, \right. \right. \\
 & \left. \left. -n, 3, \cot \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a+b) \cot \left[\frac{1}{2} (c+dx) \right]^2}{a-b} \right] \right) + 2(a-b) \operatorname{AppellF1} \left[1, \right. \\
 & \left. n, -n, 2, \cot \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a+b) \cot \left[\frac{1}{2} (c+dx) \right]^2}{a-b} \right] \tan \left[\frac{1}{2} (c+dx) \right]^2 \right) + \\
 & \left((a+b) \operatorname{AppellF1} \left[1, n, -n, 2, \tan \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \\
 & \left. \sec \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] \right) / \\
 & \left(2(a+b) \operatorname{AppellF1} \left[1, n, -n, 2, \tan \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \left. n \left((-a+b) \operatorname{AppellF1} \left[2, n, 1-n, 3, \tan \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right. \\
 & \left. \left. (a+b) \operatorname{AppellF1} \left[2, 1+n, -n, 3, \tan \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \tan \left[\frac{1}{2} (c+dx) \right]^2 \right) + \\
 & \left((a+b) \tan \left[\frac{1}{2} (c+dx) \right]^2 \left(-\frac{1}{2(a+b)} (a-b) n \operatorname{AppellF1} \left[2, n, 1-n, 3, \tan \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \sec \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] + \right. \right. \\
 & \left. \left. \frac{1}{2} n \operatorname{AppellF1} \left[2, 1+n, -n, 3, \tan \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right. \right. \\
 & \left. \left. \left. \sec \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] \right) \right) / \\
 & \left(2(a+b) \operatorname{AppellF1} \left[1, n, -n, 2, \tan \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \\
 & \left. n \left((-a+b) \operatorname{AppellF1} \left[2, n, 1-n, 3, \tan \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & (a+b) \operatorname{AppellF1}\left[2, 1+n, -n, 3, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 + \\
 & \left((a-b) \operatorname{AppellF1}\left[1, n, -n, 2, \cot\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a+b) \cot\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \right. \\
 & \left. \left(-n \left((a+b) \left(-\frac{1}{3(a-b)} 2(a+b)(1-n) \operatorname{AppellF1}\left[3, n, 2-n, 4, \cot\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a+b) \cot\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 - \right. \right. \right. \\
 & \left. \left. \frac{2}{3} n \operatorname{AppellF1}\left[3, 1+n, 1-n, 4, \cot\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a+b) \cot\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & (-a+b) \left(\frac{1}{3(a-b)} 2(a+b)n \operatorname{AppellF1}\left[3, 1+n, 1-n, 4, \cot\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a+b) \cot\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 - \frac{2}{3}(1+n) \right. \\
 & \left. \operatorname{AppellF1}\left[3, 2+n, -n, 4, \cot\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a+b) \cot\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \right. \\
 & \left. \left. \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + 2(a-b) \operatorname{AppellF1}\left[1, n, -n, 2, \right. \\
 & \left. \cot\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a+b) \cot\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \\
 & 2(a-b) \left(\frac{1}{2(a-b)} (a+b)n \operatorname{AppellF1}\left[2, n, 1-n, 3, \cot\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a+b) \cot\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 - \right. \\
 & \left. \frac{1}{2} n \operatorname{AppellF1}\left[2, 1+n, -n, 3, \cot\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a+b) \cot\left[\frac{1}{2}(c+dx)\right]^2}{a-b}\right] \right. \\
 & \left. \left. \cot\left[\frac{1}{2}(c+dx)\right] \operatorname{Csc}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(-n \left((a+b) \operatorname{AppellF1} \left[2, n, 1-n, 3, \cot \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a+b) \cot \left[\frac{1}{2} (c+dx) \right]^2}{a-b} \right] + \right. \right. \\
 & \quad (-a+b) \operatorname{AppellF1} \left[2, 1+n, -n, 3, \cot \left[\frac{1}{2} (c+dx) \right]^2, \right. \\
 & \quad \left. \left. \frac{(a+b) \cot \left[\frac{1}{2} (c+dx) \right]^2}{a-b} \right] \right) + 2(a-b) \operatorname{AppellF1} \left[1, n, -n, 2, \right. \\
 & \quad \left. \cot \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a+b) \cot \left[\frac{1}{2} (c+dx) \right]^2}{a-b} \right] \tan \left[\frac{1}{2} (c+dx) \right]^2 \right)^2 - \\
 & \left(2b(-2+n) \operatorname{AppellF1} \left[1-n, -n, 1, 2-n, \frac{(a-b) \left(-1 + \tan \left[\frac{1}{2} (c+dx) \right]^2 \right)}{2b}, \right. \right. \\
 & \quad \left. \left. 1 - \tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \operatorname{Csc} \left[\frac{1}{2} (c+dx) \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right] \right) / \\
 & \left((-1+n) \left(2b(-2+n) \operatorname{AppellF1} \left[1-n, -n, 1, 2-n, \frac{(a-b) \left(-1 + \tan \left[\frac{1}{2} (c+dx) \right]^2 \right)}{2b}, \right. \right. \right. \\
 & \quad \left. \left. 1 - \tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \left((a-b) n \operatorname{AppellF1} \left[2-n, 1-n, 1, 3-n, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \left(-1 + \tan \left[\frac{1}{2} (c+dx) \right]^2 \right)}{2b}, 1 - \tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
 & \quad \left. \left. 2b \operatorname{AppellF1} \left[2-n, -n, 2, 3-n, \frac{(a-b) \left(-1 + \tan \left[\frac{1}{2} (c+dx) \right]^2 \right)}{2b}, \right. \right. \right. \\
 & \quad \left. \left. 1 - \tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \right) \left(-1 + \tan \left[\frac{1}{2} (c+dx) \right]^2 \right) \right) + \\
 & \left(2b(-2+n) \operatorname{AppellF1} \left[1-n, -n, 1, 2-n, \frac{(a-b) \left(-1 + \tan \left[\frac{1}{2} (c+dx) \right]^2 \right)}{2b}, \right. \right. \\
 & \quad \left. \left. 1 - \tan \left[\frac{1}{2} (c+dx) \right]^2 \right] \cot \left[\frac{1}{2} (c+dx) \right] \operatorname{Csc} \left[\frac{1}{2} (c+dx) \right]^2 \left(-1 + \tan \left[\frac{1}{2} (c+dx) \right]^2 \right) \right) / \\
 & \left((-1+n) \left(2b(-2+n) \operatorname{AppellF1} \left[1-n, -n, 1, 2-n, \frac{(a-b) \left(-1 + \tan \left[\frac{1}{2} (c+dx) \right]^2 \right)}{2b}, \right. \right. \right. \\
 & \quad \left. \left. 1 - \tan \left[\frac{1}{2} (c+dx) \right]^2 \right] + \left((a-b) n \operatorname{AppellF1} \left[2-n, 1-n, 1, 3-n, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{(a-b) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}, 1 - \tan\left[\frac{1}{2}(c+dx)\right]^2 + \\
 & 2b \operatorname{AppellF1}\left[2-n, -n, 2, 3-n, \frac{(a-b) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}, \right. \\
 & \left. 1 - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right] - \\
 & \left(2b(-2+n) \cot\left[\frac{1}{2}(c+dx)\right]^2 \left(-\frac{1}{2b(2-n)}(a-b)(1-n) n \operatorname{AppellF1}\left[2-n, \right. \right. \right. \\
 & \left. \left. 1-n, 1, 3-n, \frac{(a-b) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}, 1 - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \frac{1}{2-n}(1-n) \operatorname{AppellF1}\left[2-n, -n, \right. \right. \right. \\
 & \left. \left. 2, 3-n, \frac{(a-b) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}, 1 - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
 & \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) / \\
 & \left((-1+n) \left(2b(-2+n) \operatorname{AppellF1}\left[1-n, -n, 1, 2-n, \frac{(a-b) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}, \right. \right. \right. \right. \\
 & \left. \left. 1 - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \left((a-b) n \operatorname{AppellF1}\left[2-n, 1-n, 1, 3-n, \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}, 1 - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
 & \left. \left. 2b \operatorname{AppellF1}\left[2-n, -n, 2, 3-n, \frac{(a-b) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}, \right. \right. \right. \\
 & \left. \left. 1 - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right] - \\
 & \left((a+b) \operatorname{AppellF1}\left[1, n, -n, 2, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \left(n \left((-a+b) \operatorname{AppellF1}\left[2, n, 1-n, 3, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. (a+b) \operatorname{AppellF1}\left[2, 1+n, -n, 3, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 2(a+b) \left(-\frac{1}{2(a+b)}(a-b)n \operatorname{AppellF1}\left[2, \right. \right. \\
 & \quad \left. \left. n, 1-n, 3, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{2}n \operatorname{AppellF1}\left[2, 1+n, -n, 3, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \\
 & n \tan\left[\frac{1}{2}(c+dx)\right]^2 \left((-a+b) \left(\frac{1}{3(a+b)} 2(a-b)(1-n) \operatorname{AppellF1}\left[3, n, \right. \right. \right. \\
 & \quad \left. \left. 2-n, 4, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{3}n \operatorname{AppellF1}\left[3, 1+n, 1-n, 4, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
 & (a+b) \left(-\frac{1}{3(a+b)} 2(a-b)n \operatorname{AppellF1}\left[3, 1+n, 1-n, 4, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{2}{3}(1+n) \operatorname{AppellF1}\left[3, 2+n, -n, 4, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \Big/ \\
 & \left(2(a+b) \operatorname{AppellF1}\left[1, n, -n, 2, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & n \left((-a+b) \operatorname{AppellF1}\left[2, n, 1-n, 3, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \quad \left. (a+b) \operatorname{AppellF1}\left[2, 1+n, -n, 3, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + \\
 & \left(2b(-2+n) \operatorname{AppellF1}\left[1-n, -n, 1, 2-n, \frac{(a-b)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}\right], \right. \\
 & \left. 1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]^2 \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \left(\left((a-b)n \operatorname{AppellF1}\left[2-n, 1-n, 1, 3-n, \frac{(a-b)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}\right], \right. \right. \\
 & \left. \left. 1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) + 2b \operatorname{AppellF1}\left[2-n, -n, 2, 3-n, \right. \right. \\
 & \left. \left. \frac{(a-b)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}, 1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 2b(-2+n) \left(-\frac{1}{2b(2-n)} (a-b)(1-n) \operatorname{AppellF1}\left[\right. \right. \\
 & \left. \left. 2-n, 1-n, 1, 3-n, \frac{(a-b)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}, 1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - \frac{1}{2-n} (1-n) \operatorname{AppellF1}\left[2-n, \right. \\
 & \left. -n, 2, 3-n, \frac{(a-b)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}, 1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \left((a-b)n \right. \\
 & \left(-\frac{1}{3-n} (2-n) \operatorname{AppellF1}\left[3-n, 1-n, 2, 4-n, \frac{(a-b)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}\right], \right. \\
 & \left. 1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \\
 & \frac{1}{2b(3-n)} (a-b)(1-n)(2-n) \operatorname{AppellF1}\left[3-n, 2-n, 1, 4-n, \right. \\
 & \left. \frac{(a-b)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}, 1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) + 2b \left(-\frac{1}{2b(3-n)} (a-b)(2-n) \right. \\
 & \left. n \operatorname{AppellF1}\left[3-n, 1-n, 2, 4-n, \frac{(a-b)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)}{2b}\right], \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(3 (a+b) \operatorname{AppellF1} \left[\frac{1}{2}, n, -n, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 + \right. \\
 & 2n \left((-a+b) \operatorname{AppellF1} \left[\frac{3}{2}, n, 1-n, \frac{5}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 + \right. \\
 & (a+b) \operatorname{AppellF1} \left[\frac{3}{2}, 1+n, -n, \frac{5}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \left. \right) - \\
 & \operatorname{AppellF1} \left[-\frac{1}{2}, n, -n, \frac{1}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] / \\
 & \left((a+b) \operatorname{AppellF1} \left[-\frac{1}{2}, n, -n, \frac{1}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 \right. \\
 & \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] + 2n \left((-a+b) \operatorname{AppellF1} \left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1} \left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^3 \left. \right) \left. \right) / \\
 & \left(2d \left(-\frac{1}{2} a (a+b) n (b+a \operatorname{Cos} [c+dx])^{-1+n} \operatorname{Sec} [c+dx]^n \operatorname{Sin} [c+dx] \right. \right. \\
 & \left. \left(\left(3 \operatorname{AppellF1} \left[\frac{1}{2}, n, -n, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right]^2 \right. \right. \right. \\
 & \left. \left. \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right) \right) / \left(3 (a+b) \operatorname{AppellF1} \left[\frac{1}{2}, n, -n, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + 2n \left((-a+b) \operatorname{AppellF1} \left[\frac{3}{2}, n, 1-n, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1} \left[\frac{3}{2}, 1+n, \right. \right. \\
 & \left. \left. -n, \frac{5}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \right) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 \left. \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[-\frac{1}{2}, n, -n, \frac{1}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] / \\
 & \left((a+b) \text{AppellF1}\left[-\frac{1}{2}, n, -n, \frac{1}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \text{Tan}\left[\frac{1}{2}(c+dx)\right] + 2n \left((-a+b) \text{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b)\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \text{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \right. \right. \\
 & \quad \quad \left. \left. \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^3 \Bigg) + \\
 & \frac{1}{2} (a+b) n (b+a \text{Cos}[c+dx])^n \text{Sec}[c+dx]^{1+n} \text{Sin}[c+dx] \left(\left(3 \text{AppellF1}\left[\frac{1}{2}, n, \right. \right. \right. \\
 & \quad \left. \left. -n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \text{Tan}\left[\frac{1}{2}(c+dx)\right] \right) / \\
 & \left(3 (a+b) \text{AppellF1}\left[\frac{1}{2}, n, -n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \quad 2n \left((-a+b) \text{AppellF1}\left[\frac{3}{2}, n, 1-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \quad (a+b) \text{AppellF1}\left[\frac{3}{2}, 1+n, -n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \quad \left. \left. \frac{(a-b)\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) - \\
 & \text{AppellF1}\left[-\frac{1}{2}, n, -n, \frac{1}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] / \\
 & \left((a+b) \text{AppellF1}\left[-\frac{1}{2}, n, -n, \frac{1}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \text{Tan}\left[\frac{1}{2}(c+dx)\right] + 2n \left((-a+b) \text{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b)\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \text{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \right. \right. \\
 & \quad \quad \left. \left. \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) -
 \end{aligned}$$

$$\left(\frac{1}{a+b} (a-b) n \operatorname{AppellF1} \left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] - n \operatorname{AppellF1} \left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \Bigg/$$

$$\left((a+b) \operatorname{AppellF1} \left[-\frac{1}{2}, n, -n, \frac{1}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] + 2n \left((-a+b) \operatorname{AppellF1} \left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) + (a+b) \operatorname{AppellF1} \left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^3 \Bigg) +$$

$$\left(\operatorname{AppellF1} \left[-\frac{1}{2}, n, -n, \frac{1}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \left(\frac{1}{2} (a+b) \operatorname{AppellF1} \left[-\frac{1}{2}, n, -n, \frac{1}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 + 3n \left((-a+b) \operatorname{AppellF1} \left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) + (a+b) \operatorname{AppellF1} \left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2$$

$$\operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2 + (a+b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \left(\frac{1}{a+b} (a-b) n \operatorname{AppellF1} \left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] - n \operatorname{AppellF1} \left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \operatorname{Tan} \left[\frac{1}{2} (c+dx) \right] \Bigg) +$$

$$\begin{aligned}
 & 2n \tan\left[\frac{1}{2}(c+dx)\right]^3 \left((-a+b) \left(\frac{1}{3(a+b)}(a-b)(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, n, \right. \right. \right. \\
 & \quad \left. \left. \left. 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3}n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
 & (a+b) \left(-\frac{1}{3(a+b)}(a-b)n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{1}{3}(1+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Bigg) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left((a+b) \operatorname{AppellF1}\left[-\frac{1}{2}, n, -n, \frac{1}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right] + 2n \left((-a+b) \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^3 \Bigg)^2 - \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \\
 & \tan\left[\frac{1}{2}(c+dx)\right] \left(2n \left((-a+b) \operatorname{AppellF1}\left[\frac{3}{2}, n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, -n, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(\tan\left[\frac{1}{2}(c+dx)\right] + 3(a+b) \left(-\frac{1}{3(a+b)}(a-b)n \operatorname{AppellF1}\left[\frac{3}{2}, n, 1-n, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3}n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, -n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
 & 2n \tan\left[\frac{1}{2}(c+dx)\right]^2 \left((-a+b) \left(\frac{1}{5(a+b)}3(a-b)(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, \right. \right. \right. \\
 & \quad \left. \left. \left. 2-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{3}{5}n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 1-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
 & (a+b) \left(-\frac{1}{5(a+b)}3(a-b)n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 1-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, -n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \right) \Big/ \\
 & \left(3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2n \left((-a+b) \operatorname{AppellF1}\left[\frac{3}{2}, n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, -n, \frac{5}{2}, \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Big/
 \end{aligned}$$

Problem 276: Result more than twice size of optimal antiderivative.

$$\int \text{Csc}[c + dx]^4 (a + b \text{Sec}[c + dx])^n dx$$

Optimal (type 6, 424 leaves, ? steps):

$$\begin{aligned} & -\frac{1}{2\sqrt{2}d} 3 \text{AppellF1}\left[-\frac{1}{2}, \frac{5}{2}, -n, \frac{1}{2}, \frac{1}{2} (1 - \text{Sec}[c + dx]), \frac{b(1 - \text{Sec}[c + dx])}{a+b}\right] \\ & \quad \text{Cot}[c + dx] \sqrt{1 + \text{Sec}[c + dx]} (a + b \text{Sec}[c + dx])^n \left(\frac{a + b \text{Sec}[c + dx]}{a+b}\right)^{-n} - \\ & \frac{1}{6\sqrt{2}d} \text{AppellF1}\left[-\frac{3}{2}, \frac{5}{2}, -n, -\frac{1}{2}, \frac{1}{2} (1 - \text{Sec}[c + dx]), \frac{b(1 - \text{Sec}[c + dx])}{a+b}\right] \\ & \quad \text{Cot}[c + dx]^3 (1 + \text{Sec}[c + dx])^{3/2} (a + b \text{Sec}[c + dx])^n \left(\frac{a + b \text{Sec}[c + dx]}{a+b}\right)^{-n} + \\ & \left(\text{AppellF1}\left[\frac{1}{2}, \frac{3}{2}, -n, \frac{3}{2}, \frac{1}{2} (1 - \text{Sec}[c + dx]), \frac{b(1 - \text{Sec}[c + dx])}{a+b}\right] \right. \\ & \quad \left. (a + b \text{Sec}[c + dx])^n \left(\frac{a + b \text{Sec}[c + dx]}{a+b}\right)^{-n} \text{Tan}[c + dx]\right) / \left(\sqrt{2}d\sqrt{1 + \text{Sec}[c + dx]}\right) + \\ & \left(\text{AppellF1}\left[\frac{1}{2}, \frac{5}{2}, -n, \frac{3}{2}, \frac{1}{2} (1 - \text{Sec}[c + dx]), \frac{b(1 - \text{Sec}[c + dx])}{a+b}\right] (a + b \text{Sec}[c + dx])^n \right. \\ & \quad \left. \left(\frac{a + b \text{Sec}[c + dx]}{a+b}\right)^{-n} \text{Tan}[c + dx]\right) / \left(2\sqrt{2}d\sqrt{1 + \text{Sec}[c + dx]}\right) \end{aligned}$$

Result (type 6, 8963 leaves):

$$\begin{aligned} & \left((a+b) \text{Csc}[c + dx]^4 (a + b \text{Sec}[c + dx])^n \left(\frac{1 + \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{1 - \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2}\right)^n \left(b + \frac{a - a \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{1 + \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2}\right)^n \right. \\ & \left. \left(\left(27 \text{AppellF1}\left[\frac{1}{2}, n, -n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a-b)\text{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a+b}\right] \text{Tan}\left[\frac{1}{2}(c + dx)\right] \right) / \right. \right. \\ & \left. \left(3(a+b) \text{AppellF1}\left[\frac{1}{2}, n, -n, \frac{3}{2}, \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a-b)\text{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a+b}\right] + \right. \right. \\ & \left. \left. 2n \left((-a+b) \text{AppellF1}\left[\frac{3}{2}, n, 1-n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a-b)\text{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a+b}\right] + \right. \right. \right. \\ & \left. \left. (a+b) \text{AppellF1}\left[\frac{3}{2}, 1+n, -n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \frac{(a-b)\text{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{a+b}\right] \right) \right) \right. \\ & \left. \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2 \right) + \left(5 \text{AppellF1}\left[\frac{3}{2}, n, -n, \frac{5}{2}, \text{Tan}\left[\frac{1}{2}(c + dx)\right]^2, \right. \right. \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 \Bigg/ \\
 & \left(5(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, n, -n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2n \left((-a+b) \operatorname{AppellF1}\left[\frac{5}{2}, n, 1-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, -n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) - \\
 & \left(9 \operatorname{AppellF1}\left[-\frac{1}{2}, n, -n, \frac{1}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \Bigg/ \\
 & \left((a+b) \operatorname{AppellF1}\left[-\frac{1}{2}, n, -n, \frac{1}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 2n \left((-a+b) \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 \Bigg) - \\
 & \operatorname{AppellF1}\left[-\frac{3}{2}, n, -n, -\frac{1}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \Bigg/ \\
 & \left((a+b) \operatorname{AppellF1}\left[-\frac{3}{2}, n, -n, -\frac{1}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 + 2n \left((a-b) \operatorname{AppellF1}\left[-\frac{1}{2}, n, 1-n, \frac{1}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - (a+b) \operatorname{AppellF1}\left[-\frac{1}{2}, 1+n, -n, \frac{1}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 \Bigg) \Bigg) \Bigg/
 \end{aligned}$$

$$\begin{aligned}
 & \left(24 d \left(\frac{1}{24} (a+b) n \left(\frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^n \left(-\frac{a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} - \right. \right. \right. \\
 & \quad \left. \left. \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(a - a \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)}{\left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2} \right) \right) \\
 & \left(b + \frac{a - a \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{-1+n} \left(\left(27 \operatorname{AppellF1}\left[\frac{1}{2}, n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\
 & \left(3 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \\
 & \quad 2 n \left((-a+b) \operatorname{AppellF1}\left[\frac{3}{2}, n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \\
 & \quad \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, -n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right) \\
 & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2 \left. + \left(5 \operatorname{AppellF1}\left[\frac{3}{2}, n, -n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \tan\left[\frac{1}{2}(c+dx)\right]^3 \right) \right) / \\
 & \left(5 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, n, -n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \\
 & \quad 2 n \left((-a+b) \operatorname{AppellF1}\left[\frac{5}{2}, n, 1-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \\
 & \quad \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, -n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & \left(9 \operatorname{AppellF1}\left[-\frac{1}{2}, n, -n, \frac{1}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left((a+b) \operatorname{AppellF1}\left[-\frac{1}{2}, n, -n, \frac{1}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \tan\left[\frac{1}{2}(c+dx)\right] + 2n \left((-a+b) \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^3 \Bigg) - \\
 & \operatorname{AppellF1}\left[-\frac{3}{2}, n, -n, -\frac{1}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] / \\
 & \left((a+b) \operatorname{AppellF1}\left[-\frac{3}{2}, n, -n, -\frac{1}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \quad \tan\left[\frac{1}{2}(c+dx)\right]^3 + 2n \left((a-b) \operatorname{AppellF1}\left[-\frac{1}{2}, n, 1-n, \frac{1}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - (a+b) \operatorname{AppellF1}\left[-\frac{1}{2}, 1+n, -n, \frac{1}{2}, \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^5 \Bigg) + \\
 & \frac{1}{24} (a+b) n \left(\frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{-1+n} \left(\frac{\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} + \right. \\
 & \quad \left. \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}{\left(1 - \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2} \right) \\
 & \left(b + \frac{a - a \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^n \left(\left(27 \operatorname{AppellF1}\left[\frac{1}{2}, n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right] \right) \Bigg) / \\
 & \left(3 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \quad \left. 2n \left((-a+b) \operatorname{AppellF1}\left[\frac{3}{2}, n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, -n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left. + \left(5 \operatorname{AppellF1}\left[\frac{3}{2}, n, -n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right.\right.\right. \\
 & \left.\left.\left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3\right) \right/ \\
 & \left(5(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, n, -n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & 2n \left((-a+b) \operatorname{AppellF1}\left[\frac{5}{2}, n, 1-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, -n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right.\right. \\
 & \left.\left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
 & \left(9 \operatorname{AppellF1}\left[-\frac{1}{2}, n, -n, \frac{1}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) \left/ \right. \\
 & \left((a+b) \operatorname{AppellF1}\left[-\frac{1}{2}, n, -n, \frac{1}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + 2n \left((-a+b) \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right.\right. \\
 & \left.\left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \right.\right. \\
 & \left.\left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 \right) - \\
 & \operatorname{AppellF1}\left[-\frac{3}{2}, n, -n, -\frac{1}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \left/ \right. \\
 & \left((a+b) \operatorname{AppellF1}\left[-\frac{3}{2}, n, -n, -\frac{1}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 + 2n \left((a-b) \operatorname{AppellF1}\left[-\frac{1}{2}, n, 1-n, \frac{1}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right.\right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left(\frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right) - (a+b) \operatorname{AppellF1}\left[-\frac{1}{2}, 1+n, -n, \frac{1}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^5 \right) \right) + \\
 & \frac{1}{24} (a+b) \left(\frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^n \left(b + \frac{a - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right)^n \\
 & \left(\left(27 \operatorname{AppellF1}\left[\frac{1}{2}, n, -n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \right. \\
 & \left. \left(2 \left(3 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, n, -n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) + \right. \right. \\
 & \left. \left. 2n \left((-a+b) \operatorname{AppellF1}\left[\frac{3}{2}, n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, -n, \frac{5}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \left(27 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \left(-\frac{1}{3(a+b)} (a-b)n \operatorname{AppellF1}\left[\frac{3}{2}, n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \left. \left. \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, -n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) / \right. \\
 & \left(3 (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, n, -n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) + \\
 & \left. 2n \left((-a+b) \operatorname{AppellF1}\left[\frac{3}{2}, n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, -n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right]\right) \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) + \left(15 \operatorname{AppellF1}\left[\frac{3}{2}, n, -n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \\
 & \left(2 \left(5 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, n, -n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. 2n \left((-a+b) \operatorname{AppellF1}\left[\frac{5}{2}, n, 1-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, -n, \frac{7}{2}, \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
 & \left(5 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^3 \left(-\frac{1}{5(a+b)} 3 (a-b) n \operatorname{AppellF1}\left[\frac{5}{2}, n, 1-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \left. \left. \frac{3}{5} n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, -n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \\
 & \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \\
 & \left(5 (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, n, -n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \\
 & \left. 2n \left((-a+b) \operatorname{AppellF1}\left[\frac{5}{2}, n, 1-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right. \right. \\
 & \left. \left. (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, -n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left(9 \left(\frac{1}{a+b} (a-b) n \operatorname{AppellF1} \left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right. \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] - n \operatorname{AppellF1} \left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \tan \left[\frac{1}{2} (c+ \right. \right. \right. \\
 & \quad \left. \left. \left. dx) \right]^2, \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right] \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] \right) \right) / \\
 & \left((a+b) \operatorname{AppellF1} \left[-\frac{1}{2}, n, -n, \frac{1}{2}, \tan \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \\
 & \quad \tan \left[\frac{1}{2} (c+dx) \right] + 2n \left((-a+b) \operatorname{AppellF1} \left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan \left[\frac{1}{2} (c+dx) \right] \right]^2, \right. \\
 & \quad \left. \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) + (a+b) \operatorname{AppellF1} \left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \right. \\
 & \quad \left. \tan \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \tan \left[\frac{1}{2} (c+dx) \right]^3 \Big) - \\
 & \left(-\frac{1}{a+b} 3 (a-b) n \operatorname{AppellF1} \left[-\frac{1}{2}, n, 1-n, \frac{1}{2}, \tan \left[\frac{1}{2} (c+dx) \right] \right]^2, \right. \\
 & \quad \left. \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] + \\
 & \quad 3n \operatorname{AppellF1} \left[-\frac{1}{2}, 1+n, -n, \frac{1}{2}, \tan \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{2} (c+dx) \right]^2 \tan \left[\frac{1}{2} (c+dx) \right] \right) / \\
 & \left((a+b) \operatorname{AppellF1} \left[-\frac{3}{2}, n, -n, -\frac{1}{2}, \tan \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \\
 & \quad \tan \left[\frac{1}{2} (c+dx) \right]^3 + 2n \left((a-b) \operatorname{AppellF1} \left[-\frac{1}{2}, n, 1-n, \frac{1}{2}, \tan \left[\frac{1}{2} (c+dx) \right] \right]^2, \right. \\
 & \quad \left. \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) - (a+b) \operatorname{AppellF1} \left[-\frac{1}{2}, 1+n, -n, \frac{1}{2}, \right. \\
 & \quad \left. \tan \left[\frac{1}{2} (c+dx) \right] \right]^2, \frac{(a-b) \tan \left[\frac{1}{2} (c+dx) \right]^2}{a+b} \right) \tan \left[\frac{1}{2} (c+dx) \right]^5 \Big) +
 \end{aligned}$$

$$\begin{aligned}
 & \left(\text{AppellF1}\left[-\frac{3}{2}, n, -n, -\frac{1}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \\
 & \left. \left(\frac{3}{2}(a+b)\text{AppellF1}\left[-\frac{3}{2}, n, -n, -\frac{1}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right. \right. \\
 & \left. \left. \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 + 5n \left((a-b)\text{AppellF1}\left[-\frac{1}{2}, n, 1-n, \frac{1}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] - (a+b)\text{AppellF1}\left[-\frac{1}{2}, 1+n, \right. \right. \right. \right. \\
 & \left. \left. \left. -n, \frac{1}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \right) \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^4 + (a+b)\tan\left[\frac{1}{2}(c+dx)\right]^3 \left(-\frac{1}{a+b} 3(a-b)n\text{AppellF1}\left[-\frac{1}{2}, \right. \right. \\
 & \left. \left. n, 1-n, \frac{1}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right] + 3n\text{AppellF1}\left[-\frac{1}{2}, 1+n, -n, \frac{1}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \\
 & 2n\tan\left[\frac{1}{2}(c+dx)\right]^5 \left((a-b) \left(-\frac{1}{a+b}(a-b)(1-n)\text{AppellF1}\left[\frac{1}{2}, n, 2-n, \right. \right. \right. \\
 & \left. \left. \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right] - n\text{AppellF1}\left[\frac{1}{2}, 1+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) - \\
 & (a+b) \left(\frac{1}{a+b}(a-b)n\text{AppellF1}\left[\frac{1}{2}, 1+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b)\tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \right. \\
 & \left. (1+n)\text{AppellF1}\left[\frac{1}{2}, 2+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 - n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \left] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right] \right) + \\
 & (a+b) \left(-\frac{1}{3(a+b)} (a-b) n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \frac{1}{3} (1+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2+n, -n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right] \right) \Bigg) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left((a+b) \operatorname{AppellF1}\left[-\frac{1}{2}, n, -n, \frac{1}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \tan\left[\frac{1}{2}(c+dx)\right] + 2n \left((-a+b) \operatorname{AppellF1}\left[\frac{1}{2}, n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{1}{2}, 1+n, -n, \frac{3}{2}, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^3 \right)^2 - \\
 & \left(27 \operatorname{AppellF1}\left[\frac{1}{2}, n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right. \\
 & \tan\left[\frac{1}{2}(c+dx)\right] \left(2n \left((-a+b) \operatorname{AppellF1}\left[\frac{3}{2}, n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, -n, \frac{5}{2}, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \tan\left[\frac{1}{2}(c+dx)\right] + 3(a+b) \left(-\frac{1}{3(a+b)} (a-b) n \operatorname{AppellF1}\left[\frac{3}{2}, n, 1-n, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3}n \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, -n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
 & \left. \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right] + \\
 & 2n \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \left((-a+b) \left(\frac{1}{5(a+b)} 3(a-b)(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, n, \right. \right. \right. \\
 & \left. \left. \left. 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \frac{3}{5}n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 1-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right] \right) \right) + \right. \\
 & (a+b) \left(-\frac{1}{5(a+b)} 3(a-b)n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, 1-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + \right. \right. \right. \\
 & \left. \left. \left. \frac{3}{5}(1+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+n, -n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right] \right) \right) \right) \Big/ \\
 & \left(3(a+b) \operatorname{AppellF1}\left[\frac{1}{2}, n, -n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + \right. \\
 & 2n \left((-a+b) \operatorname{AppellF1}\left[\frac{3}{2}, n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \left. \left. \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] + (a+b) \operatorname{AppellF1}\left[\frac{3}{2}, 1+n, -n, \frac{5}{2}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 - \\
 & \left(5 \operatorname{AppellF1}\left[\frac{3}{2}, n, -n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b)\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b} \right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{2}(c+dx)\right]^3 \left(2n \left((-a+b) \operatorname{AppellF1}\left[\frac{5}{2}, n, 1-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + (a+b) \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, -n, \frac{7}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \tan\left[\frac{1}{2}(c+dx)\right] + 5(a+b) \left(-\frac{1}{5(a+b)} 3(a-b)n \operatorname{AppellF1}\left[\frac{5}{2}, n, 1-n, \right. \right. \\
 & \quad \left. \left. \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{3}{5}n \operatorname{AppellF1}\left[\frac{5}{2}, 1+n, -n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \\
 & 2n \tan\left[\frac{1}{2}(c+dx)\right]^2 \left((-a+b) \left(\frac{1}{7(a+b)} 5(a-b)(1-n) \operatorname{AppellF1}\left[\frac{7}{2}, n, \right. \right. \right. \\
 & \quad \left. \left. 2-n, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{5}{7}n \operatorname{AppellF1}\left[\frac{7}{2}, 1+n, 1-n, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \\
 & (a+b) \left(-\frac{1}{7(a+b)} 5(a-b)n \operatorname{AppellF1}\left[\frac{7}{2}, 1+n, 1-n, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. \frac{5}{7}(1+n) \operatorname{AppellF1}\left[\frac{7}{2}, 2+n, -n, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Big/ \\
 & \left(5(a+b) \operatorname{AppellF1}\left[\frac{3}{2}, n, -n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \frac{(a-b) \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}\right] + \right.
 \end{aligned}$$

$$2 n \left((-a + b) \operatorname{AppellF1} \left[\frac{5}{2}, n, 1 - n, \frac{7}{2}, \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right]^2, \right. \right. \\ \left. \left. \frac{(a - b) \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right]^2}{a + b} \right] + (a + b) \operatorname{AppellF1} \left[\frac{5}{2}, 1 + n, -n, \frac{7}{2}, \right. \right. \\ \left. \left. \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right]^2, \frac{(a - b) \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right]^2}{a + b} \right] \operatorname{Tan} \left[\frac{1}{2} (c + d x) \right]^2 \right)^2 \right)$$

Problem 294: Result unnecessarily involves higher level functions.

$$\int \frac{(e \operatorname{Csc}[c + d x])^{3/2}}{a + a \operatorname{Sec}[c + d x]} dx$$

Optimal (type 4, 145 leaves, 8 steps):

$$\frac{4 e \operatorname{Cos}[c + d x] \sqrt{e \operatorname{Csc}[c + d x]}}{5 a d} + \frac{2 e \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x] \sqrt{e \operatorname{Csc}[c + d x]}}{5 a d} - \frac{2 e \operatorname{Csc}[c + d x]^2 \sqrt{e \operatorname{Csc}[c + d x]}}{5 a d} - \frac{4 e \sqrt{e \operatorname{Csc}[c + d x]} \operatorname{EllipticE} \left[\frac{1}{2} (c - \frac{\pi}{2} + d x), 2 \right] \sqrt{\operatorname{Sin}[c + d x]}}{5 a d}$$

Result (type 5, 219 leaves):

$$\left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right]^2 (e \operatorname{Csc}[c + d x])^{3/2} \left(\left(8 \sqrt{2} e^{-i(c+d x)} \sqrt{\frac{i e^i (c+d x)}{-1 + e^{2 i (c+d x)}}} \right. \right. \right. \\ \left. \left. \left(-1 + e^{2 i (c+d x)} + (1 + e^{2 i c}) \sqrt{1 - e^{2 i (c+d x)}} \operatorname{Hypergeometric2F1} \left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, e^{2 i (c+d x)} \right] \right) \right. \right. \\ \left. \left. \operatorname{Sec}[c + d x] \right) \right) / (d (1 + e^{2 i c}) \operatorname{Csc}[c + d x]^{3/2}) - \frac{2 \left(4 \operatorname{Cos}[d x] \operatorname{Sec}[c] + \operatorname{Sec} \left[\frac{1}{2} (c + d x) \right]^2 \right) \operatorname{Tan}[c + d x]}{d} \right) / (5 a (1 + \operatorname{Sec}[c + d x]))$$

Problem 296: Result unnecessarily involves higher level functions.

$$\int \frac{1}{\sqrt{e \operatorname{Csc}[c + d x]} (a + a \operatorname{Sec}[c + d x])} dx$$

Optimal (type 4, 99 leaves, 7 steps):

$$\frac{2 \cot [c+d x]}{a d \sqrt{e \csc [c+d x]}} - \frac{2 \csc [c+d x]}{a d \sqrt{e \csc [c+d x]}} + \frac{4 \operatorname{EllipticE}\left[\frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), 2\right]}{a d \sqrt{e \csc [c+d x]} \sqrt{\sin [c+d x]}}$$

Result (type 5, 82 leaves):

$$-\left(\left(2\left(2 i-\cot [c+d x]+\csc [c+d x]-\frac{4 i \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, e^{2 i(c+d x)}\right]}{\sqrt{1-e^{2 i(c+d x)}}}\right)\right)\right) / \left(a d \sqrt{e \csc [c+d x]}\right)$$

Problem 298: Result unnecessarily involves higher level functions.

$$\int \frac{1}{\left(e \csc [c+d x]\right)^{5 / 2}\left(a+a \sec [c+d x]\right)} d x$$

Optimal (type 4, 120 leaves, 7 steps):

$$-\frac{4 \operatorname{EllipticE}\left[\frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), 2\right]}{5 a d e^2 \sqrt{e \csc [c+d x]} \sqrt{\sin [c+d x]}} + \frac{2 \sin [c+d x]}{3 a d e^2 \sqrt{e \csc [c+d x]}} - \frac{2 \cos [c+d x] \sin [c+d x]}{5 a d e^2 \sqrt{e \csc [c+d x]}}$$

Result (type 5, 91 leaves):

$$\left(24 i-\frac{48 i \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, e^{2 i(c+d x)}\right]}{\sqrt{1-e^{2 i(c+d x)}}}+20 \sin [c+d x]-6 \sin [2(c+d x)]\right) / \left(30 a d e^2 \sqrt{e \csc [c+d x]}\right)$$

Problem 301: Result unnecessarily involves higher level functions.

$$\int \frac{\left(e \csc [c+d x]\right)^{3 / 2}}{\left(a+a \sec [c+d x]\right)^2} d x$$

Optimal (type 4, 250 leaves, 16 steps):

$$-\frac{4 e \cos [c+d x] \sqrt{e \csc [c+d x]}}{15 a^2 d} + \frac{16 e \cot [c+d x] \csc [c+d x] \sqrt{e \csc [c+d x]}}{45 a^2 d} - \frac{2 e \cot [c+d x]^3 \csc [c+d x] \sqrt{e \csc [c+d x]}}{9 a^2 d} - \frac{4 e \csc [c+d x]^2 \sqrt{e \csc [c+d x]}}{5 a^2 d} - \frac{2 e \cot [c+d x] \csc [c+d x]^3 \sqrt{e \csc [c+d x]}}{9 a^2 d} + \frac{4 e \csc [c+d x]^4 \sqrt{e \csc [c+d x]}}{9 a^2 d} - \frac{4 e \sqrt{e \csc [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}\left(c-\frac{\pi}{2}+d x\right), 2\right] \sqrt{\sin [c+d x]}}{15 a^2 d}$$

Result (type 5, 238 leaves):

$$\left(\cos\left[\frac{1}{2}(c+dx)\right]^4 (e \operatorname{Csc}[c+dx])^{3/2} \operatorname{Sec}[c+dx] \left(\left(16\sqrt{2} e^{-i(c+dx)} \sqrt{\frac{i e^i(c+dx)}{-1+e^{2i(c+dx)}}} \right. \right. \right. \\ \left. \left. \left. (-1+e^{2i(c+dx)} + (1+e^{2ic}) \sqrt{1-e^{2i(c+dx)}}) \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, e^{2i(c+dx)}\right] \right) \right. \right. \\ \left. \left. \operatorname{Sec}[c+dx] \right) / \left(d(1+e^{2ic}) \operatorname{Csc}[c+dx]^{3/2} \right) - \frac{1}{3d} \right. \\ \left. 2 \left(24 \cos[dx] \operatorname{Sec}[c] + (8+13 \cos[c+dx]) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 \right) \tan[c+dx] \right) / \\ \left(15a^2 (1+\operatorname{Sec}[c+dx])^2 \right)$$

Problem 303: Result unnecessarily involves higher level functions.

$$\int \frac{1}{\sqrt{e \operatorname{Csc}[c+dx]} (a+a \operatorname{Sec}[c+dx])^2} dx$$

Optimal (type 4, 199 leaves, 14 steps):

$$\frac{16 \cot[c+dx]}{5a^2 d \sqrt{e \operatorname{Csc}[c+dx]}} - \frac{2 \cot[c+dx]^3}{5a^2 d \sqrt{e \operatorname{Csc}[c+dx]}} - \frac{4 \operatorname{Csc}[c+dx]}{a^2 d \sqrt{e \operatorname{Csc}[c+dx]}} - \\ \frac{2 \cot[c+dx] \operatorname{Csc}[c+dx]^2}{5a^2 d \sqrt{e \operatorname{Csc}[c+dx]}} + \frac{4 \operatorname{Csc}[c+dx]^3}{5a^2 d \sqrt{e \operatorname{Csc}[c+dx]}} + \frac{28 \operatorname{EllipticE}\left[\frac{1}{2}\left(c-\frac{\pi}{2}+dx\right), 2\right]}{5a^2 d \sqrt{e \operatorname{Csc}[c+dx]} \sqrt{\sin[c+dx]}}$$

Result (type 5, 241 leaves):

$$\left(4 \cos\left[\frac{1}{2}(c+dx)\right]^4 \sqrt{\operatorname{Csc}[c+dx]} \operatorname{Sec}[c+dx]^2 \right. \\ \left(-\frac{1}{1+e^{2ic}} 28\sqrt{2} e^{-i(c+dx)} \sqrt{\frac{i e^i(c+dx)}{-1+e^{2i(c+dx)}}} \left(-1+e^{2i(c+dx)} + \right. \right. \\ \left. \left. (1+e^{2ic}) \sqrt{1-e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, e^{2i(c+dx)}\right] \right) + \sqrt{\operatorname{Csc}[c+dx]} \right. \\ \left. \left. \left(-(-23+5 \cos[2c]) \cos[dx] \operatorname{Sec}[c] + 2 \left(-10 + \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 + 5 \sin[c] \sin[dx] \right) \right) \right) \right) / \\ \left(5a^2 d \sqrt{e \operatorname{Csc}[c+dx]} (1+\operatorname{Sec}[c+dx])^2 \right)$$

Problem 305: Result unnecessarily involves higher level functions.

$$\int \frac{1}{(e \operatorname{Csc}[c+dx])^{5/2} (a+a \operatorname{Sec}[c+dx])^2} dx$$

Optimal (type 4, 215 leaves, 13 steps):

$$-\frac{2 \operatorname{Cot}[c+dx]}{a^2 d e^2 \sqrt{e \operatorname{Csc}[c+dx]}} - \frac{2 \operatorname{Cos}[c+dx]^2 \operatorname{Cot}[c+dx]}{a^2 d e^2 \sqrt{e \operatorname{Csc}[c+dx]}} + \frac{4 \operatorname{Csc}[c+dx]}{a^2 d e^2 \sqrt{e \operatorname{Csc}[c+dx]}} -$$

$$\frac{44 \operatorname{EllipticE}\left[\frac{1}{2}\left(c-\frac{\pi}{2}+dx\right), 2\right]}{5 a^2 d e^2 \sqrt{e \operatorname{Csc}[c+dx]} \sqrt{\operatorname{Sin}[c+dx]}} + \frac{4 \operatorname{Sin}[c+dx]}{3 a^2 d e^2 \sqrt{e \operatorname{Csc}[c+dx]}} - \frac{12 \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{5 a^2 d e^2 \sqrt{e \operatorname{Csc}[c+dx]}}$$

Result (type 5, 351 leaves):

$$\left(176 \sqrt{2} e^{-i(c+dx)} \sqrt{\frac{i e^{i(c+dx)}}{-1+e^{2i(c+dx)}}} \operatorname{Cos}\left[\frac{c}{2}+\frac{dx}{2}\right]^4 \operatorname{Csc}[c+dx]^{5/2} \right.$$

$$\left. \left(-1+e^{2i(c+dx)} + (1+e^{2ic}) \sqrt{1-e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, e^{2i(c+dx)}\right] \right) \right.$$

$$\left. \operatorname{Sec}[c+dx]^2 \right) / \left(5 d (1+e^{2ic}) (e \operatorname{Csc}[c+dx])^{5/2} (a+a \operatorname{Sec}[c+dx])^2 \right) +$$

$$\left(\operatorname{Cos}\left[\frac{c}{2}+\frac{dx}{2}\right]^4 \operatorname{Csc}[c+dx]^3 \operatorname{Sec}[c+dx]^2 \left(\frac{56}{3d} - \frac{8 \operatorname{Cos}[2c] \operatorname{Cos}[2dx]}{3d} + \frac{2 \operatorname{Cos}[3c] \operatorname{Cos}[3dx]}{5d} \right. \right.$$

$$\left. \left. \frac{(-129+47 \operatorname{Cos}[2c]) \operatorname{Cos}[dx] \operatorname{Sec}[c]}{5d} - \frac{94 \operatorname{Sin}[c] \operatorname{Sin}[dx]}{5d} + \frac{8 \operatorname{Sin}[2c] \operatorname{Sin}[2dx]}{3d} - \frac{2 \operatorname{Sin}[3c] \operatorname{Sin}[3dx]}{5d} \right) \right) / \left((e \operatorname{Csc}[c+dx])^{5/2} (a+a \operatorname{Sec}[c+dx])^2 \right)$$

Problem 306: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{(e \operatorname{Csc}[c+dx])^{7/2} (a+a \operatorname{Sec}[c+dx])^2} dx$$

Optimal (type 4, 172 leaves, 13 steps):

$$-\frac{4}{a^2 d e^3 \sqrt{e \operatorname{Csc}[c+dx]}} + \frac{26 \operatorname{Cos}[c+dx]}{21 a^2 d e^3 \sqrt{e \operatorname{Csc}[c+dx]}} + \frac{2 \operatorname{Cos}[c+dx]^3}{7 a^2 d e^3 \sqrt{e \operatorname{Csc}[c+dx]}} +$$

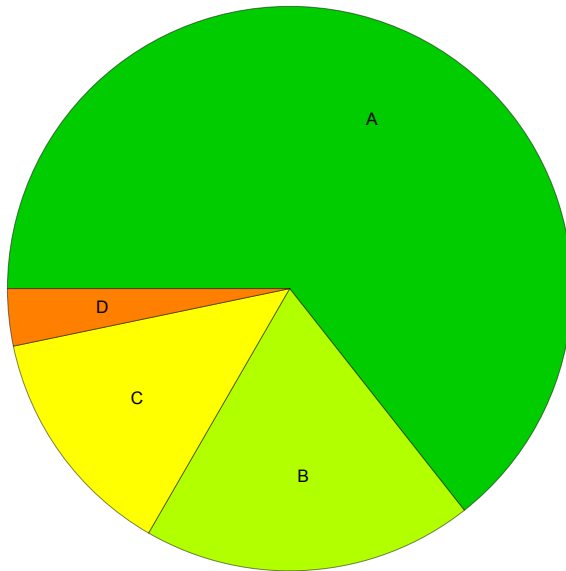
$$\frac{52 \operatorname{EllipticF}\left[\frac{1}{2}\left(c-\frac{\pi}{2}+dx\right), 2\right]}{21 a^2 d e^3 \sqrt{e \operatorname{Csc}[c+dx]} \sqrt{\operatorname{Sin}[c+dx]}} + \frac{4 \operatorname{Sin}[c+dx]^2}{5 a^2 d e^3 \sqrt{e \operatorname{Csc}[c+dx]}}$$

Result (type 4, 365 leaves):

$$\begin{aligned}
& \left(\cos \left[\frac{c}{2} + \frac{dx}{2} \right]^4 \operatorname{Csc}[c+dx]^4 \operatorname{Sec}[c+dx]^2 \right. \\
& \left(\frac{58 \cos[2dx] \sin[2c]}{21d} - \frac{2 \cos[dx] \operatorname{Sec}[c] (-520 \sin[c] + 357 \sin[2c])}{105d} - \right. \\
& \frac{4 \cos[3dx] \sin[3c]}{5d} + \frac{\cos[4dx] \sin[4c]}{7d} - \frac{4(-260 + 357 \cos[c]) \sin[dx]}{105d} + \\
& \left. \left. \frac{58 \cos[2c] \sin[2dx]}{21d} - \frac{4 \cos[3c] \sin[3dx]}{5d} + \frac{\cos[4c] \sin[4dx]}{7d} \right) \right) / \\
& \left((e \operatorname{Csc}[c+dx])^{7/2} (a + a \operatorname{Sec}[c+dx])^2 \right) - \left(104 \cos \left[\frac{c}{2} + \frac{dx}{2} \right]^4 \operatorname{Csc}[c+dx]^{7/2} \operatorname{Sec}[c+dx]^2 \right. \\
& \left(\frac{1}{d} 2 \sqrt{\operatorname{Csc}[c+dx]} \operatorname{EllipticF} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right), 2 \right] \sqrt{\sin[c+dx]} + (2 \cos[c+dx]^2 \operatorname{Sec}[c]) \right) / \\
& \left(d \sqrt{\operatorname{Csc}[c+dx]} \sqrt{(-1 + \operatorname{Csc}[c+dx]^2) \sin[c+dx]^2} \sqrt{1 - \sin[c+dx]^2} \right) \right) / \\
& \left(21 (e \operatorname{Csc}[c+dx])^{7/2} (a + a \operatorname{Sec}[c+dx])^2 \right)
\end{aligned}$$

Summary of Integration Test Results

306 integration problems



A - 197 optimal antiderivatives

B - 58 more than twice size of optimal antiderivatives

C - 41 unnecessarily complex antiderivatives

D - 10 unable to integrate problems

E - 0 integration timeouts